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Formalizing the Panarchy Adaptive Cycle with the Cusp Catastrophe

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Computational Social Science

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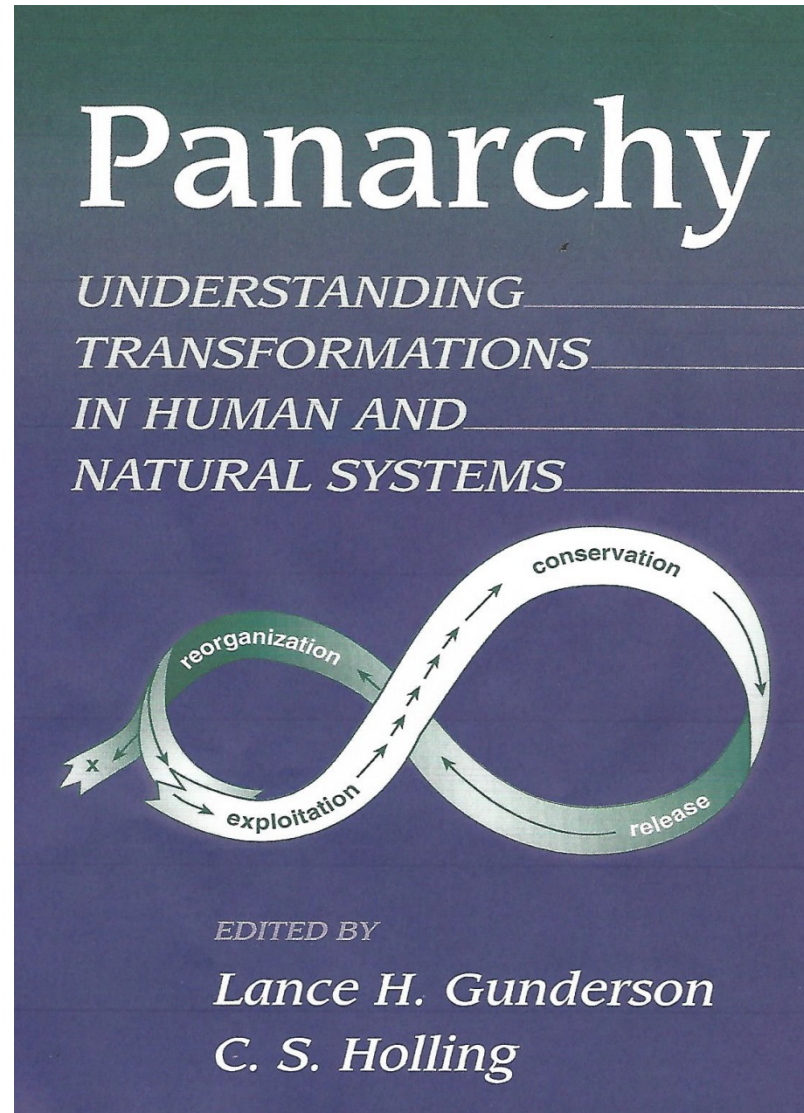
Abstract

The panarchy **adaptive cycle**, a general model for change in natural and human systems, can be **formalized** by the **cuspid catastrophe** of René Thom's topological theory. Both the adaptive cycle and the cuspid catastrophe have been used to model **ecological** and **socio-economic** systems in which slow & small continuous changes in two control variables produce fast & large discontinuous changes in system behavior. The panarchy adaptive cycle has been used so far only for **qualitative** descriptions of typical dynamics of such systems. The cuspid catastrophe, while also often employed qualitatively, is a mathematical model capable of being used **quantitatively**.

If the control variables from the adaptive cycle are taken as the parameters in the equation for the cuspid catastrophe, **a cycle very similar to the adaptive cycle can be constructed**. Formalizing the panarchy adaptive cycle with the cuspid catastrophe may provide direction for more rigorous applications of the adaptive cycle, thereby augmenting its usefulness in guiding sustainability efforts.

