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# Reconstructability Analysis and Its Occam Implementation

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# Reconstructability Analysis & Its Occam Implementation

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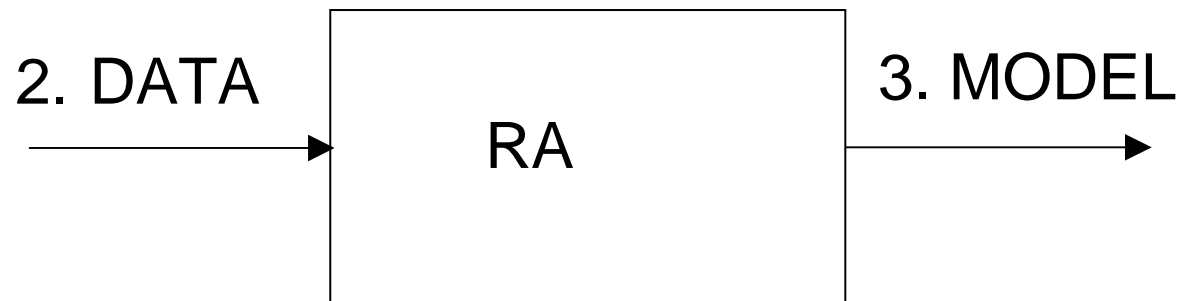
[http://www.pdx.edu/sysc/research\\_dmm.html](http://www.pdx.edu/sysc/research_dmm.html)

ICCS 2020, July 29

# 1. Introduction: what is RA

2. Input data to RA

3. Output model from RA



## ***INTRODUCTION: WHAT IS RA?***

- **Reconstructability Analysis** (RA) = a probabilistic graphical modeling methodology
- RA = Information theory + Graph theory
- Graphs, applied to data, are **models**:
- node = variable; link = relationship
- RA uses not only graphs (a link joins 2 nodes), but hypergraphs (a link can join **>2** nodes)

## ***WHY RA MIGHT BE OF INTEREST*** <sup>1/2</sup>

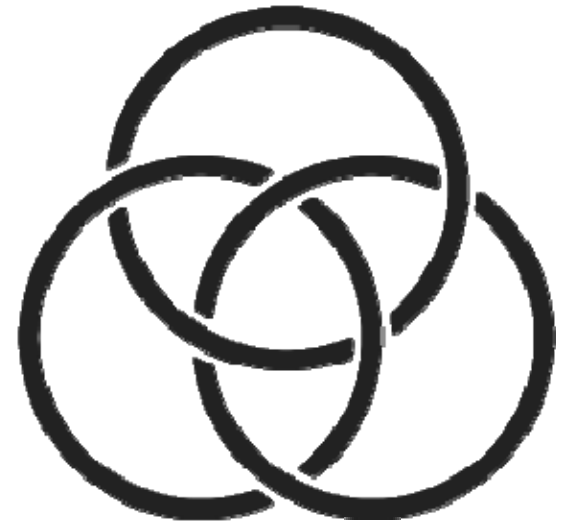
- Can detect **many-variable** or **non-linear** interactions not hypothesized in advance, i.e., it is explicitly designed for **exploratory** search
- **Transparent** -- not a black box like deep learning NNs
- Easily **interpretable & communicable**
- Designed for **nominal** variables
- Can also analyze **continuous** variables via **binning**
- **Prediction**/classification, **clustering**/network models
- **Time series, spatial** analyses
- Overlaps common **statistical & machine-learning** methods, but has unique features

## ***WHY RA MIGHT BE OF INTEREST*** 2/2

- Analyses at **3 levels of refinement**:
  - coarse (very fast, in principle *many* variables)
  - fine (slower, 100s of variables) (~500 is max so far)
  - ultra-fine (slow, < 10 variables)
- **Standard application**: frequency data  $f(A_i, B_j, C_k, Z_l)$
- Variety of **non-standard capabilities**
  - Data: set-theoretic relations & mappings
  - Predict continuous dependent variables
  - Integrate multiple inconsistent data sets (not yet in Occam)
  - Regression-like Fourier version (not yet in Occam)

## ***OCCAM, SOFTWARE FOR RA***

- OCCAM, developed by Systems Science Program, Portland State University, is now **open source**
- <https://www.occam-ra.io/>
- [github.com/occam-ra/occam](https://github.com/occam-ra/occam)
- Contact me if you want to become involved:
- zwick@pdx.edu



# RA (DMM) WEB PAGE

<http://pdx.edu/sysc/research-discrete-multivariate-modeling>

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PSU » System Science » Research » Research: Discrete Multivariate Modeling

## Research: Discrete Multivariate Modeling

The methods used are also known in the systems literature as "reconstructability analysis" (RA). RA overlaps significantly with the fields of logic design and machine learning and with log-linear statistical modeling. The papers "Wholes and Parts in General Systems Methodology" and "An Overview of Reconstructability Analysis" listed below offer a concise review of RA methodology.

### Projects

Theory/Methodology

**OCCAM: RA software for data analysis & data mining**

- [Occam3](#) (web accessible; try it out)
- [User manual \(PDF\)](#)

**EDA: Extended Dependency Analysis**

Heuristic RA search for loopless models.

- [Download executable, sample files, and documentation](#) (for Windows)

RA utility programs

Below is the lattice of structures for a 4-variable *directed* system with 1 dependent variable (output).  
Boxes = relations; lines = variables;  
bold lines = the dependent variable.



# ***PAST RA APPLICATIONS***

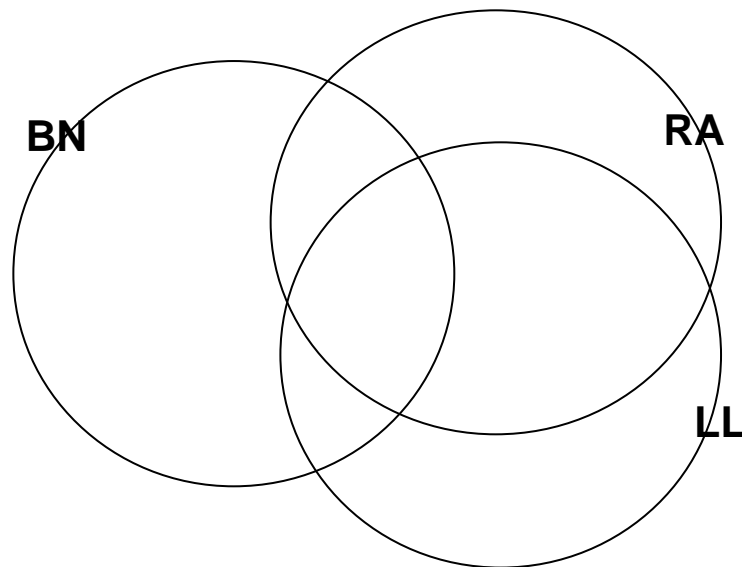
- ***BIOMEDICAL***  
Gene-disease association, disease risk factors, gene expression, health care use & outcomes, **dementia**, diabetes, heart disease, prostate cancer, brain injury, primate health, surgery
- ***FINANCE-ECONOMICS-BUSINESS***  
Stock market, bank loans, credit decisions, apparel analyses, market segmentation
- ***SOCIAL-POLITICAL-ENVIRONMENTAL***  
Socio-ecological interactions, wars, urban water use, rainfall, forest attributes
- ***MATH-ENGINEERING***  
Logic circuits, automata dynamics, genetic algorithm & neural network preprocessing, chip manufacturing, pattern recognition, decision analysis
- ***OTHER***  
Textual analysis, language analysis

