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## **Citation Details**

Bristol, T. Reconsidering the Foundations of Thermodynamics from an Engineering Perspective. Preprints 2018, 2018070139 (doi: 10.20944/preprints201807.0139.v1).

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1 Article

# Reconsidering the Foundations of Thermodynamics from an Engineering Perspective

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6 Received: date; Accepted: date; Published: date

7 Abstract: Currently, there are two approaches to the foundations of thermodynamics. One, 8 associated with the mechanistical Clausius-Boltzmann tradition, is favored by the physics 9 community. The other, associated with the post-mechanical Carnot tradition, is favored by the 10 engineering community. The bold hypothesis is that the conceptual foundation of engineering 11 thermodynamics is the more comprehensive. Therefore, contrary to the dominant consensus, 12 engineering thermodynamics (ET) represents the true foundation of thermodynamics. The 13 foundational issue is crucial to a number of unresolved current and historical issues in 14 thermodynamic theory and practice. ET formally explains the limited successes of the 'rational 15 mechanical' approaches as idealizing special cases. Thermodynamic phenomena are uniquely 16 dissymmetric and can never be completely understood in terms of symmetry-based mechanical 17 concepts. Consequently, ET understands thermodynamic phenomena in new way, in terms of the 18 post-mechanical formulation of action. The ET concept of action and the action framework trace 19 back to Maupertuis's Principle of Least Action, both clarified in the engineering worldview research 20 program of Lazare and Sadi Carnot. Despite the intervening Lagrangian 'mechanical idealization of 21 action', the original dualistic, indeterminate engineering understanding of action, somewhat 22 unexpectedly, re-emerged in Planck's quantum of action. The link between engineering 23 thermodynamics and quantum theory is not spurious and each of our current formulations helps 24 us develop our understanding of the other. Both the ET and quantum theory understandings of 25 thermodynamic phenomena, as essentially dissymmetric (viz. embracing complementary), entail 26 that there must be an irreducible, cumulative historical, qualitatively emergent, aspect of reality.

Keywords: Foundations of thermodynamics; Boltzmann vs. Carnot; engineering thermodynamics;
 quantum thermodynamics; Principle of Least Action; complementarity; Maupertuis; Lazare Carnot

29

# 30 1. Introduction

Historically, there were two paths to thermodynamics: the engineering path of Sadi Carnot and the mechanical path of Clausius and Boltzmann. Oxford's Peter Atkins, in his book, *The Second Law*, maintains: "The aims adopted and the attitudes struck by Carnot and Boltzmann epitomize thermodynamics. ... Carnot traveled toward thermodynamics from the direction of the engine, then the symbol of industrial society: his aim was to improve its efficiency. ... Boltzmann traveled to thermodynamics from the atom, the symbol of emerging scientific fundamentalism, his aim was to increase our comprehension of the world at the deepest levels then conceived [1]."

Despite many unanswered questions, the modern consensus at least in the physics community, favors Boltzmann's mechanistic formulation of thermodynamics and the corresponding historical narrative of development of thermodynamics. Sadi Carnot and the caloric theory are presented as 'mere' historical footnotes. That is how I was taught thermodynamics in my physics and chemistry education at UC Berkeley. And yet to my surprise Atkins adds: "Thermodynamics still has both aspects, and reflects complementary aims, attitudes, and applications [1]."

44 I confess that it took me a full three years of digging into the foundations to convince myself that 45 not only was Atkins correct about the history, but that, in actual practice, there are indeed, two 46 distinct modern formulations of thermodynamics. One typically favored in the physics community, 47 the other in the engineering community. As a rough initial characterization, the former uses a closed 48 system paradigm and the latter uses an open system paradigm (viz. hot source-working system-cold 49 sink). The Clausius-Boltzmann paradigm embraces the concept of entropy and the objectivity of the 50 standard Four Laws [2]. The engineering paradigm identified with Sadi Carnot is often identified 51 with the limit of efficiency and the Carnot cycle.

52 Discussing Atkins's two formulations theme with a colleague, Robert Ulanowicz, he offered: 53 "Oh, yes! When completing my Ph.D. in chemical engineering at Johns Hopkins, in my orals, in 54 response to the obligatory thermodynamics question, if I had answered in terms of the Boltzmann 55 paradigm, I would have been on the street the next day looking for a job selling real estate."

In convincing myself of Atkins's historical thesis and the continuing modern separation in current practice, I also discovered to my satisfaction that the two resulting formulations are not compatible. The crucial foundational question then presents itself: what is the relationship between mechanical thermodynamics and engineering thermodynamics? Atkins suggests that they are complementary, and I can see that in a certain sense, the open-closed difference makes this plausible. At the very least neither one is reducible to the other. The differences suggest a difference of type, a qualitative conceptual difference. They appear to be logico-mathematically incommensurable.

63 Certainly, the dominant representation of thermodynamics that comes from the physics and 64 philosophy of physics community favors the Clausius-Boltzmann formulation [3][4][5]. In history of 65 science scholarship, the engineering thermodynamics tradition is frequently represented as based on 66 misconceptions, such as the caloric theory. And although key features of the open systems model are 67 taught, such as limit of efficiency and the Carnot cycle, there is a presumption that engines are not 68 fundamental or foundational and are somehow reducible to their component particles and to closed 69 system mechanics.