- Adaptive Cycle
- Cusp Catastrophe
- Modeling Adaptive Cycle with the Cusp
- Discussion

Adaptive Cycle



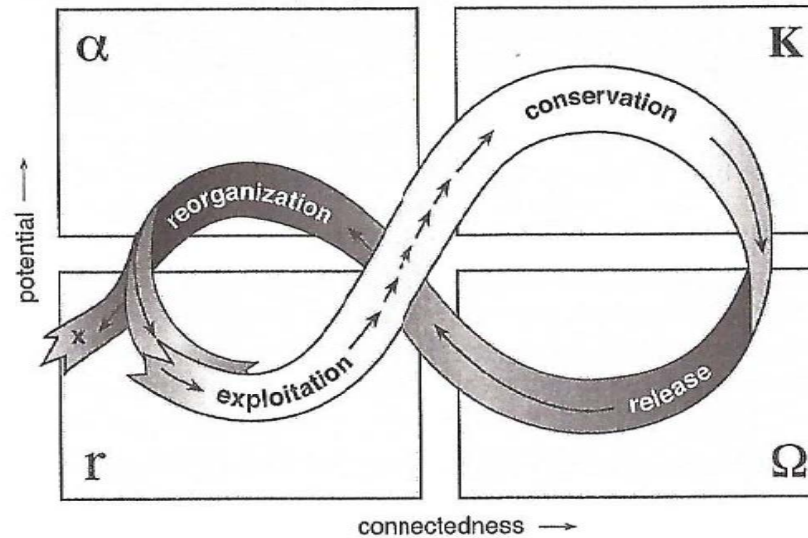
Adaptive Cycle

- Theory developed by Holling & colleagues
- Applicable to **ecological** & **socio-economic** systems
- AC is a three-variable model
- Potential = function(connectedness, resilience)

- **Potential** = ‘capital’ of system, e.g., biomass, assets
- **Connectedness** = strength, pervasiveness of network of relations
- **Resilience** = basin structure of dynamic system => basin stability
 - Closeness of attractor to basin boundary, size of basin, etc.

- AC is “**archetypal**” behavior, but other behaviors are possible
- “Panarchy” applies the AC to multiple **spatial-temporal scales**
- AC is an extension of familiar **S-shaped** (r-K) **growth** model

Adaptive Cycle



- G&H, p.34: P, potential; C, connectedness; R = resilience
- **r-phase** (*exploitation*): Exponential increase of dominant species: C ↑, P ↑, R ↑
- **K-phase** (*conservation*): Complexification; C ↑ (until **over-connected**), P ↑↓ (peaks), R ↓
- **Ω-phase** (*release*): Collapse: C ↓, P (**major** drop) ↓
- **α-phase** (*reorganization*): “Hundred flowers blossom”: C ↓, P ↑↓ (minor drop), R ↑