# ***OVERLAP WITH STATISTICAL, ML METHODS***

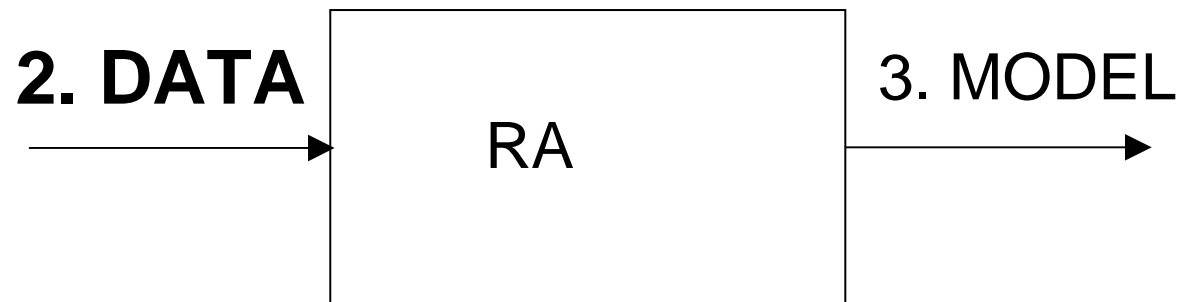
Closely related to other PGM methods, e.g., **log linear** (LL) (& logistic regression) models & **Bayesian networks** (BN)

Where methods overlap, they're **equivalent**

These PGM methods totally **different** from **neural nets**



1. Introduction: what is RA
- 2. Input data to RA**
3. Output model from RA



# ***FORM OF DATA***

## *Variables*

- Type: **nominal**; **bin** if continuous (continuous DV needn't be binned)
- Number: few variables to 100s (in principle >1000s coarse analysis)

## Data analysis

### *directed system*

- IV-DV distinction: *predict/classify* a DV from IVs

### *neutral system*

- No IV-DV distinction: model association, **clustering**

# FORM OF DATA

- frequency( $A_i, B_j, C_k, Z_l$ ) or individual cases

|       |       |       |       | frequency |
|-------|-------|-------|-------|-----------|
| $A_0$ | $B_0$ | $C_0$ | $Z_0$ | 13        |
| $A_0$ | $B_0$ | $C_0$ | $Z_1$ | 2         |
| $A_0$ | $B_0$ | $C_1$ | $Z_0$ | 9         |
| $A_0$ | $B_0$ | $C_1$ | $Z_1$ | 11        |
| ...   | ...   | ...   | ...   | —         |
|       |       |       |       | N         |

N = sample size

|                   | A     | B     | C     | Z     |
|-------------------|-------|-------|-------|-------|
| case <sub>1</sub> | $A_0$ | $B_0$ | $C_0$ | $Z_0$ |
| case <sub>2</sub> | $A_1$ | $B_2$ | $C_3$ | $Z_1$ |
| ...               |       |       |       |       |
| case <sub>N</sub> | $A_0$ | $B_0$ | $C_0$ | $Z_0$ |

Cases are indexed by  
 individual (in a population),  
 time, or  
 space

$$\text{frequency}(ABCZ) / N = p_{\text{data}}(ABCZ)$$

# OCCAM input file, **DATA** CASES INDEXED BY **INDIVIDUAL**

ID ,413,0,ID #Index specifying individual  
 APOE ,2,1,Ap  
 Gender ,2,1,Sx  
 Education ,3,1,Ed  
 AgeLastExam ,3,1,Ag  
 rs1801133 ,3,1,A  
 rs3818361 ,4,1,B  
 rs7561528 ,3,1,C  
 rs744373 ,3,1,D  
 rs6943822 ,3,1,E  
 rs4298437 ,3,1,F  
 rs7012010 ,3,1,G  
 rs11136000 ,3,1,H  
 rs10786998 ,4,1,J  
 rs11193130 ,4,1,K  
 rs610932 ,3,1,L  
 rs3851179 ,3,1,M  
 rs3764650 ,4,1,N  
 rs3865444 ,4,1,P  
 Dementia ,2,2,Z

**DEMENTIA EXAMPLE**  
 Z = 0 no disease; Z = 1 disease

| #ID | Ap | Sx | Ed | Ag | A | B | C | D | E | F | G | H | J | K | L | M | N | P | Z |
|-----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 101 | 0  | 0  | 2  | 2  | 1 | 1 | 0 | 1 | 2 | 2 | 1 | 1 | 2 | 0 | 1 | 1 | 2 | 2 | 1 |
| 103 | 0  | 0  | 2  | 1  | 0 | 2 | 2 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 1 | 1 | 0 | 1 | 0 |
| 111 | 0  | 1  | 2  | 1  | 2 | 2 | 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 2 | 2 | 0 | 1 | 0 |
| 112 | 0  | 0  | 2  | 2  | 2 | 2 | 1 | 1 | 1 | 2 | 1 | 1 | 0 | 2 | 2 | 0 | 0 | 2 | 0 |
| 118 | 0  | 1  | 0  | 2  | 2 | 2 | 2 | 0 | 0 | 1 | 1 | 1 | . | . | 1 | 1 | 0 | 2 | 0 |
| 120 | 0  | 1  | 2  | 2  | 1 | 2 | 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 1 | 2 | 0 | . | 1 |
| 121 | 0  | 0  | 2  | 2  | 2 | 2 | 1 | 1 | 2 | 0 | 0 | 0 | 2 | 0 | 1 | 1 | 1 | . | 1 |
| 122 | 0  | 0  | 1  | 2  | 1 | 2 | 1 | 1 | 2 | 0 | 0 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 |
| 123 | 0  | 0  | 2  | 2  | 2 | 2 | 2 | 0 | 1 | 1 | 0 | 0 | 2 | 0 | 2 | 1 | 0 | 1 | 1 |

...

## **DATA CASES INDEXED BY TIME**

|     | X  | Y  | Z  |
|-----|----|----|----|
| t-4 | -- | -- | -- |
| t-3 | 0  | 1  | 2  |
| t-2 | 3  | 4  | 5  |
| t-1 | 6  | 7  | 8  |
| t   | 9  | 10 | 11 |

original data

| A  | B  | C  | X  | Y  | Z  |
|----|----|----|----|----|----|
| -- | -- | -- | -- | -- | -- |
| -- | -- | -- | -- | -- | -- |
| 0  | 1  | 2  | 3  | 4  | 5  |
| 3  | 4  | 5  | 6  | 7  | 8  |
| 6  | 7  | 8  | 9  | 10 | 11 |

transformed data

Values are labels for variable states at particular times

XYZ = **generating variables**

Apply **mask** (here # lags = 1) to data

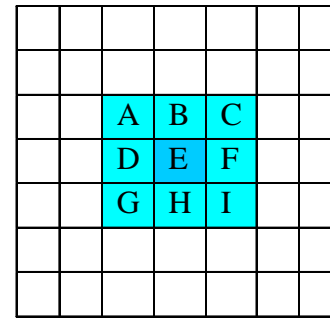
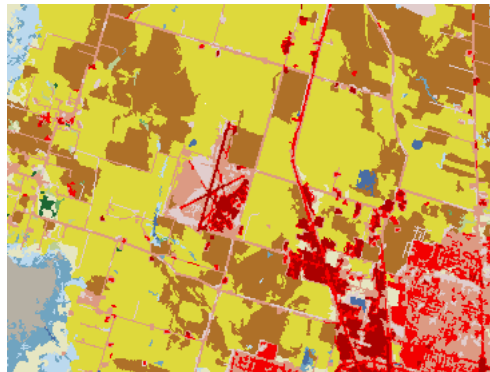
**Mask adds lagged variables**,  $ABC(t) = XYZ(t-1)$