70 I came to thermodynamics from physics, later expanding my perspective in philosophy of 71 science. In the Popperian tradition of bold hypotheses [6], my thesis here is that: engineering 72 thermodynamics, properly understood, is more general and more fundamental than mechanical 73 thermodynamics. According to this thesis, all the mechanical formulations of thermodynamics must 74 involve idealizations making them special cases of limited validity within the more general 75 engineering framework. The bold hypothesis entails that engineering thermodynamics is 76 foundational, formally subsuming and superseding all possible mechanical formulations. It is 77 important to be clear that I understand 'science' as 'mechanics', and all mechanical frameworks as 78 defined by classical presupposition of symmetry and conservation. An entailment of the bold 79 hypothesis is that these symmetry and conservation principles must be limited, based on 80 idealizations.

Atkins further maintains that the empirical research that discovered and defined
thermodynamic phenomena as 'real', and, per hypothesis, as not reducible to the classical mechanical
phenomena, in effect, discovered a fundamental, post-mechanical dissymmetry in the nature of
reality [1]. <sup>1</sup>

#### 85 2. Approach and Methods: Subsume and Supersede

To claim that one theory subsumes another means that all the successes of the subsumed theory can be accounted for by the more general subsuming theory [7]. However, the subsumed theory is 'not even wrong'. A simple analogy illustrates. For instance, the flat earth theory worked quite well,

<sup>&</sup>lt;sup>1</sup> Atkins (page9) [1]: "The Second Law recognizes that there is a fundamental dissymmetry in Nature: the rest of this book is focused on that dissymmetry, and so we shall say little of it here. All around us, though, are aspects of the dissymmetry: hot objects cool, but cool objects do not spontaneously become hot; a bouncing ball comes to rest, but the stationary ball does not spontaneously begin to bounce."

89 apparently for millennia. The advanced spherical earth theory is more general and accounts for all 90 the successes of the flat earth theory. The historical reasonableness of the flat earth theory is pointed 91 out in that we are very small observers on a very large sphere. The flat earth theory still works quite 92 well within certain boundary conditions. However, the more general, subsuming, advanced spherical 93 earth theory does not include the falsity content and predictions of the flat earth theory, such as falling 94 off the edge of the earth at some point. Similarly, NASA's Apollo mission to land on the Moon 95 programmed their computers using Newtonian physics even though it was presumed that 96 Newtonian physics is subsumed by the more advanced Relativistic physics. For the Apollo mission, 97 the nine-mile correction suggested by relativistic effects was well within the practical uncertainty of 98 the positions resulting from each rocket-burn.

99 In the later developments of quantum theory Bohr offered a formal criterion of proper 100 succession, what he called The Correspondence Principle: the later, more general theory must be able 101 to account for the successes of the earlier theories without including their falsity content [8].

102 To claim that one theory supersedes another is more subtle and conceptual [7]. The transition to 103 a more general, superseding theory is conceptually discontinuous, meaning that you cannot simply 104 reason your way from the initial theory to the superseding theory. You cannot derive the more 105 general superseding conceptual system from the superseded theory. The conceptual discontinuity 106 entails the logical discontinuity. In his seminal book, The Structure of Scientific Revolutions, physicist 107 and historian of physics, Thomas Kuhn, highlighted the conceptual discontinuity that characterized 108 advances in knowledge and understanding [10]. Kuhn appropriately branded major advances as 109 'revolutionary' and, as involving a paradigm shift in both concepts and experimental techniques. The 110 advanced, superseding theory adopts a qualitatively distinct, conceptually novel, framework. The 111 successes of the previous theories are subsumed, albeit understood, conceptually, in a new way. 112 Characteristic of advanced conceptual tools is that they allow one to generate novel questions, 113 qualitatively new types of questions that were inconceivable in the previous, limited conceptual 114 framework. Again, by analogy, in the spherical earth theory one can imagine new types of exploration 115 and investigation such as circumnavigation and launching artificial satellites. The range of 116 meaningful inquiry expands – emerges qualitatively.<sup>2</sup>

117 Per hypothesis, engineering thermodynamics subsumes and supersedes all possible mechanical 118 representations of thermodynamics. Kuhn's paradigm shifts are represented as from one scientific 119 theory to a more general scientific theory, always remaining within an overall scientific (mechanical) 120 framework, defined by some sort of symmetry and conservation principles. The paradigm shift to 121 the engineering thermodynamic framework is a step more general. As the flat earth is understood as 122 a limited idealization from within the spherical earth theory, the symmetry and conservation 123 principles definitive of all possible mechanical worldviews are to be understood as limited 124 idealizations from within the more general understanding of the engineering thermodynamic 125 framework.

An important consequence of the conceptual advances involved in paradigm shifts is that just as one cannot logically derive, for instance, Einstein's relativistic physics from Newtonian physics, it is also the case that one cannot understand the conceptual apparatus of Einstein's relativistic physics from within the conceptual framework of Newtonian physics. Similarly, the more sophisticated postmechanical conceptual framework of quantum theory cannot be either derived from or understood from within the conceptual frameworks of either Newtonian particle mechanics or Maxwellian electromagnetic wave mechanics.

133 The point of all this is that according to my bold hypothesis the conceptual apparatus of the 134 engineering framework cannot be derived from or understood in terms of any classical mechanical 135 conceptual framework. Stated another way, the concepts of the more advanced engineering

<sup>&</sup>lt;sup>2</sup> This emergent aspect of actual advances remains largely unexplained. In the idealized scientific (mechanical) model, advances should be systematic, logico-mathematically consistent and convergence toward complete knowledge, wherein the range of meaningful questions should narrow as the uncertainty declines.