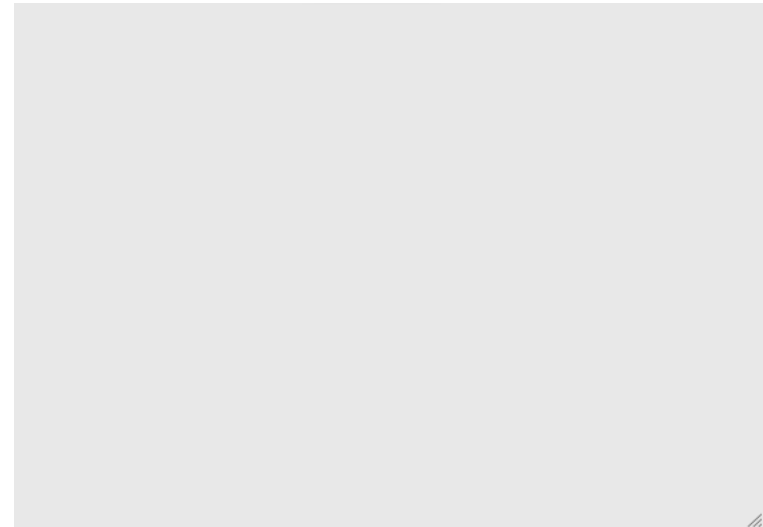
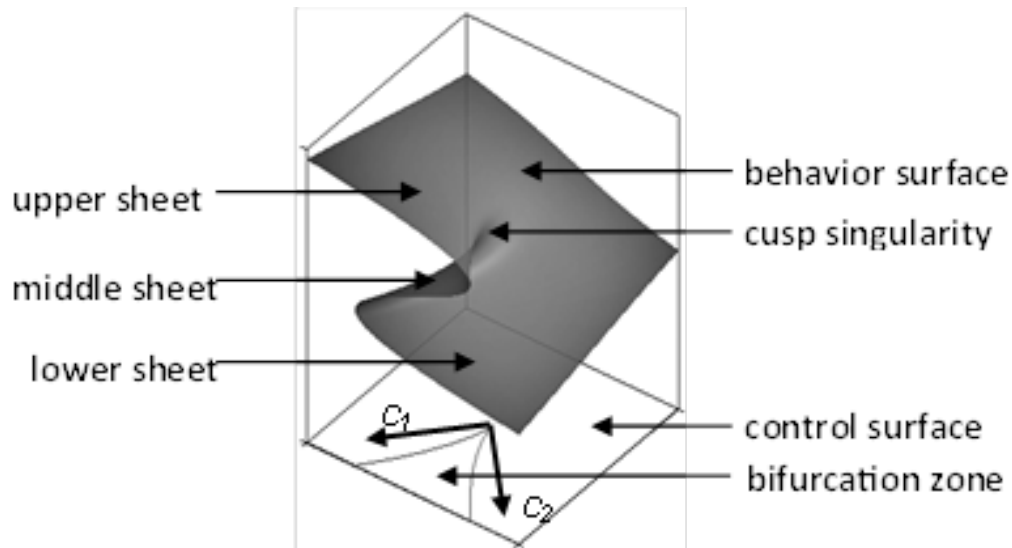
Cusp Catastrophe

- Part of Rene Thom's catastrophe theory
 - Popularized by E.C. Zeeman
- Applicable to systems of widely differing type in natural/social sciences
- Theory rigorously applies only to gradient systems, $dy/dt = -k dV/dy$
 - y is state ("behavior," "effect") variable or vector
 - V is "potential" – **NOT** related to "potential" of AC
 - $V = V(y, x)$, where x is a control ("causal") parameter or vector of parameters
- This is a topological theory
 - Applies only "**near**" the singularity
 - Equilibrium surfaces can be **stretched** but not torn. (Will use this later...)
 - **Topological** character makes **empirical testing difficult** but **not impossible**