E.g.,  $A(t) = X(t-1)$ , labeled 6

Masking: time series data → **atemporal** data

# DATA CASES INDEXED BY SPACE : 1 generating variable

A,14,1,A  
 B,14,1,B  
 C,14,1,C  
 D,14,1,D  
**E,14,2,E**  
 F,14,1,F  
 G,14,1,G  
 H,14,1,H  
 I,14,1,I



Moore neighborhood

**E = DV**

A,B,C,D,F,G,H,I = IVs

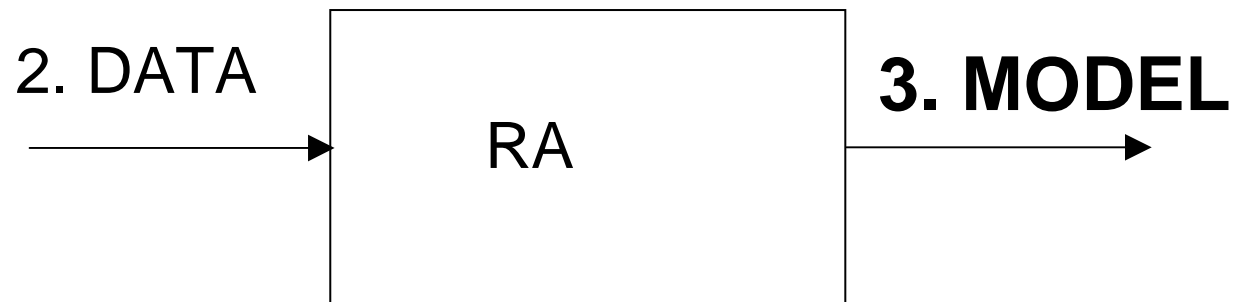
IVs & DV have 14 possible states

| #A | B  | C  | D  | E  | F  | G  | H  | I  |
|----|----|----|----|----|----|----|----|----|
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 | 71 |
| 71 | 71 | 71 | 95 | 71 | 95 | 71 | 71 | 71 |
| 95 | 71 | 95 | 95 | 71 | 95 | 71 | 71 | 71 |
| 95 | 95 | 95 | 95 | 95 | 71 | 71 | 71 | 95 |
| 71 | 95 | 95 | 90 | 95 | 95 | 71 | 95 | 95 |
| 95 | 95 | 90 | 90 | 71 | 95 | 95 | 95 | 95 |
| 95 | 90 | 90 | 90 | 95 | 90 | 95 | 95 | 90 |

...



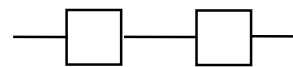
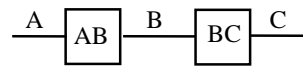
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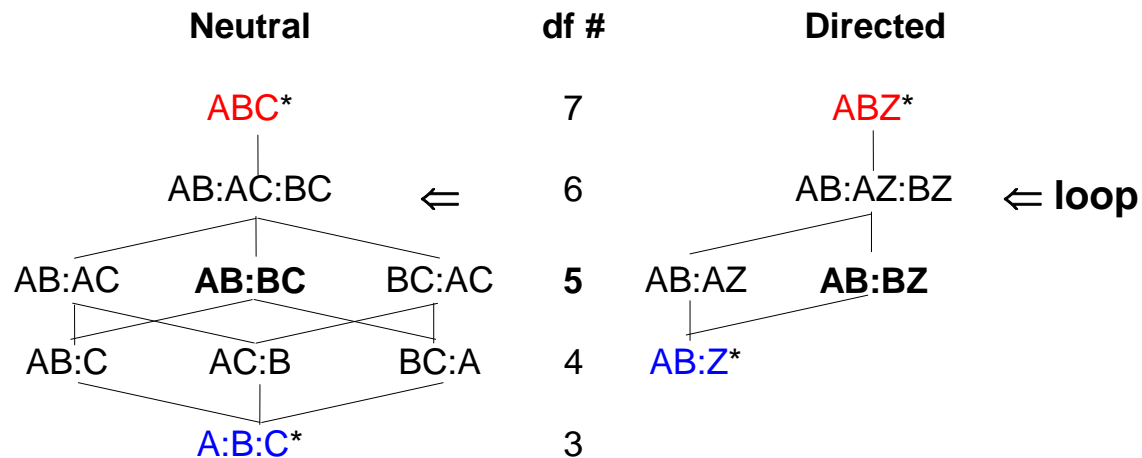
# **MODEL = STRUCTURE APPLIED TO DATA**

**A structure (graph or hypergraph) is a set of relationships (GT)**

Specific structure **AB:BC**    General structure

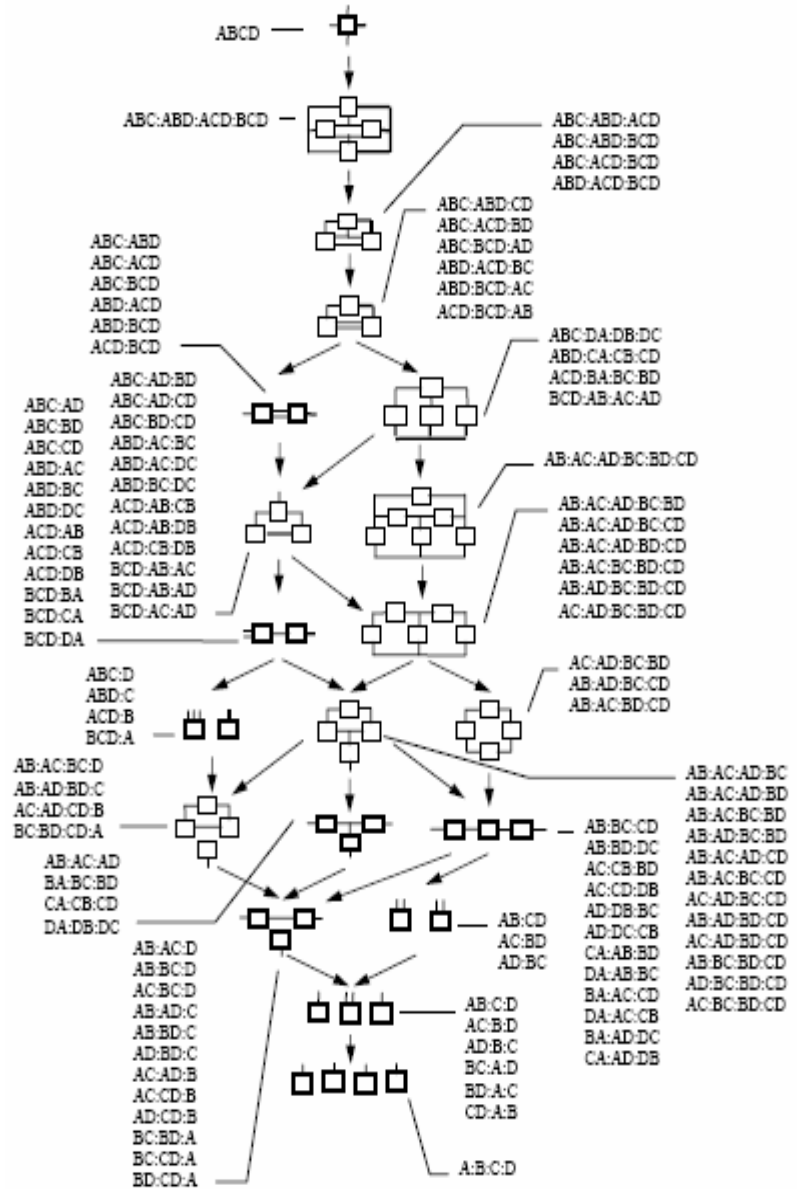
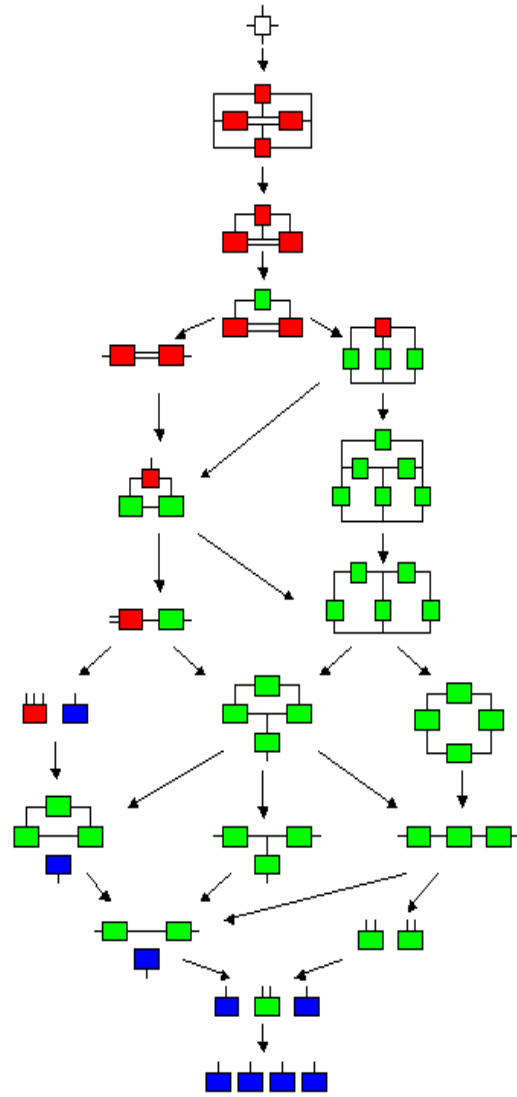