136 thermodynamics framework, by their very nature, are not reducible to, or properly understood in 137 terms of, classical scientific, mechanical concepts.

An illustrative consequence, in the recent philosophy of engineering literature, is offered by Stanford aeronautical engineer, Walter Vincenti, in his seminal book, *What Engineers Know and How they Know It* [11]. He argues that engineering knowledge is conceptually distinct from scientific knowledge. Concerning the common representation of engineering as 'applied science', Vincenti responds: "Engineers know from experience that this is untrue." Vincenti challenges us to develop a more general epistemology that is not, by its very nature, reducible to any possible classically scientific, mechanical epistemology.

145 Duke engineer, Henry Petroski, in his book, *The Essential Engineer*, argues that what we have 146 previously imagined to be scientific inquiry and scientific knowledge, is only properly understood, 147 from within a more general superseding engineering framework as engineering inquiry and 148 engineering knowledge [12].

Per hypothesis, engineering knowledge and engineering activity, by their very nature, can only be properly understood within the more general, foundational, engineering thermodynamic framework. In the engineering worldview the universe evolves thermodynamically, a way of understanding that subsumes and supersedes all possible classical scientific, mechanical worldviews.

153 Engineering is thermodynamics. Thermodynamics is engineering.

# 154 **3. Strategy and Transition**

155 In order to develop and defend the bold hypothesis there are two closely related tasks. First, we 156 need to articulate engineering thermodynamics from within an engineering conceptual framework. 157 For instance, rejecting attempts to represent Carnot's insights in the terms of a rational mechanics. 158 Second, the proper understanding of engineering thermodynamics requires a reconsideration of the 159 actual history of the emergence of thermodynamics. Despite acceptance that thermodynamics 160 originally arose from engineering and was not the result of any scientific research program, many 161 historians have offered 'rational reconstructions' from a mechanical perspective. These begin with 162 the presupposition that the 'real' development must have happened a certain way, consistent with a 163 'rational mechanics', because 'we know' that, ultimately, in the long run, the correct representation 164 of knowledge and advances in knowledge must be rational mechanical, as in the postulated scientific 165 Theory of Everything [13].

166 3.1. Donald Cardwell and the History of Thermodynamics

167 Historian of science and technology Donald Cardwell, being based at University of Manchester, 168 naturally took a special interest in the history of the industrial revolution and the crucial influence of 169 heat engines. More than other historians Cardwell realized that many of the 20th century histories of 170 science and technology misrepresented the history of thermodynamics. Cardwell came to believe that 171 the late 19th and early 20th century dominance of the mechanical worldview had led to misguided 172 'rational reconstructions' of the history of science and technology [14].

173 If one accepted the dominant cultural belief that the universe is governed by one universal 174 mechanical order, 'it stood to reason' that advances in understanding reality must have occurred 175 'rationally', mirroring the supposed 'one' logico-mathematically, rationally consistent mechanical 176 order governing reality. Whether advances could even potentially proceed in this way was the core 177 controversy animating the latter half of 20th century history and philosophy of science [9]. Thomas 178 Kuhn had served to crystalize a large body of diverse research suggesting the need for an alternative 179 approach to the history of science and technology. What has been lacking philosophically, over the 180 ensuing period, is a more general framework that can properly subsume and supersede the limited 181 mechanical theories and their apparently limited ways of representing both successful practice and

182 conceptual advances. Per hypothesis, we have been lacking a clear understanding of the more general
 183 engineering conceptual framework [15]. <sup>3</sup>

184 Cardwell came to believe that the dominant histories of thermodynamics, largely built on the 185 work of Clausius, Kelvin, Joule and Boltzmann had misrepresented both the actual history of 186 thermodynamics and, as a consequence, the correct understanding of engineering thermodynamics 187 as foundational. Cardwell reflects [16]:

188 "Almost traditionally, it seems, accounts of the development of the concepts of work and energy 189 have tended to describe them within the classical framework of Newtonian mechanics. They are seen 190 as the end products of the celebrated *vis-viva* dispute in the eighteenth century: the outcome of a 191 debate within the confines of the science of rational mechanics. I would like to suggest that this may 192 be to take too narrow a view of the case."

193 I will argue that reconsideration of 'the celebrated vis-viva' debate reveals the origin of what 194 Atkins identified as the 'two paths' to thermodynamics. Cardwell's careful scholarship on the history 195 of thermodynamics also led him to recognize the competition between the two historical approaches 196 to the formulation of thermodynamics [17]. The 'rational mechanics' approach, favored by theorists, 197 mathematicians and logicians, represented thermodynamics as one logically consistent axiomatic 198 system. This approach tacitly implied that advances in understanding must occur by means of some 199 logically consistent rational process. The alternative, 'empirical mechanics' approach, favored by 200 engineers, rejects the rationalist formulation wherein advances in understanding are 'rationally' 201 foreseeable. In the 'empirical mechanics' approach advances require genuinely exploratory hands-on 202 empirical investigation resulting in novel discovery.<sup>4</sup>