Cusp Catastrophe

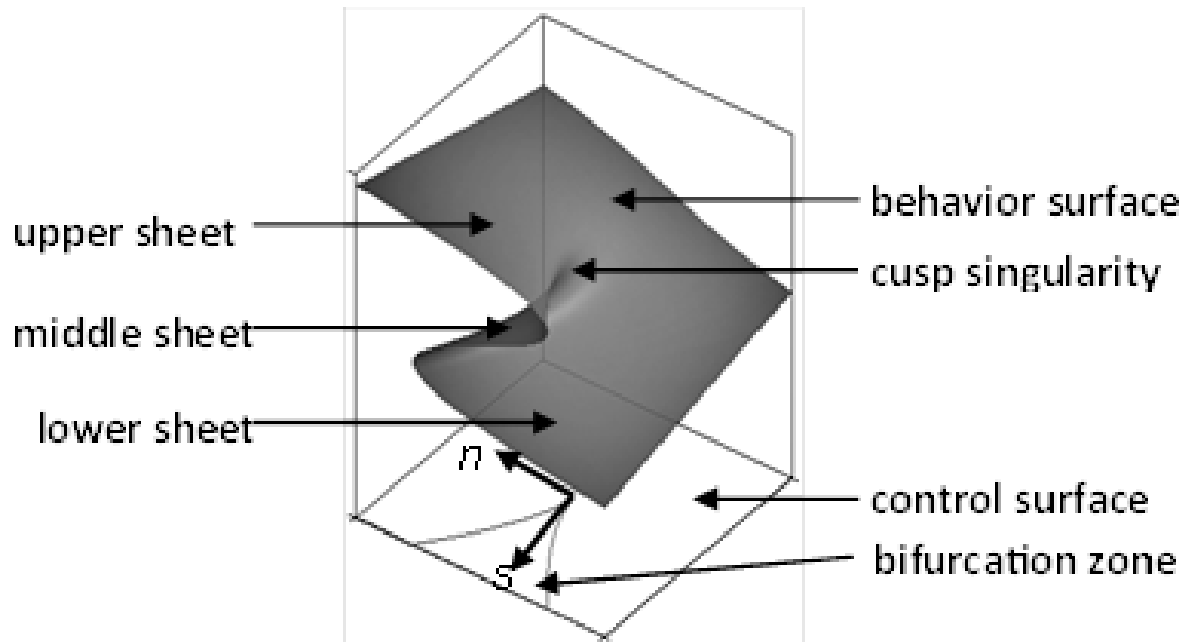
- Cusp catastrophe is an “elementary” catastrophe; these ECs are limited to ≤ 5 control parameters
- Cusp is a three-variable (2 control parameters) model: y, n, s
- **Potential**, V , that is maximized/minimized by **gradient system** is:
- $V = \frac{1}{4} y^4 - n y - \frac{1}{2} s y^2$
 - 1 behavior (effect) variable, y
 - 2 control (causal) parameters, n & s , normal & splitting factors
- Alternative control parameters: conflicting factors c_1 & c_2 , which are sum & difference of n & s
- **Behavior (equilibrium) surface**: $dy/dt = dV/dy = 0 = y^3 - n - s y$
- Behavior surface is bimodal, with a 3rd inaccessible surface

Cusp Catastrophe



- Vertical dimension = behavior variable, y
- Control parameters = **conflicting factors** c_1 & c_2
- Behavior (equilibrium) point always above control point

Cusp Catastrophe



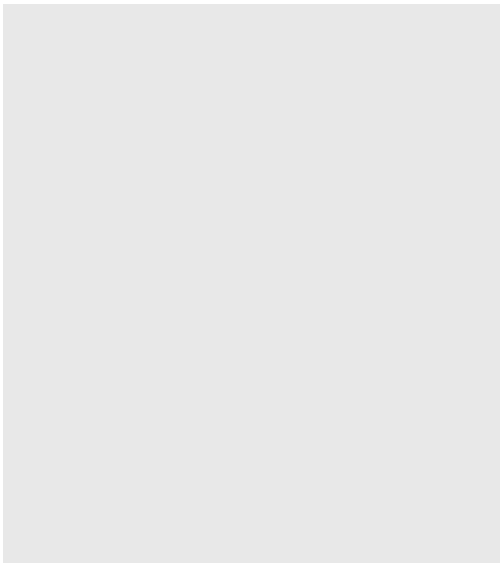
- Vertical dimension = behavior variable, y
- Control parameters = **normal & splitting** factors, n & s