## LATTICE OF SPECIFIC STRUCTURES (3 variables)



\* **Reference model is data or independence**  
 # df (degrees of freedom) values are for binary variables

# STRUCTURES 4 variables (GT)



# ***STRUCTURES* (GT)**

## Combinatorial explosion

| # variables                                  | 3 | 4   | 5     | 6         |
|--|---|-----|-------|-----------|
| # general structures <small>neutral</small>  | 5 | 20  | 180   | 16,143    |
| # specific structures <small>neutral</small> | 9 | 114 | 6,894 | 7,785,062 |
| one DV <small>directed</small>               | 5 | 19  | 167   | 7,580     |
| one DV, no loops <small>directed</small>     | 4 | 8   | 16    | 32        |

NEED **INTELLIGENT HEURISTICS** TO **SEARCH LATTICE**

Can analyze 100s of variables, & for simple models, many more.

# ***TYPES OF STRUCTURES (GT)***

FOR **PREDICTION / CLASSIFICATION** (directed system)

- **Variable-based**

- **no loops** [coarse]      *many* variables (**fast**)  
IV:ACZ                      simple prediction, **feature selection**

- **with loops** [fine]      up to 100s of variables (slow)  
IV:ABZ:BCZ              better prediction

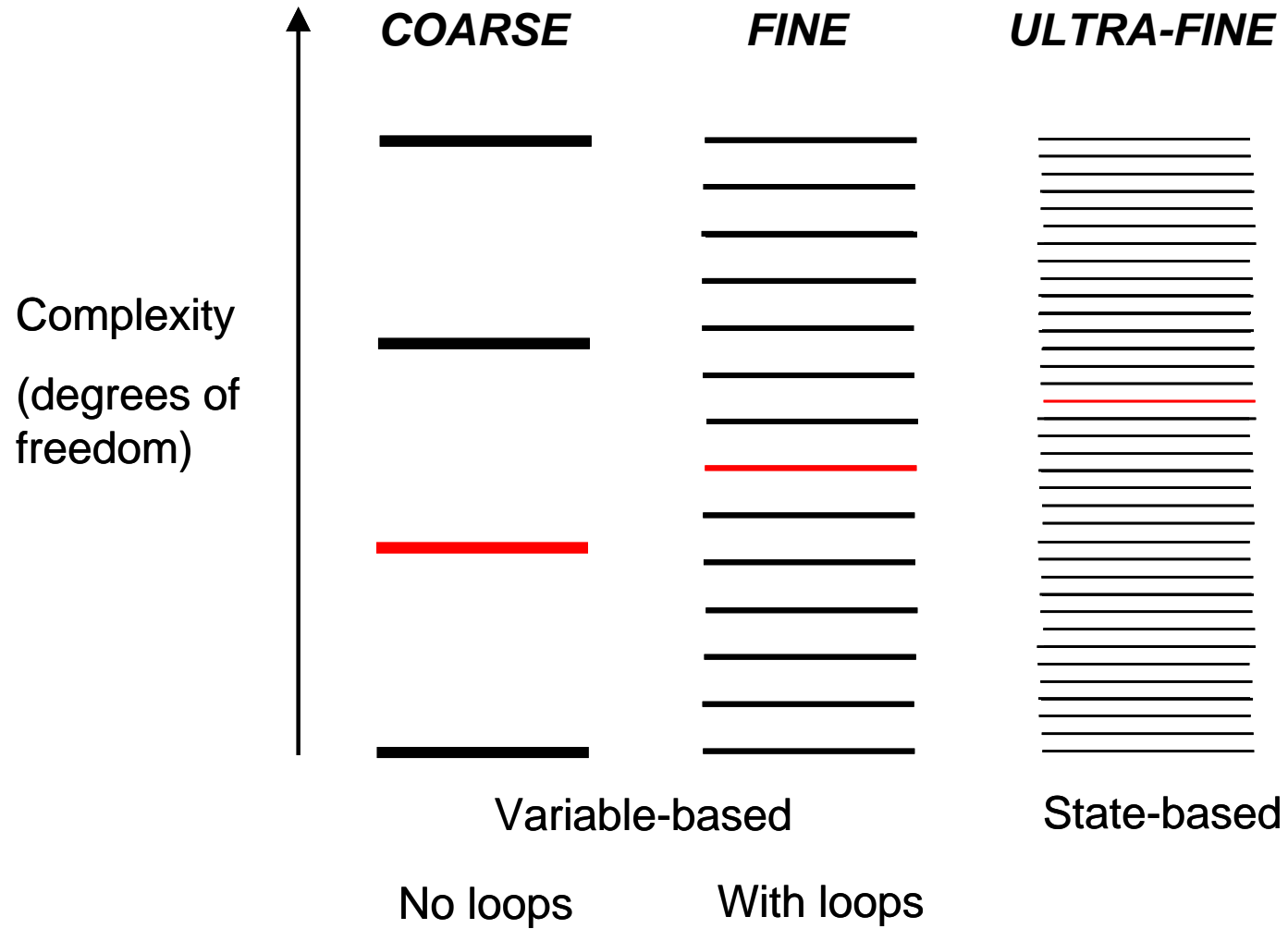
- **State-based** [ultra-fine]      < 10 variables (**very slow**)