203 Cardwell re-introduced historical consideration of the practical, 'empirical mechanical' 204 tradition. He soon recognized this as the engineering tradition. Appropriately Cardwell discovered 205 the research and innovations of engineers such as Roger Smeaton [17] concerning the power and 206 efficiency of waterwheel designs. And he recognized these as historical antecedents of Sadi Carnot's 207 later investigations of the power and efficiency of steam engine designs. Questions such as how to 208 design an engine for either maximum power or maximum efficiency are at the foundation of 209 engineering thermodynamics. Such fundamental engineering questions have ancient roots and yet 210 don't even arise within the 'just-so stories' of the rational mechanical narrative of the history of

<sup>4</sup> What has been particularly misleading is that after each conceptually discontinuous advance the new way of understanding is re-axiomatized using the new concepts and definitions. Superficially, it can 'appear' that the sequence of advances have all occurred within one logico-mathematical framework, now, 'more clearly understood' in the concepts and definitions of this new latest axiomatization. Such an attitude is at least reasonable if one presupposes that the eventual final theory of everything will have a single, unified axiomatizable structure. Only with careful historical scholarship can it be established that the axiomatized advances are a sequence of logically discontinuous axiomatizations, each involving a paradigm shift to a more general conceptual framework that supersedes the prior axiomatized understandings. Only with quantum theory and the abandonment of the presupposition that the final theory will be mechanical, does a new approach begin to be taken seriously. Only with the embrace of post-mechanical quantum framework does the 'rational mechanist' dream of a conceptually uniform, logico-mathematically consistent final theory seem to be impossible.

<sup>&</sup>lt;sup>3</sup> We have been lacking a philosophy of engineering and engineering worldview that could subsume and supersede the previously dominant philosophy of science and the scientific (viz. mechanical) worldview. We need to reexamine both current scientific epistemology and ontology from a new post-mechanical point of view.

211 thermodynamics. <sup>5</sup> Cardwell's evolving hypothesis was that the real history of thermodynamics 212 requires a post-mechanical framework.

213 The emergence of the post-mechanical framework of quantum theory was completely 214 unexpected from the perspective of the rational mechanics research program. Quantum theory 215 challenged the rationalist historical narrative by undermining the claim that the classical, objectivist, 216 mechanical framework could be foundational. Quantum theory is, by its very nature, more general 217 than all possible mechanics, superseding, in particular, both Newtonian mechanics and the 218 complementary Maxwellian mechanics [18]. Following Cardwell's insight as to the need to reconsider 219 the history and foundations of thermodynamics from a post-mechanical perspective, it should not 220 perhaps have been entirely surprising to discover a fundamental link between the real origin and

- 221
- nature of engineering thermodynamics and quantum theory.
- 222 Cardwell was eventually led to the work of Lazare Carnot.

#### 223 3.2. Lazare Carnot's Engineering Worldview Project

224 Anyone who has studied the history thermodynamics is at least aware of Sadi Carnot, whose 225 Reflexions on the Motive Power of Fire [19], first published in 1824 but unnoticed until 1834, is often 226 cited as the founding treatise of thermodynamics. There is far less awareness in the thermodynamics 227 community of his father, Lazare Carnot, who was writing on 'engineering mechanics' (viz. per 228 hypothesis, thermodynamics) a decade or more before Sadi was born. As has recently been argued, 229 and I agree, Sadi's founding treatise on heat engines is best understood as a direct application of 230 Lazare's earlier engineering approach to understanding 'the fundamental laws of the communication 231 of movement' [20].

232 The obscurity of Lazare's important, foundational work calls for an additional comment. Very, 233 very briefly, Lazare was one of the three principals managing the French Revolution and had become 234 the General in charge of the army of the revolution. Lazare was a key influence in the decision to 235 behead Louis XVI. Subsequently, when the Bourbon monarchy was partially restored in France, 236 Lazare books were banned. It was well into the 20th century before Princeton University historian 237 Gillispie rediscovered and appreciated the significance of Lazare Carnot's fundamental contributions 238 [21]. Since then awareness of his work has been growing [20].<sup>6</sup>

239 Lazare's scholarship was not isolated. He was one of a number of engineers, physicists and 240 mathematicians clustered in time around the new École Polytechnique in Paris during an 241 extraordinarily productive intellectual period. Among the other faculty and students were Ampere, 242 Cauchy, Lagrange, Navier, Poinsot, Fourier, Fresnel, Clapeyron and Coriolis.

243 Lazare Carnot clearly differentiates his empirical engineering mechanics project from the 244 dominant alternative rational mechanics projects. Lazare points out, definitively, that "Every person 245 knows, that in machines in movement, we always lose in time or in velocity what we gain in power 246 [22]." He continues, that after carefully examining all the rational mechanics he finds that they are 247 unable to explain this. Moreover, such options, such choices, can't even arise, can't even be made 248 sense of in any fully deterministic rational mechanics.

249 Lazare is pointing out the obvious presupposition of all engineers, that there are alternative 250 courses of action – with tradeoffs. There are options as to how a task might be accomplished, for 251 instance, to lift something directly or, more slowly by using a pulley. Lazare's 'everyone knows' 252 might more sympathetically be expressed as 'every engineer knows', although anyone active in the 253 world tacitly knows that there are typically different approaches available to accomplish any task.

<sup>&</sup>lt;sup>5</sup> Stephen Jay Gould introduced the metaphor of 'just-so stories' into the philosophy of biology as a critique of imagined explanations that 'make sense' and 'stand to reason' but lack any real empirical basis. Gould's 'justso stories' reference is to Rudyard Kipling's 1902 Just So Stories, deliberately fanciful stories for children in which the stories pretend to explain animal characteristics such as the leopard's spots or the elephant's truck.