Cusp Catastrophe

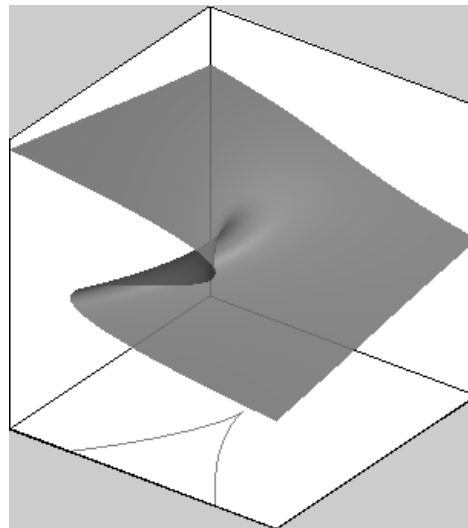
- **User** (*not* catastrophe theory) specifies trajectory of **control** parameters
 - In applying CC to AC, we'll assume elliptical trajectory
 - Alternatively, a back-and-forth trajectory would show hysteresis
- **Catastrophe theory** then specifies motion of **state variable** above the control point on behavior surface
- Basic CT dynamics can be augmented by
 - Stochasticity of control or behavior point
 - Feedback of state variable, y , on control parameters, x

Cusp Catastrophe

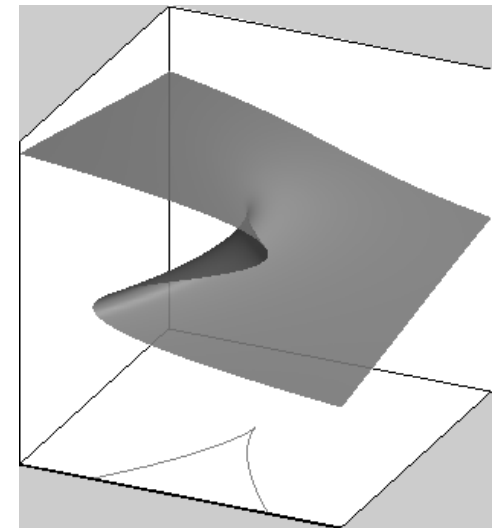
- **Simulations:** user-specified trajectories (green) & resulting behavior (red)
- For motion in normal direction, back-and-forth generates **hysteresis**
- **Splitting**