- IV:Z:  $A_1B_1Z : B_2C_3Z_1$       best prediction; detailed models

“IV” = ABC (all IVs); Z = DV

All directed system models include an IV component

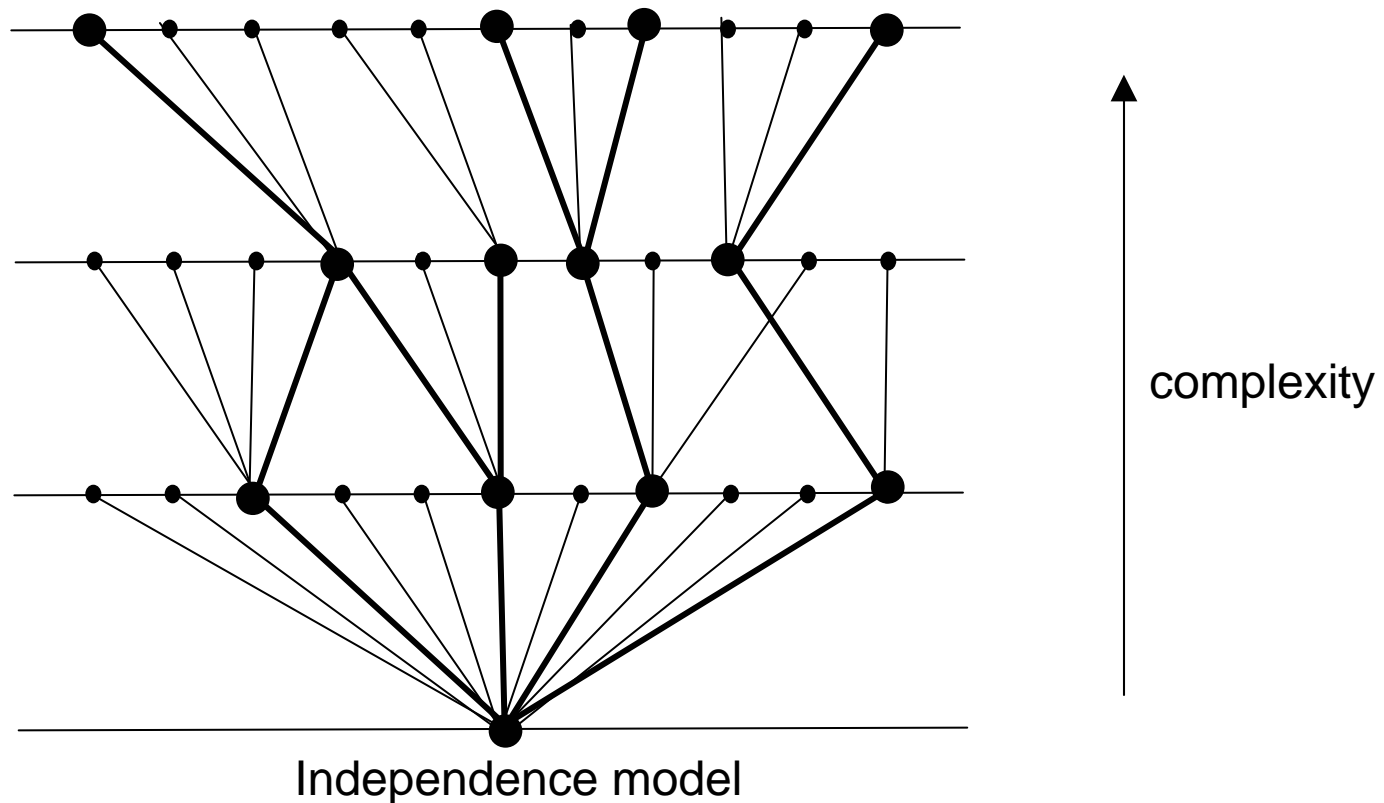
# ***TYPES OF STRUCTURES (GT)***



# ***OCCAM SEARCH of LATTICE of STRUCTURES***

beam search, levels = 3, width = 4 (node = model)

(there are many other search algorithms)



## ***MODEL = PROBABILITY DISTRIBUTION (IT)***

### Neutral system:

- Model = calculated *joint* distribution,  
e.g.,  $p_{ABC:AZ:BZ}(A_i B_j C_k Z_l)$

### Directed system:

- Model = calculated *conditional* distribution,  
e.g.,  $p_{ABC:AZ:BZ}(Z_l | A_i B_j C_k)$
- Distribution gives *rule* to *predict* Z from A,B,C  
And *increase/decrease risk* relative to margins



## ***SELECTING A MODEL (IT)***

### 1. High **information** (or low **error**) in model

#### *Directed system*

- *Info-theory measure: high  $\Delta H$ , reduction of uncertainty of DV*
- *Generic measure: high %correct, accuracy of prediction*

### 2. Low **complexity**: df, degrees of freedom

### 3. Information $\leftrightarrow$ complexity **tradeoff**

- Statistical **significance** (Chi-square p-values)
- **Integrated** measures: AIC, BIC  
(Akaike & Bayesian Information Criteria)
- BIC a **conservative** selection criterion

# UNCERTAINTY REDUCTION: SIMPLE EXAMPLE

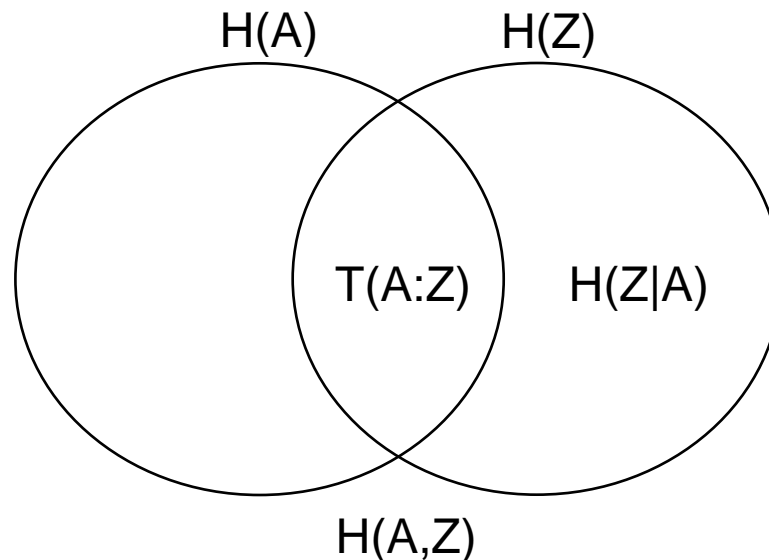
2 variables:  $IV=A$ ;  $DV = Z$ ;  $T(A:Z)$ =mutual information (*association*)

- *Uncertainty reduction* is like variance explained

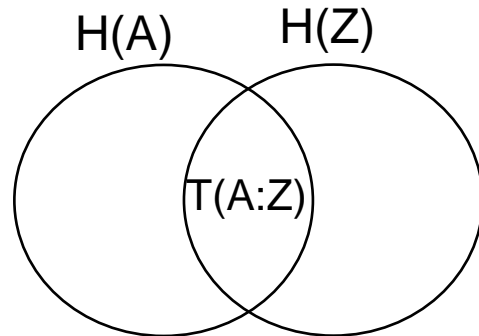
Model  $AZ$  = predict  $Z$ , i.e., reduce  $H(Z)$ , by knowing  $A$

- Uncertainty *reduced* =  $T(A:Z)$ ; uncertainty *remaining* =  $H(Z|A)$

$\Delta H = T(A:Z) / H(Z)$  *fractional uncertainty reduction* (express in %)



# UNCERTAINTY REDUCTION: SIMPLE EXAMPLE



|                | Z <sub>0</sub> | Z <sub>1</sub> |    |
|----------------|----------------|----------------|----|
| A <sub>0</sub> | .67*.5         | .33*.5         | .5 |
| A <sub>1</sub> | .33*.5         | .67*.5         | .5 |
| df=3           | .5             | .5             |    |

- $p(Z_1)/p(Z_0) = 1:1$ , not knowing A  $\rightarrow$  2:1 or 1:2, knowing A
- $\Delta H(Z) = T(A:Z) / H(Z) = 8\%$
- 8% reduction in uncertainty is *large* (unlike variance!)