<sup>&</sup>lt;sup>6</sup> I am currently involved in a project translating, from French into English, Lazare Carnot's two mature works of 1803: The Fundamental Principles of Equilibrium and Motion and, The Geometry of Position.

Prominent in Lazare's thinking is the role of simple machines identified in the ancient engineeringtradition.

Another way to characterize Lazare's project is as an attempt to develop a more general, postmechanical worldview that is able to make sense of the place the engineer, common engineering knowledge and engineering practices, in the universe. The rational mechanics (viz. scientific) worldviews have no way to make sense of the creative freedom presupposed in engineering.

#### 260 *3.3. Pierre Maupertuis*

Just as Cardwell reached back in the practical engineering tradition to see the relevance of Roger Smeaton to Sadi Carnot's work, it is important to seek earlier theoretical considerations contributing to Lazare's seminal engineering project. The intellectual milieu in physics and mathematics in the 150 years prior to Lazare Carnot's (1753-1823) investigations was defined by the contributions of Galileo Galilei (1564-1642), Rene Descartes (1596-1650), Isaac Newton (1642-1727) and Gottfried Leibniz (1646-1716).

In the more immediate 50 years the work Jean d'Alembert (1717-1783), Leonard Euler (1707-1783), Daniel Bernoulli (1700-1782) and Pierre Maupertuis (1698-1759) are most relevant to our narrative. One foundational debate among physicists, engineers, philosophers and mathematicians centered on the *vis-viva* controversy.

Lazare Carnot identifies Pierre Maupertuis's proposed resolution of the *vis-viva* debate as crucial to his mature engineering mechanics project [22]. And it is an understanding of Maupertuis's proposed resolution, I will argue, that clarifies the unexpected connection between engineering thermodynamics and quantum theory.

275 The vis-viva debate is commonly represented as concerned with the proper understanding (viz. 276 conception) of the quantity conserved in motion and interactions. Before proceeding it is important 277 to clarify why what is conserved is a crucial foundational issue. Symmetry and conservation 278 principles are what define any mechanical framework. Therefore, the identification of just what 279 quantity is actually conserved provides the conceptual foundation of the mechanical framework. 280 Rene Descartes, in his Mechanics [23], had quite reasonably argued that the correct conception of the 281 quantity of motion was momentum, the product of mass times velocity (mv). For Descartes, the total 282 quantity of motion in the universe is conserved. <sup>7</sup> Newton agreed, in his Principia, that the 283 momentum of bodies at rest or in uniform motion is conserved, in a closed (viz. isolated) system.

Gottfried Leibniz initiates the *vis viva* controversy, rejecting the Cartesian (viz. and implicitly Newtonian) proposals. He argues that what is conserved is properly conceived of as the product of mass times velocity squared (mv<sup>2</sup>) [24][25]. However, following Cardwell's insight it is possible that many of the modern accounts of the *vis viva* controversy offer us only a 'rational reconstruction' of the history and supposed resolution from a mechanical perspective.

<sup>&</sup>lt;sup>7</sup> Bertrand Russell, in his *An Essay on the Foundations of Geometry*, points out that all possible geometries require a Principle of Equality (e.g. the Axiom of Free Mobility (or Congruence)). Symmetry and Conservation Principles are analogously required to define any possible rational, axiomatizable mechanics.

See also "The Meaning of Symmetry", Introduction, page 2 "First, we have the interpretation of the *equality of the parts with respect to the whole* in the sense of their *interchangeability* (equal parts can be exchanged with one another, while preserving the whole). Then, we have the introduction of specific mathematical operations, such as reflections, rotations, and translations, that are used to describe with precision how the parts are to be exchanged. As a result, we arrive at a definition of the symmetry of a geometrical figure in terms of its *invariance* when equal component parts are exchanged according to one of the specified operations." *Symmetries in Physics: Philosophical Reflections* (edited by Katherine Brading and Elena Castellani)

As physicist Patrick Hamill points out, although Isaac Newton and Gottfried Leibniz both invented the calculus, they had quite different conceptions of reality and how it evolved in time [26]." 8

292 Leibniz reasoned that every kinetic event generated a new equal and opposite potential event. 293 To illustrate he notes that the kinetic event of raising a body to a certain height against gravity results 294 in an equal and opposite potential kinetic event [27]. <sup>9</sup> Leibniz new dynamic equilibrium of kinetic 295 and potential events was proposing a new more general type of 'metaphysical' framework (viz. post-296 mechanical), a new way of understanding reality and how it changes. The postulate that the 'quantity 297 of motion' in the dynamic equilibrium is conserved later became the central feature of Lagrange's 298 analytic mechanics. It is well beyond the scope of this essay to argue for a definitive resolution of the 299 vis-viva debate, but Leibniz's conception of a living force (vis viva) appears to supersede the previous 300 conceptions of the dead force of Cartesian and Newtonian mechanics. The 'entities' of Leibniz's 301 reality are not inherently passive particles. In Leibniz's ontology, his entities embody the living force, 302 like agents, and 'change' naturally on their own, by their very nature. By contrast, Newtonian entities 303 move/change only by the action of an external agent. At least superficially, Leibniz's dynamic 304 ontology seems to have anticipated the thermodynamic phenomenon of Brownian motion.