Normal



Cyclic

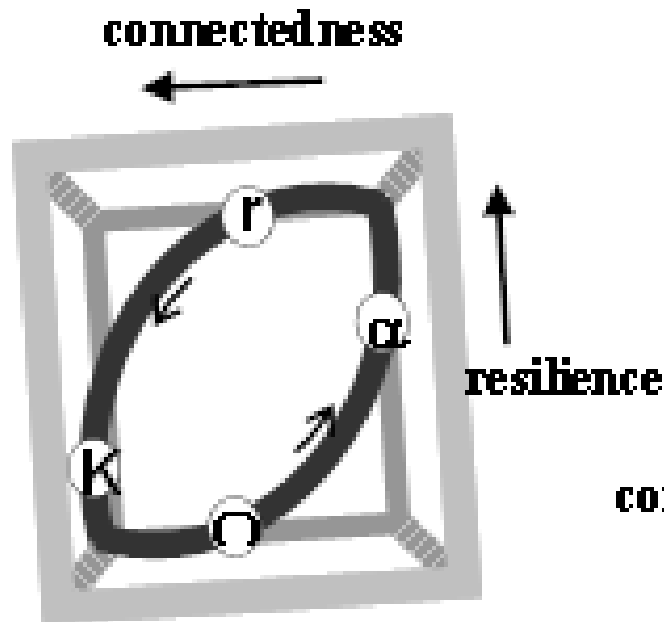


Modeling the AC with the CC

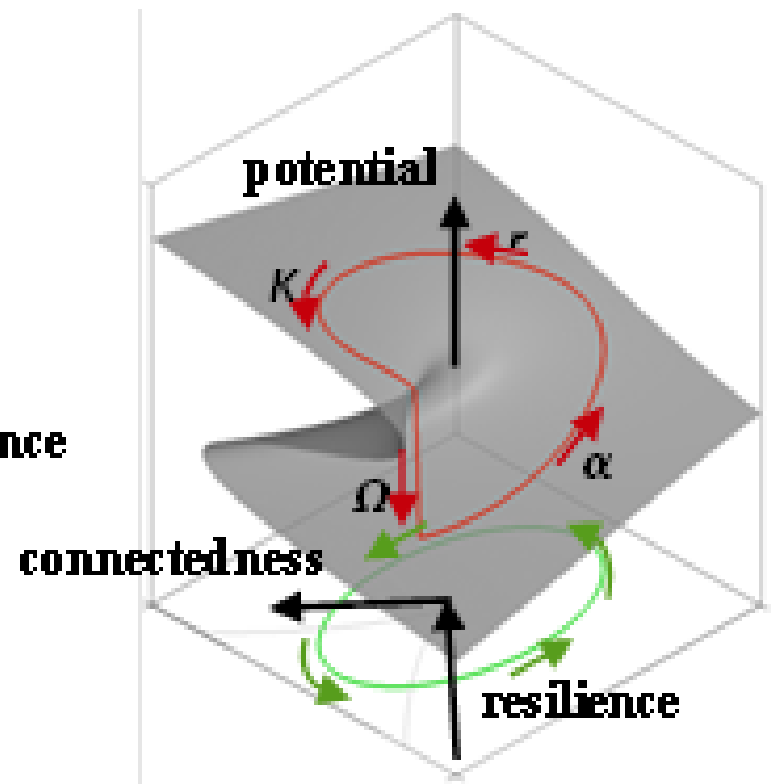
- Both AC and CC have 1 effect and 2 cause variables
- In both, continuous causal change => discontinuous effects
- Take AC potential as the behavior variable and connectedness, resilience as the control parameters of the Cusp
- Assume elliptical control point trajectory (or similar closed path)

Modeling the AC with the CC

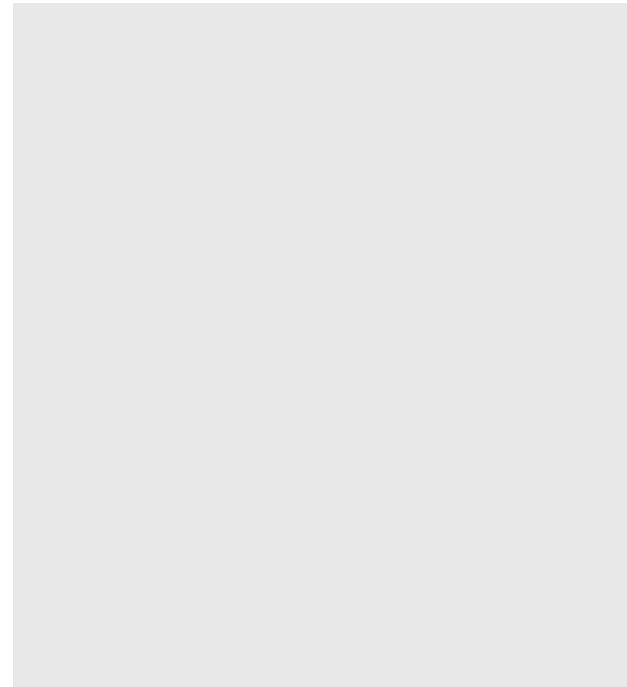
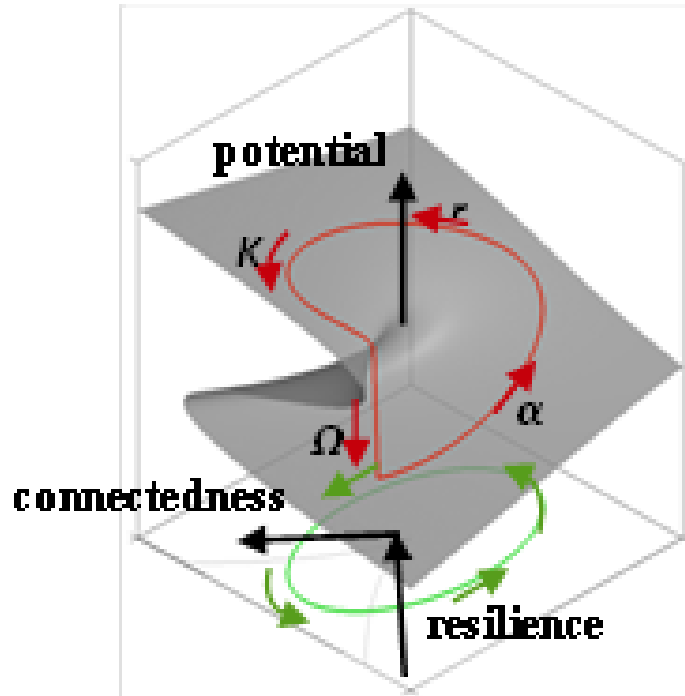
Adaptive cycle