# SELECTING A MODEL DEMENTIA EXAMPLE

| <u>Criterion</u> | <u>model</u> | <u>ΔH(%)</u> | <u>Δdf</u> | <u>%c</u> | <u>ΔBIC</u> |
|------------------|--------------|--------------|------------|-----------|-------------|
|------------------|--------------|--------------|------------|-----------|-------------|

*Variable-based with loops (fine)*

|     |                           |    |   |    |    |
|-----|---------------------------|----|---|----|----|
| BIC | IV: $A_p Z : E_d Z : K Z$ | 16 | 5 | 70 | 59 |
|-----|---------------------------|----|---|----|----|

|         |                                       |    |   |    |  |
|---------|---------------------------------------|----|---|----|--|
| p-value | IV: $A_p Z : E_d Z : K Z : C Z : L Z$ | 18 | 9 | 71 |  |
|---------|---------------------------------------|----|---|----|--|

|     |                                   |    |    |    |  |
|-----|-----------------------------------|----|----|----|--|
| AIC | IV: $B A_p Z : E_d Z : K Z : C Z$ | 20 | 11 | 72 |  |
|-----|-----------------------------------|----|----|----|--|

*State-based (ultra-fine)*

|     |  |    |   |    |    |
|-----|--|----|---|----|----|
| BIC | (model below; each interaction = 1 df) | 20 | 6 | 72 | 81 |
|-----|--|----|---|----|----|

IV:Z:  $A_{p_1} Z : E_{d_0} Z : K_2 Z : A_{p_0} E_{d_2} C_2 Z : A_{p_0} E_{d_1} C_2 K_1 Z : A_{p_0} E_{d_1} C_0 K_1 Z$

Models integrate multiple predicting interactions

IV =  $A_p E_d C K L \dots$  (all the independent variables);