Following Cardwell's suspicion that the history and nature of thermodynamics has been misrepresented as mechanical, it seems likely, as one might have expected, that the same misrepresentation applies to the supposed resolution of the *vis viva* controversy. Indeed, Cardwell in last chapter of his book, *From Watt to Clausius*, he is quite explicit in criticizing Peter Tait's supposed resolution that dominated the English-speaking literature for 100 years [28]. As will become clear I suspect, as did Cardwell, that the *vis viva* controversy remains unresolved in the modern milieu.

311 One of the illustrative technical problems concerning motion in the *vis-viva* debates had to do 312 with understanding of the shortest path between two points. In Cartesian mechanics the answer was 313 simple: a straight line. But with Leibniz's tacit introduction of Newtonian gravity as a consideration 314 there were now two components of any motion. First there was the simple linear motion with 315 constant velocity 'v', thought of as the horizontal component. Second was the vertical component of 316 motion governed by continuous gravitational acceleration –  $v^{2'}$ . Assuming two points are neither 317 perfectly horizontal nor perfectly vertical with respect to each other the path between the two points 318 must be the result of some sort of combination of the two components. The empirical observation 319 was that the actual path was quite definite and repeatable. In the ideal case this path came to be

<sup>9</sup> Leibniz (page 20) [27]: "Our new philosophers commonly make use of the famous rule that God always conserves the same quantity of motion in the world, In fact, this rule is extremely plausible, and, in the past, I held it as indubitable. But I have since recognized what is wrong with it. It is that Descartes and many other able mathematicians have believed that the quantity of motion, that is, the speed multiplied by the size of the moving body, coincides exactly with the moving force, or, to speak geometrically, that the forces are proportional to the product of the speeds and [sizes of] bodies." However, after considering an example of a body raised to a certain height and descending, Leibniz goes on. "Hence, there is a great difference between quantity of motion and force... Force must be calculated from the quantity of the effect it can produce, for example, by the height to which a heavy body of a certain size and kind can be raised; this is quite different from the speed that can be imparted to it. Nothing is simpler than this proof."

<sup>&</sup>lt;sup>8</sup> Hamill (page 16) [26] "It is well known that Isaac Newton and Gottfried Leibniz both invented the calculus independently. It is less well known that they had different notions concerning the time development of a system of particles. Newton's second law gives us a vector relationship between the force on a particle and its acceleration. ... Leibniz believed that the motion of the particles could be better analyzed by considering their *vis viva*.

represented as the brachistochrone curve (viz. later recognized as a portion of a cycloid). The problemwas how to explain this particular path, this particular combination.

Following his reanalysis of Fermat's earlier account of the shortest-time path of refracted light, Pierre Maupertuis argued that the brachistochrone curve, the actual, observed path, was not just any combination of the two components, but was the path optimized to take the shortest time. In fact, geometrically, by distance, it is a longer path. The continuously accelerating vertical component is what serves to differentiate the shortest time-path from the simple uniform straight line path expectation by the Cartesian and Newtonian mechanics.

Maupertuis's insight matured, leading to his general proposal, his Principle of Least Action: that all actual motion was an optimized combination – time-minimizing, least-effort – of these two idealized type of mechanical motion. Maupertuis's bold hypothesis was that all change and all structures and functions in the universe manifested this divine optimization [29].

332 These two idealized types of mechanical motion – one the perfectly horizontal 'mv' and the 333 other, the perfectly vertical ' $mv^{2'}$  – taken individually – can only provide incomplete descriptions of 334 actual motion. The horizontal is an idealized uniform mv-motion where the vertical component is 335 zero. The vertical is an idealized continuously accelerating mv<sup>2</sup>-motion where the horizontal 336 component is zero. Since they are orthogonal the one way of describing motion cannot be reduced 337 to, cannot be expressed in terms of, the other. They are contraries. In modern parlance, they are 338 conjugates. They are logico-mathematically and conceptually incommensurable, per hypothesis, 339 complementary [30].

340 In so far as mechanical frameworks are defined by their symmetry and conservation 341 presuppositions, each of these opposite types of motion defines a different type of mechanical 342 framework. Each framework with its corresponding principles of conservation and symmetry. 343 Maupertuis's great insight is that both perspectives must be valid, depending on the choice of frame 344 of reference. Maupertuis is pleased that the greatest mathematician of the era, Leonard Euler, 345 comments approvingly of his insight. Specifically, Euler points out that it applies to, and helps us to 346 understand, the orbits of the planets as optimized combinations of their linear and curvilinear 347 components. 10

Maupertuis eventually takes us one step further to denying that perfectly horizontal (mv) mechanical motion and perfectly vertical (mv<sup>2</sup>) mechanical motion are realizable. Consequently, no actual motion can be completely described or explained mechanically – that is, in terms of *one* idealized mechanics (viz. consistent with the symmetry and conservation presuppositions of one type of mechanics). Furthermore, since the actual paths are a combination of orthogonal, conjugate components, the paths cannot be characterized as any sort of simple sum of the two incommensurable types. <sup>11</sup>

Maupertuis needs a new way to portray the actual optimized path between any two points. Here he brilliantly introduces the notion of 'action'. All possible paths are possible actions and the actual paths, the actual actions, are the optimized paths of least action. What is important to recognize here is that, with the introduction of the notion of action, Maupertuis is introducing a conceptually novel framework – the action framework.

