

# MathBook XML and APEX Calculus

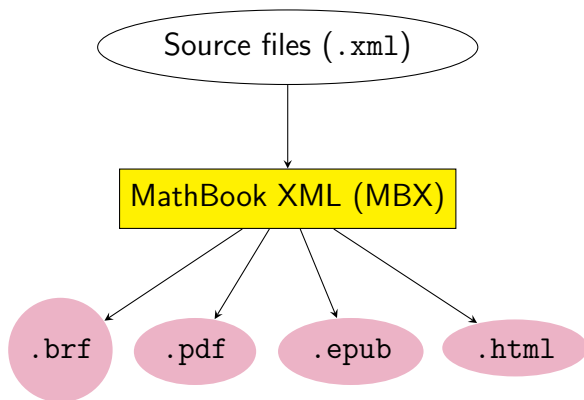
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alex.jordan@pcc.edu  
Mathematics Instructor  
Portland Community College

OER Symposium May 11<sup>th</sup>, 2017

# My introduction to MBX

- Met Rob Beezer of U. Puget Sound in June 2013.
- Rob explained a new-and-different approach to book-writing.
- Intriguing to fellow PCC instructor Chris Hughes and myself.
- Seed planted to use MBX for a precalculus text.

# What is MBX?



# Intimidated by XML

Wanted to learn  
MBX, but code  
was intimidating:

```
<section xml:id="section-function-basics">

  <title>The Basics of Function Vocabulary</title>

  <outcomes>
    <outcome>Understand the definition of a function.</outcome>
    <outcome>Use standard notation for functions correctly, and recognize
    <outcome>Recognize some real examples of functions in your life.</outcome>
  </outcomes>

  <sidebyside>
    <!-- <paragraphs valign="top" width="60%">-->
      <p valign="top" width="60%">Most of us are familiar with the <math>x^2</math>
    <!-- </paragraphs>-->

    <table xml:id="table-squareroots" valign="top" width="40%">
      <caption>Values of <math>\sqrt{x}</math></caption>
      <tabular halign="center">
        <thead />
        <row><cell><math>\sqrt{9}</math></cell><cell><math>{}=3</math></cell>
        <row><cell><math>\sqrt{\frac{1}{4}}</math></cell><cell><math>{}=\frac{1}{2}</math></cell>
        <row><cell><math>\sqrt{2}</math></cell><cell><math>{} \approx 1.414</math></cell>
        <tfoot />
      </tabular>
      <todo>Make better table</todo>
    </table>
```

# Intimidated by XSL

MBX itself's code  
even moreso:

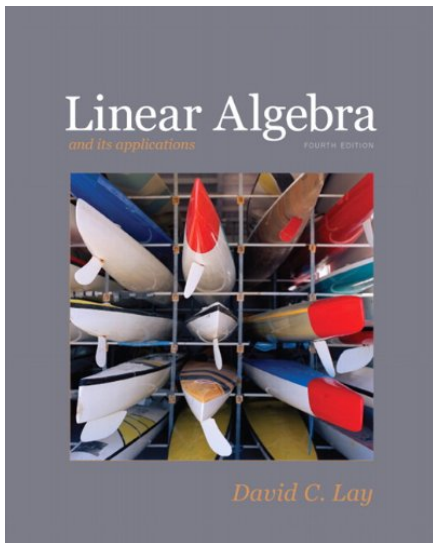
```
<xsl:template match="sidebyside">
  <xsl:text>\begin{figure}&#xa;</xsl:text>
  <xsl:text>\centering&#xa;</xsl:text>
  <xsl:apply-templates select="*[not(self::caption)]" mode="sidebyside">
  <!-- output the child nodes -->
  <xsl:text>\popValignCaptionBottom&#xa;</xsl:text>
  <!-- global caption -->
  <xsl:apply-templates select="caption" />
  <xsl:text>\end{figure}&#xa;</xsl:text>
</xsl:template>
```

```
<!-- vertical alignment of objects inside sidebyside -->
<xsl:template match="*" mode="sidebyside-subitem-valign">
  <!-- process the width attribute -->
  <xsl:variable name="width">
    <!-- the width of a <object/> inside a sidebyside is translated in
    a fraction of \textwidth
    we do this by stripping the % sign, and
    adding a leading .
    for example 50% is turned into .50\textwidth
    -->
    <xsl:choose>
      <xsl:when test="@width">
        <xsl:value-of select="substring-before(@width,'%')" />
      </xsl:when>
      <xsl:otherwise>
        <!-- default width is calculated by computing 100/(number of
        for example, if there are 4 figures, the default width
```