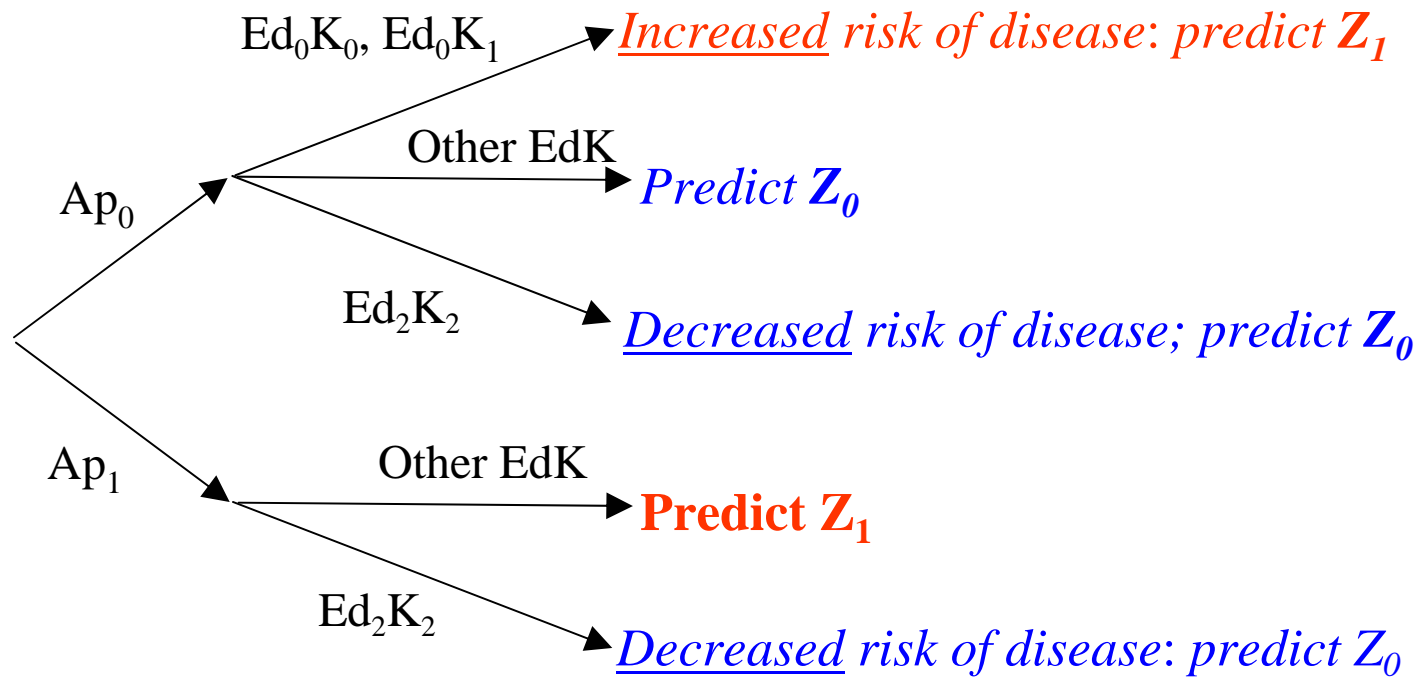
$\%c(IV:Z) = 52$

# PROBABILITY DISTRIBUTION DEMENTIA EXAMPLE

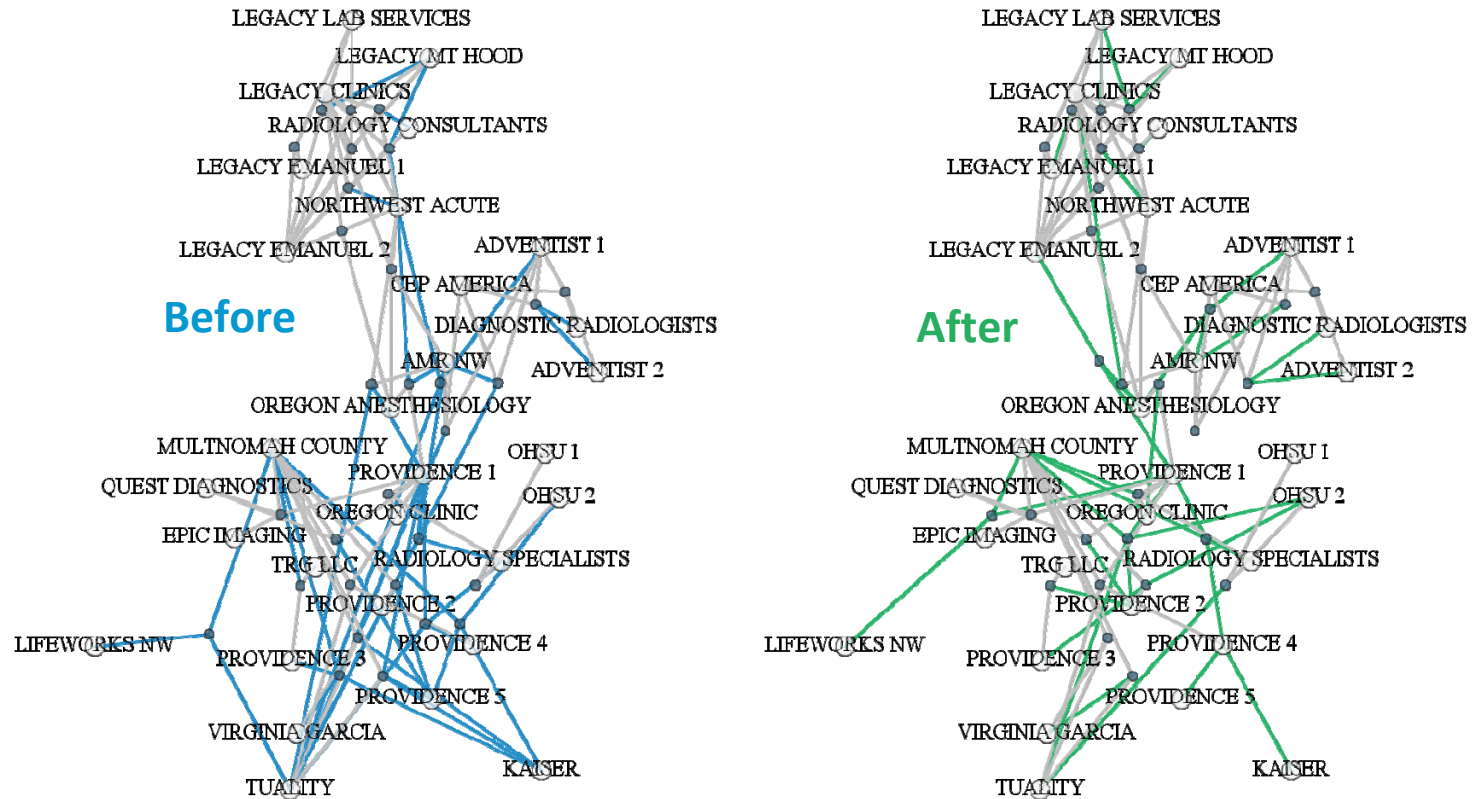
| DATA     |          |          |      | MODEL IV:ApZ:EdZ:KZ |                |                |                |          |                   |                 |
|----------|----------|----------|------|---------------------|----------------|----------------|----------------|----------|-------------------|-----------------|
| IV       |          |          |      | obs p(Z   IV)       |                | calc p(Z   IV) |                | rule     | p-value           |                 |
| Ap       | Ed       | K        | freq | Z <sub>0</sub>      | Z <sub>1</sub> | Z <sub>0</sub> | Z <sub>1</sub> |          | p <sub>rule</sub> | P <sub>Ap</sub> |
| <b>0</b> | <b>0</b> | <b>0</b> | 4    | 0.0                 | 1.000          | <b>.122</b>    | <b>.878</b>    | 1        | 0.131             | <b>0.028</b>    |
| <b>0</b> | <b>0</b> | <b>1</b> | 8    | .125                | .875           | <b>.124</b>    | <b>.876</b>    | <b>1</b> | <b>0.033</b>      | <b>0.002</b>    |
| 0        | 0        | 2        | 4    | .250                | .750           | .294           | .706           | 1        | 0.409             | 0.138           |
| 0        | 1        | 0        | 31   | .645                | .355           | .616           | .384           | 0        | 0.198             | 0.707           |
| 0        | 1        | 1        | 37   | .622                | .378           | .619           | .381           | 0        | 0.147             | 0.714           |
| <b>0</b> | <b>1</b> | <b>2</b> | 23   | .783                | .217           | <b>.827</b>    | <b>.173</b>    | <b>0</b> | <b>0.002</b>      | 0.072           |
| <b>0</b> | <b>2</b> | <b>0</b> | 66   | .636                | .364           | <b>.640</b>    | <b>.360</b>    | <b>0</b> | <b>0.023</b>      | 0.894           |
| <b>0</b> | <b>2</b> | <b>1</b> | 61   | .656                | .344           | <b>.644</b>    | <b>.357</b>    | <b>0</b> | <b>0.025</b>      | 0.942           |
| <b>0</b> | <b>2</b> | <b>2</b> | 33   | .848                | .152           | <b>.842</b>    | <b>.158</b>    | <b>0</b> | <b>0.000</b>      | <b>0.020</b>    |
| 0        | --       | --       | 267  | .648                | .352           | <b>.648</b>    | <b>.352</b>    | <b>0</b> |                   |                 |
| 1        | 0        | 0        | 1    | .000                | 1.000          | .026           | .974           | 1        | 0.343             | 0.571           |
| <b>1</b> | <b>0</b> | <b>1</b> | 7    | .143                | .857           | <b>.026</b>    | <b>.974</b>    | 1        | <b>0.012</b>      | 0.134           |
| 1        | 0        | 2        | 2    | .000                | 1.000          | .074           | .926           | 1        | 0.228             | 0.514           |
| 1        | 1        | 0        | 13   | .308                | .692           | .234           | .766           | 1        | 0.055             | 0.709           |
| <b>1</b> | <b>1</b> | <b>1</b> | 24   | .167                | .833           | <b>.237</b>    | <b>.763</b>    | 1        | <b>0.010</b>      | 0.633           |
| 1        | 1        | 2        | 11   | .545                | .455           | .478           | .522           | 1        | 0.884             | 0.146           |
| <b>1</b> | <b>2</b> | <b>0</b> | 32   | .219                | .781           | <b>.254</b>    | <b>.746</b>    | 1        | <b>0.005</b>      | 0.732           |
| <b>1</b> | <b>2</b> | <b>1</b> | 39   | .256                | .744           | <b>.256</b>    | <b>.744</b>    | 1        | <b>0.002</b>      | 0.735           |
| 1        | 2        | 2        | 17   | .529                | .471           | <b>.504</b>    | <b>.496</b>    | <b>0</b> | 0.973             | <b>0.040</b>    |
| 1        | --       | --       | 146  | .281                | .719           | <b>.281</b>    | <b>.719</b>    | <b>1</b> |                   |                 |
|          |          |          | 413  | .518                | .482           | <b>.518</b>    | <b>.482</b>    | 0        |                   |                 |

# DECISION TREE DEMENTIA EXAMPLE

Obtained from conditional probability distribution  
Increase/decrease of risk compared to prediction based only on  $A_p$