360 Maupertuis's action framework subsumes and supersedes all possible mv-mechanical 361 frameworks and all possible mv<sup>2</sup>-mechanical frameworks. By subsuming, Maupertuis's action 362 framework is able to explain the limited, incomplete successes of each opposite, idealized mechanics.

<sup>10</sup> The stable and regular planetary orbits also serve to illustrate Maupertuis's emerging post-mechanical worldview. The stabilities and regularities (viz. the mechanical-like relations) of reality are to be understood in a new way in Maupertuis action framework. These specific optimizations are like 'creative design solutions'. Optimization is unique to engineering where problem solving is value actualization. From an engineering point of view Maupertuis's optimized actions are the result of engineering work.

<sup>11</sup> More generally the paths cannot be related by any continuous, logico-mathematical function.

363 Maupertuis's action framework is post-mechanical, conceptually superseding, understanding all 364 mechanical concepts and frameworks in a new way, as partial, limited idealizations of actual 365 phenomena. The action framework understands the idealized mechanical conceptions of motion in a 366 new way – the new way being is in terms of action.

That these opposite idealized mechanical types are actually incommensurable is suggestively supported by the historical independence within Newtonian mechanics itself of the Three Laws (viz. where motion is always linear) and the Law of Gravitation (viz. accounting for the curvilinear component of actual motions). Newton's Three Law might be reasonably represented as a sort of generalization of the Cartesian mechanics since all motion in both cases is presumed to be naturally rectilinear. Newton's Theory of Gravity however stands apart in so far as it entails an accelerating curvilinear component that is not reducible to uniform rectilinear motion.<sup>12</sup>

374 *3.4. Engineering Thermodynamics and Quantum Theory* 

In the context of my overall bold hypothesis there seems to be a foundational link, generallyunexpected, between engineering thermodynamics and quantum theory.

377 In the several decades before quantum theory one might have characterized our uncomfortable 378 situation as having an embarrassing over-abundance of different types of 'objectivities', for instance, 379 the Newtonian and the Maxwellian. With quantum theory we have something more like a range of 380 potential objectivities – each practically optimized combination, valid within its defining constraints. 381 Maupertuis's thesis that there is an irreducible component of each opposite type of idealized 382 mechanics in all change is entirely analogous to Louis de Broglie's quantum theory thesis that every 383 observation involves an irreducible component of the complementary particle and wave aspects of 384 reality.<sup>13</sup>

With even superficial reflection there are other connections, at least analogies, between Lazare Carnot's engineering thermodynamics project and quantum theory. Both require an active agent, an actualizing observer or a participant engineer, as an essential, irreducible component of any selfreferentially coherent representation. This participant aspect of quantum theory has been thoroughly enigmatic in the attempts at a mechanical representation of quantum theory. Per hypothesis, in a more general, superseding engineering worldview 'the observer of quantum theory' is understood in a new way, as a naturally active, inquiring, actualizing engineer.

392 In both quantum theory and engineering thermodynamics prior to the choice of the appropriate 393 frame of reference, boundary conditions and experimental setup the future is indeterminate. The 394 present, although constraining, does not determine a unique future. The observer's choice in 395 quantum theory that collapses the wave function is usually characterized as 'analytically arbitrary'. 396 The 'indeterminate situation' in engineering thermodynamics, by analogy at least, might be 397 represented in terms of the Gibbs free-energy situation – constrained but enabling. However, it is 398 important to recognize, per hypothesis, that the Helmholtz free-energy situation is complementary. 399 The Gibbs and Helmholtz situations define the possibility of performing two alternative, opposite 400 types of work.

401 It is perhaps helpful to recall that quantum theory was, and still is, a theory of thermodynamics.402 Max Planck's investigation of black body radiation is properly understood as an engineering

<sup>&</sup>lt;sup>12</sup> Of all the possible combinations what selects what is optimum? Maupertuis suggests that the order of the universe, the structures and functions and, how they evolve, reflect design solutions and, consequently, some sort of purpose (teleos) – practical and perhaps divine.

<sup>&</sup>lt;sup>13</sup> Bohr's insight was that not only are idealized particle and wave phenomena complementarity, but the idealized structure and function of the experimental designs required to observe them must be complementary. Indeed, the sequence of actions required to generate those mechanically idealized experimental designs must be complementary.

403 thermodynamics research project. Per hypothesis, the proper history of quantum theory requires an404 engineering thermodynamics framework.

#### 405 3.4.1. A Little Confusion

Euler's endorsement certainly emboldened Maupertuis. Then something strange and truly confusing happened. Euler says in effect: 'Yes, Maupertuis's fundamental insight about the optimized structures and functions of reality is correct', but it's not very 'useful' [29]. Here is where the two historical paths identified by Atkins acquire their more modern characteristics. If I understand Euler, he is saying that Maupertuis's insight isn't very useful for empirical mechanical inquiry and practical problem solving.

What emerges is the Euler-Lagrange line of development defining a new type of mechanics – Lagrangian. What differentiates Lazare's engineering thermodynamics from the new Euler-Lagrange advance is that the latter adopts symmetry and conservation principles that keep it well within the foundational tradition of determinate mechanics. Despite the introduction of the new types of dynamic equilibrium between kinetic and potential, Lagrangian mechanics is still mechanically symmetric and, ontologically, 'energy' is conserved.