**Modeled with
cusp catastrophe**

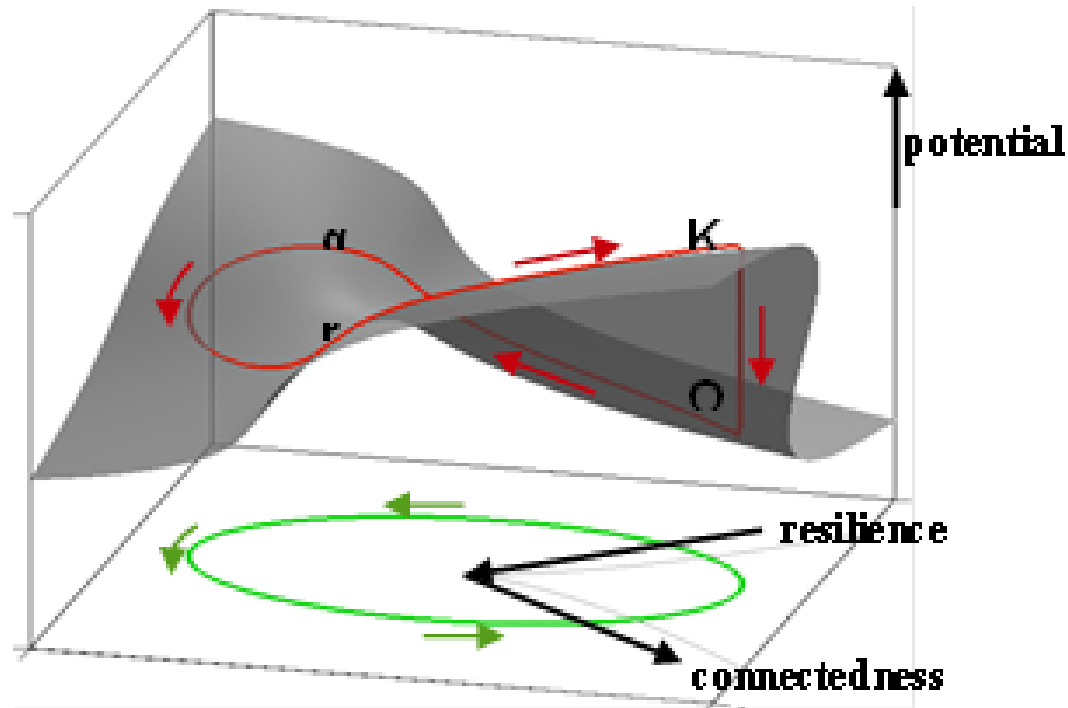


Simulating the AC with the CC



Modeling the AC with the CC

Taking advantage of **topological** character of theory:
adding **2nd** (less prominent in AC theory) **drop in potential** in α -phase



Discussion

- Modeling AC with Cusp **implicit** (but *not* explicit) in Gunderson & Holling book: Scheffer et al (e.g., p. 207) refer to & show “catastrophic folds,” which exhibit hysteresis (stress = normal factor):