# A year and a half later...

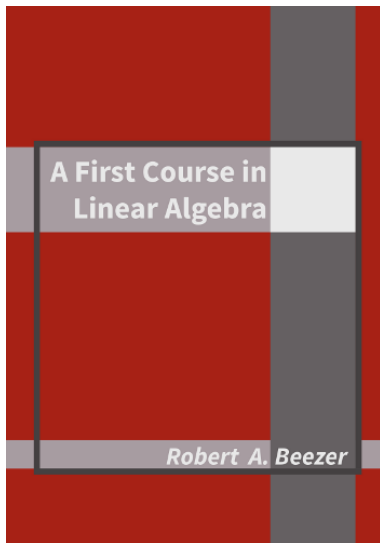
Great book, but too expensive: \$177.70 new at PCC bookstore.

For CC students, books are 30% of education expenses.



# Pitch Rob's book to colleagues

Free HTML, inexpensive physical, but is it good?

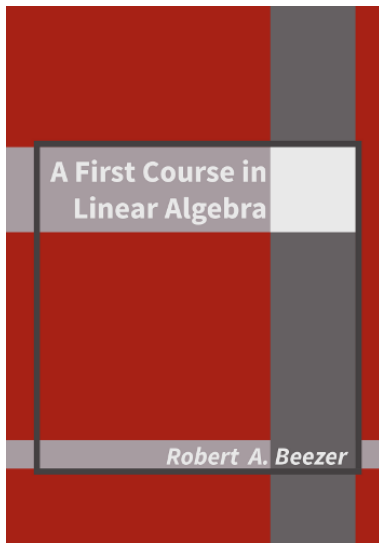


# Pitch Rob's book to colleagues

Free HTML, inexpensive physical, but is it good?

Yes!

But colleagues want more applications and some customization. . . perfect!





# Contribution to Rob's Book

Added  
a chapter.

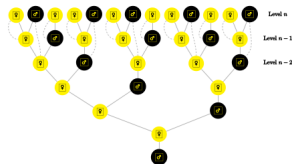
Learned MBX  
through this  
small, focused  
project.

Moved on with  
confidence.

QR (Gram-Schmidt) Decomposition
Singular Value Decomposition
Cholesky Decomposition
<b>3 Canonical Forms</b>
Generalized Eigenspaces
Nilpotent Linear Transformations
Jordan Canonical Form
<b>4 Applications</b>
Least Squares
Curve Fitting
<b>Linear Recurrence Relations</b>
Quadric Curves
<b>5 Topics</b>
Vandermonde Matrices
Determinants
<b>6 GNU Free Documentation License</b>

## Subsection 4.3.1 Examples

**Example 4.3.2 Honeybee Ancestors** . Male honeybees (also known as drones) hatch from unfertilized eggs, and so they have a mother but no father. Female honeybees (both queens and workers) hatch from fertilized eggs, and so each female honeybee has two parents (one of each sex). This leads to an interesting family tree for any single honeybee. If we consider a male, he only has one parent. That parent must have been female, so our male had two grandparents. As we continue to count, we will ignore any possibility for tangled family trees, which is admittedly unrealistic. Figure 4.3.3 displays the bees family tree going back several generations.