# NEUTRAL ANALYSIS EXAMPLE

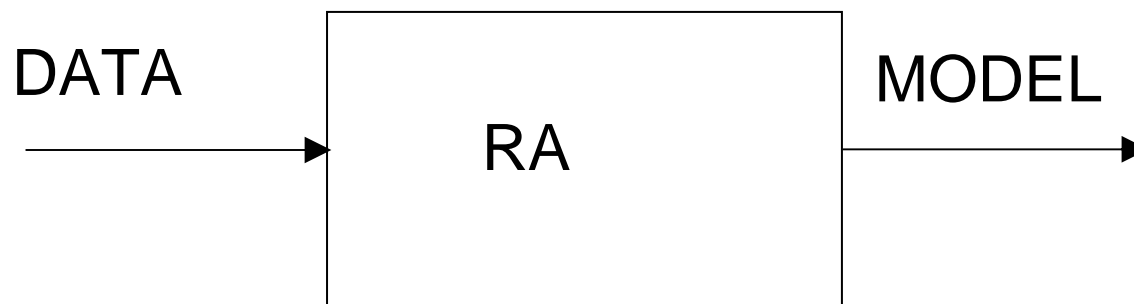


- THANK YOU.
- zwick@pdx.edu





1. Introduction: what is RA
2. Input data to RA
3. Output model from RA
4. RA methodology

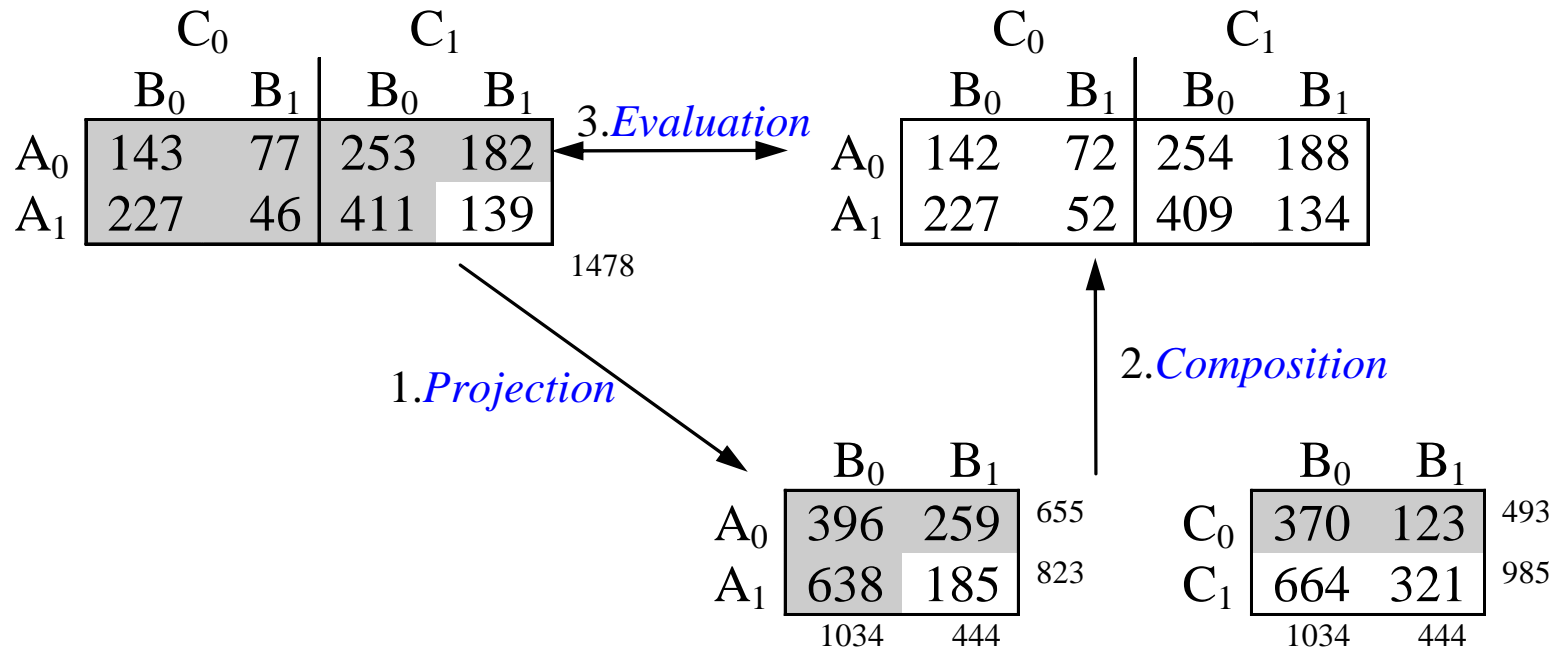


# GENERATE MODEL

frequencies shown, not probabilities

**data:** observed ABC (df=7)

**model:** calculated ABC<sub>AB:BC</sub>



## ***GENERATE MODEL*** (*Projection, Composition*)

- *Projection* = sum frequencies or probabilities
- *Composition*

***Maximize*** model **entropy** ***subject to*** model **constraints**

Model entropy:  $H(p_{\text{model}}) = - \sum p_{\text{model}} \log_2 p_{\text{model}}$

E.g., for model AB:BC, ***maximize***  $H(p_{\text{AB:BC}})$  ***subject to***

$$p_{\text{AB:BC}}(\text{AB}) = p_{\text{data}}(\text{AB})$$

$$p_{\text{AB:BC}}(\text{BC}) = p_{\text{data}}(\text{BC})$$

Composition is **critical computational step**; done

(a) Algebraically (very fast)

loopless models

(b) **Iteratively** (Iterative Proportional Fitting)

models with loops

# EVALUATE MODEL (1/2)

- *Evaluation* (1 = data dependent; 2 = data independent)

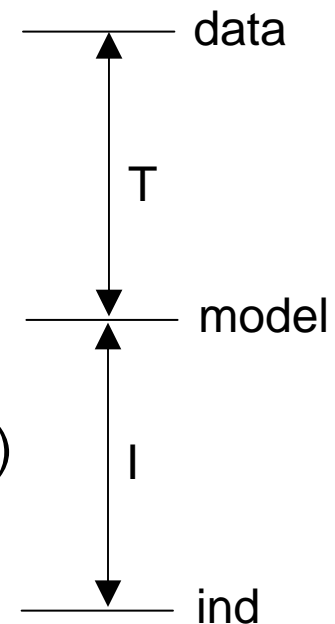
## 1. [reference=data]

$$\begin{aligned} \text{error, } T_{\text{model}} &= H_{\text{model}} - H_{\text{data}} \\ &= \sum p_{\text{data}} \log_2(p_{\text{data}}/p_{\text{model}}) \end{aligned}$$

## [reference=independence]

$$\begin{aligned} \text{information, } I_{\text{model}} &= H_{\text{ind}} - H_{\text{model}} \\ &= \sum p_{\text{data}} \log_2(p_{\text{model}}/p_{\text{ind}}) \end{aligned}$$

$$\text{uncertainty reduction} = H(\text{DV}) - H_{\text{model}}(\text{DV} | \text{IV})$$



## 2. [reference=independence]

$$\text{complexity} = \Delta df = df_{\text{model}} - df_{\text{ind}}$$

## ***EVALUATE MODEL (2/2)***

Trade off information (or error) & complexity, define **best model** criterion, via:

Use likelihood ratio Chi-square,  $LR = k N T$

- **p-values** from  $\Delta LR$ ,  $\Delta df$ , Chi-square table

Or linear combinations of information & complexity

- **$\Delta AIC = \Delta LR + 2 \Delta df$**
- **$\Delta BIC = \Delta LR + \ln(N) \Delta df$**


## ***BASIC OCCAM ACTIONS***

- **Search** = **exploratory** modeling, examine many models, find best or good ones  
(OCCAM actions: Search, SB-Search)
- **Fit** = **confirmatory** modeling, look at one model in detail (see probability distribution) & use for prediction  
(OCCAM actions: Fit, SB-Fit)

(OCCAM actions: Show Log, Manage Jobs = managerial functions)

# OCCAM Initial Screen

← → ↻ 🏠 🖨️ dmit.sysc.pdx.edu/weboccam.cgi

 **Portland State**  
UNIVERSITY

**Occam** version 3.4.0 — Tue Jun 19 14:41:08 2018

Do Search     Do SB-Search     Do Fit     Do SB-Fit    |     Do Compare

Show Log     Manage Jobs     Cached Data Mode

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## ***INFORMATION ON RA***

- Review articles on DMM page
  - “Wholes & Parts in General Systems Methodology” (accessible)
  - “An Overview of Reconstructability Analysis” (encompassing)
- Krippendorff, Klaus (1986). *Information Theory. Structural Models for Qualitative Data* (Quantitative Applications in the Social Sciences Monograph #62). New York: Sage Publications.
- *International Journal of General Systems*
- *Kybernetes*, Vol. 33, No. 5/6 2004: special RA issue