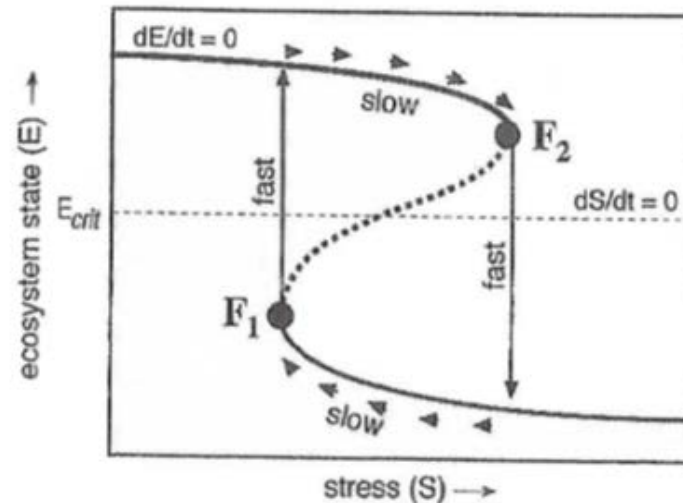


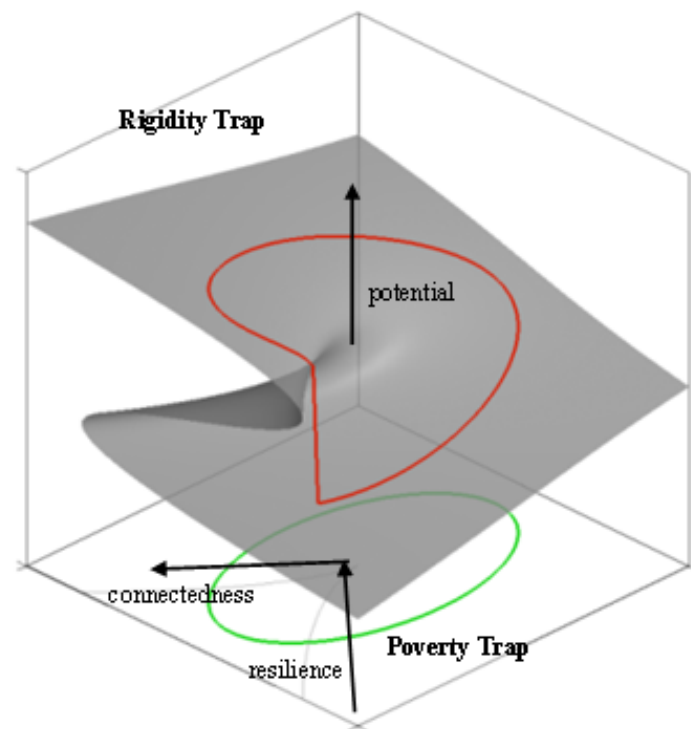
Figure 8-5. Cycles can occur if stress (S) responds in a dynamic way to ecosystem state such that below a critical level of the state indicator (E_{crit}), stress decreases slowly, whereas above that level, it increases.

Discussion

- Also, spruce budworm model by Holling and other ecological models explicitly use CT
- While **other frameworks might formalize** AC, CC is a “**natural**” way of doing so
- Why didn't G&H propose this? We don't know, but...
- **Controversy** over catastrophe theory (over-reaction to hype by Zeeman) may account for non-explicitness in G&H

Discussion

- Other paths/locations of CC control point might help model other (non-archetypal) possibilities discussed in panarchy literature:
- “poverty trap”: low connectedness, resilience, & potential
- “rigidity trap”: high connectedness, resilience, & potential



Discussion

- **Conclusion:** Comparison of the panarchy adaptive cycle, a general model of change in natural and human systems, with the cusp catastrophe shows that **the adaptive cycle can be formalized by this elementary catastrophe**. Other ways of formalizing the adaptive cycle are **possible**, but the widespread use of the cusp in ecological modeling makes this a **natural approach** to formalization.
- By using the control variables from the adaptive cycle as parameters in the behavior equation for the cusp catastrophe, a **cycle very similar to the adaptive cycle can be constructed**. Modeling the adaptive cycle with the cusp may provide direction for more **rigorous** and **diverse** applications of the panarchy framework.

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- Thank you
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