# Calculus Lab Manual

## PCC's calculus I lab manual.

### Activity 10

Many limit values do not exist. Sometimes the non-existence is caused by the function value either increasing without bound or decreasing without bound. In these special cases we use the symbols  $\infty$  and  $-\infty$  to communicate the non-existence of the limits. Figures 10.1-10.3 can be used to illustrate some ways in which we communicate the non-existence of these type of limits.

In Figure 10.1 we could (correctly) write  $\lim_{x \rightarrow 2} k(x) = \infty$ ,  $\lim_{x \rightarrow 2^-} k(x) = \infty$ , and  $\lim_{x \rightarrow 2^+} k(x) = \infty$ .

In Figure 10.2 we could (correctly) write  $\lim_{t \rightarrow 4} w(t) = -\infty$ ,  $\lim_{t \rightarrow 4^-} w(t) = -\infty$ , and  $\lim_{t \rightarrow 4^+} w(t) = -\infty$ .

In Figure 10.3 we could (correctly) write  $\lim_{x \rightarrow -3^-} T(x) = \infty$  and  $\lim_{x \rightarrow -3^+} T(x) = -\infty$ . There is no shorthand way of communicating the non-existence of the two sided limit  $\lim_{x \rightarrow -3} T(x)$ .

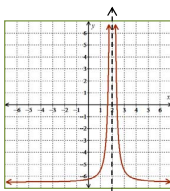


Figure 10.1:  $k$   $x = 2$

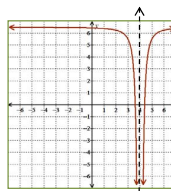


Figure 10.2:  $w$   $t = 4$

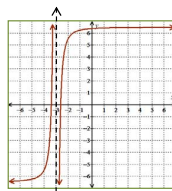


Figure 10.3:  $T$   $x = -3$

### Problem 10.1

Draw onto Figure 10.4 a single function  $f$  that satisfies each

# Calculus Lab Manual

PCC's calculus I  
lab manual.

Not ADA accessi-  
ble, hard to up-  
keep, and could  
have better fea-  
tures in HMTL.

## Activity 10

Many limit values do not exist. Sometimes the non-existence is caused by the function value either increasing without bound or decreasing without bound. In these special cases we use the symbols  $\infty$  and  $-\infty$  to communicate the non-existence of the limits. Figures 10.1-10.3 can be used to illustrate some ways in which we communicate the non-existence of these type of limits.

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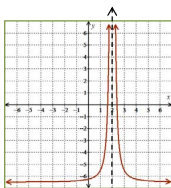


Figure 10.1:  $k$   $x = 2$

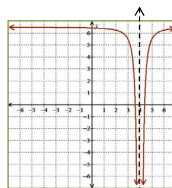
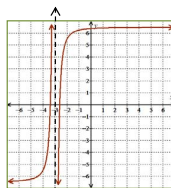


Figure 10.2:  $w$   $t = 4$



$x = -3$  Figure 10.3:  $T$

## Problem 10.1

Draw onto Figure 10.4 a single function  $f$  that satisfies each

# XML conversion

## Converted to MBX.

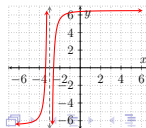
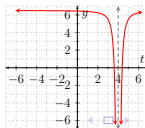
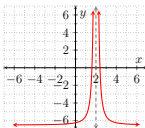
### ACTIVITY 2.7. NON-EXISTENT LIMITS

19

#### 2.7 Non-existent Limits

Many limit values do not exist. Sometimes the non-existence is caused by the function value either increasing without bound or decreasing without bound. In these special cases we use the symbols  $\infty$  and  $-\infty$  to communicate the non-existence of the limits. Figures 2.7.1–2.7.3 can be used to illustrate some ways in which we communicate the **non-existence** of these types of limits.

- In Figure 2.7.1 we could (correctly) write  $\lim_{x \rightarrow 2} k(x) = \infty$ ,  $\lim_{x \rightarrow 2^-} k(x) = \infty$ , and  $\lim_{x \rightarrow 2^+} k(x) = \infty$ .
- In Figure 2.7.2 we could (correctly) write  $\lim_{t \rightarrow 4} w(t) = -\infty$ ,  $\lim_{t \rightarrow 4^-} w(t) = \infty$ , and  $\lim_{t \rightarrow 4^+} w(t) = -\infty$ .
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# XML conversion

Converted to MBX.

Fall 2015: tablet students can stop purchasing print. All students can use extra HTML features. HTML version is ADA accessible.

Limits at Infinity Tending to Zero
Ratios of Infinities
<b>Non-existent Limits</b>
Vertical Asymptotes
Continuity
Discontinuities
Continuity on an Interval
Discontinuous Formulas
Piecewise-Defined Functions
<b>3 Introduction to the First Derivative</b>
Instantaneous Velocity
Tangent Lines
The First Derivative
Derivative Units
<b>4 Functions, Derivatives, and Antiderivatives</b>
Graph Features
Graphical Derivatives
Nondifferentiability
Higher-Order Derivatives

## Activity 2.7 Non-existent Limits

Many limit values do not exist. Sometimes the non-existence is caused by the function value either increasing without bound or decreasing without bound. In these special cases we use the symbols  $\infty$  and  $-\infty$  to communicate the non-existence of the limits. Figures 2.7.1–2.7.3 can be used to illustrate some ways in which we communicate the *non-existence* of these types of limits.

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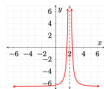


Figure 2.7.1.  
 $y = k(x)$

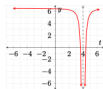


Figure 2.7.2.  
 $y = w(t)$

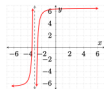


Figure 2.7.3.  
 $y = T(x)$

# WeBWorK

WeBWorK is an open-source online homework systems, with a library of 35,000 homework exercises.

A closer simulation of human instructor feedback.

Entered	Answer Preview	Result	Messages
$t^{112}$	$t^{112}$	incorrect	When multiplying terms with the same base, you do not multiply the exponents.

The answer above is NOT correct.

(1 point) **BasicAlgebra/Exponents**  
**/exponentsMultiplication0.pg**

Use the properties of exponents to simplify the following

$$t^8 \cdot t^{14}$$



**Solution:**

# WeBWorK

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Entered	Answer Preview	Result	Messages
12	12	incorrect	You have the solution, but the answer to this question should be in the form $z = \underline{\quad}$

The answer above is NOT correct.

(1 point) **BasicAlgebra/SolveLinearEquations**

**/solveLinearEqnOneStepMultiDiv10.pg**

Solve the following linear equation; the answer could be in the form  $z = \underline{\quad}$ , no solution, or all real numbers.

$$7z = 84$$



**Solution:**  
.....

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Entered	Answer Preview	Result	Messages
25		incorrect	Your answer doesn't look like a number with units
75		incorrect	Your answer doesn't look like a number with units

At least one of the answers above is NOT correct.

(1 point) **BasicAlgebra/Geometry**  
**/RectanglePerimeterEquation20.pg**

A rectangle's perimeter is 200 cm. Its length is 3 times as long as its width. Use an equation to find the rectangle's length and width.

Its width is  .

Its length is  .

**Solution:**



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Entered	Answer Preview	Result	Messages
<code>[-inf,inf]</code>		incorrect	Infinite endpoints must be open

The answer above is NOT correct.

(1 point) **BasicAlgebra/LinearInequalities**

**/SolveSpecialInequality30.pg**

Solve this inequality.

- Use interval notation in your response.
- If there is no solution, you may enter **no solution**.
- If the solution set is all real numbers, you may enter **(-inf, inf)** or **all real numbers**.

$$-10 + 4x + 17 \geq 4x + 7$$



**Solution:**

.....

# WeBWorK

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Entered	Answer Preview	Result	Messages
$(y^2)+9*y+8$	$y^2 + 9y + 8$	incorrect	Your answer is equivalent to the polynomial in the correct answer, but not completely factored or simplified

The answer above is NOT correct.

(1 point) **BasicAlgebra/Factoring/factoring170.pg**

Factor the given polynomial

$$y^2 + 9y + 8 = \text{y}^2+9y+8$$

If the expression cannot be factored then answer with **prime**.

**Solution:**  
.....

# WeBWorK and MBX

What if WeBWorK and MBX had a bridge?

Idea: WeBWorK cells in an HTML page, contacting a WeBWorK server for interactive feedback.

Either specify an OPL problem in the source, or make building block WeBWorK code templates.

**Exercise 5** This is just a prototype test of an embedded WeBWorK problem. It still has issues. .

**WeBWorK Editor using host:**

**[https://hosted2.webwork.rochester.edu/mod\\_xmlrpc](https://hosted2.webwork.rochester.edu/mod_xmlrpc),  
format: simple**

(1 point) Library/ASU-topics/setCalculus/stef/stef3\_7p1\_mo.pg

Let

$$f(x) = 3x^3 + 8x - 5$$

Use the limit definition of the derivative to calculate the derivative of  $f$ :

$$f'(x) = \text{[input box]}$$

Use the same formula from above to calculate the derivative of this new function (i.e. the second derivative of  $f$ ):

$$f''(x) = \text{[input box]}$$

Proof of concept built by Mike Gage.

# WeBWork and MBX

What if WeBWork and MBX had a bridge?

Idea: WeBWork cells in an HTML page, contacting a WeBWork server for interactive feedback.

Either specify an OPL problem in the source, or make building block WeBWork code templates.

**Exercise 5** This is just a prototype test of an embedded WeBWork problem. It still has issues. .

**WeBWork Editor using host:**

**[https://hosted2.webwork.rochester.edu/mod\\_xmlrpc](https://hosted2.webwork.rochester.edu/mod_xmlrpc),  
format: simple**

(1 point) Library/ASU-topics/setCalculus/stef/stef3\_7p1\_mo.pg

Let

$$f(x) = 3x^3 + 8x - 5$$

Use the limit definition of the derivative to calculate the derivative of  $f$ :

$$f'(x) = \text{[input box]}$$

Use the same formula from above to calculate the derivative of this new function (i.e. the second derivative of  $f$ ):

$$f''(x) = \text{[input box]}$$

submit answers

Proof of concept built by Mike Gage.  
Thanks to OpenOregon funding in 2015, we built it.

# APEX and Active

Our HECC grant:  
convert APEX Calculus  
and Active Calculus to  
MBX.

Two strong OERs in  
calculus: relatively  
mature and widely  
adopted already as far as  
calculus OERs go.

**APEX**  
**CALCULUS**  
Version 3.0

by Gregory Hartman

**ACTIVE CALCULUS**  
2016 Edition

by Matt Boelkins

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Two strong OERs in  
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calculus OERs go.

These are *much* bigger  
projects!

**APEX**  
**CALCULUS**  
Version 3.0

by Gregory Hartman

**ACTIVE CALCULUS**  
2016 Edition

by Matt Boelkins

# Future Work

This year has been about converting APEX and Active, not enhancing them.

More features to leverage:

- GeoGebra embeddings
- Sage cells
- YouTube videos
- Desmos graphing calculator

# Getting Started

Getting started with using MathBook XML and/or WeBWork is much easier if you have an experienced person to guide you. But here are some general resources, and with determination and grit, these will get you started too.

- MathBook XML home page, with documentaiton, getting started guide, and more
- Alternative guide to get started with an existing MBX project
- Information on WeBWork