However, as Coopersmith [31] notes Lagrangian mechanics falters in its ability to account for dissipation. Per hypothesis, this 'dissipation' is the conjugate mechanical component. <sup>14</sup> In Lagrangian mechanics what is conserved, the energy, is of *one type*. In the Lagrangian system each present defines a unique determinate 'objective' future in the classical scientific sense. And yet there are no actualizing observers and, no constructive engineering agents.

The confusion, according to this analysis, generated by the Euler-Lagrange path is compounded
by their introduction of idealizing mechanical definitions of both 'action' and the Principle of Least
Action.

Historically, despite theoretical limitations, as Euler envisioned, Lagrangian mechanics has been tremendously useful. This led to further advances in the work of William Rowan Hamilton, plausibly still within the mechanics research program. However, whether 'energy' is conserved has been questioned and, the nature of the defining symmetry is arguably somewhat ambiguous. Nonetheless the Hamiltonian toolkit has proved quite useful in experimental investigations and applications of quantum theory.

432 Lazare Carnot actually provides the clearest, most accessible account of what is behind Euler's 433 not very 'useful' critique of Maupertuis's insight. In one of Lazare's earliest contributions, later 434 published as Reflexions On the Metaphysical Principles of the Infinitesimal Analysis, notes that the use of 435 infinitesimal analysis lacks formal rational justification [32]. Basically, it doesn't make sense. To see 436 his point, one need only reflect on the inherently ambiguous or, perhaps outright self-contradictory, 437 statements common in modern thermodynamics such as - 'the piston moves infinitely slowly'. 438 Lazare argues that infinitesimal analysis, nonetheless, is an essential tool in empirical mechanics 439 research. If reality involves complementary orders, then to empirically discover the 'useful' 440 relationships of one idealized mechanical order you need to minimize the complementary aspect, 441 making it practically irrelevant, 'ignorable'. In suggesting a superseding understanding of 442 infinitesimal analysis, Lazare is suggesting a superseding engineering understanding of the use and 443 value of idealizations in empirical inquiry.

In Lazare's superseding understanding 'objectivity' is 'real' but always bounded. Engineering
 'objectivity' is never the universal time-space invariant objectivity imagined in the classical scientific

<sup>&</sup>lt;sup>14</sup> Coopersmith (page 36) [31]: "It is very strange to say, but this profound yet banal human experience of time plays no part whatsoever in the dynamics of either Newton or Lagrange. Even though the dynamics examines macroscopic effects (but, crucially, microscopic dissipative effects, like friction or air resistance, are ignored) there is no sense of time flowing, no difference between making time run forward or backward in the equations. As Einstein wrote: "… the distinction between past, present, and future is only an illusion, however persistent.""

446 tradition. From within a more general engineering worldview Lazare presents a justification of 447 differential calculus as not only 'useful', but as an essential tool in empirical research. Inquiry is newly 448 understood as seeking to discover the regularities and uniformities describable by idealizing 449 continuous functions within 'objective' boundary conditions. At the same time, Lazare is offering a 450 more general, non-standard logic justification of induction – within uniform boundaries [33]. In 451 standard, formal logic, induction is not deductively valid, but within the boundaries of a stable 452 uniformity, within an engineering 'objectivity', it is valid. In the modern post-mechanical context, 453 Newtonian mechanics and Maxwellian mechanics are both 'objectively valid' in the engineering 454 sense, within boundary condition and with respect to specific types of experimental setups.

455 Lazare's representation of 'science' is similar to Henri Poincare's conventionalist model wherein 456 scientific inquiry, by its very nature, must always be idealizing [33]. In the modern debate about the 457 falsifiability of scientific theories, University of London philosopher of science Imre Lakatos argued 458 in keeping with Lazare's understanding that all meaningful scientific theories are necessarily false – 459 in the sense of being inherently incomplete (viz. bounded). No meaningful, falsifiable theory (viz. 460 knowledge) can achieve the classical objectivist ideal of being demonstrably reproducible over 461 changes in time and location, of being universally time-space invariant. Lakatos attributes a similar 462 position to George Hegel who suggested that 'to conceive is to falsify' in that it requires selecting a 463 way to conceive, to observe, to understand [34]. One way to express this is to say that reality is more 464 ample than any single conception, than any single way of observing. In Lazare's engineering 465 worldview reality is more ample than any single mechanical description.

466 Bohr emphasized that to observe and investigate the particle-like aspect of reality you need a 467 different type of experimental setup than if you wish to investigate the wave-like aspect of reality. 468 When Bohr's colleagues pressed him as to the nature of underlying quantum reality, he responded: 469 'There is no quantum reality. Get over it.' Bohr was emphasizing that quantum theory is post-470 objective as well as post-mechanical, subsuming and superseding the idealized particle and wave 471 ontologies of the corresponding mechanics. Consequently, there are no particles and there are no 472 waves in the Newtonian or Maxwellian senses. Physicist Nick Herbert offers what remains as one of 473 the best presentations of the problem of making sense of quantum reality [35].

Einstein expressed the problem of replacing the classical ideal of 'physical reality' with a more general, more advanced quantum reality (page 81) [36]:

476 "[Classically] Physics is an attempt conceptually to grasp reality as it is thought independently 477 of its being observed. In this sense one speaks of "physical reality." In pre-quantum physics there 478 was no doubt as to how this was to be understood. In Newton's theory reality was determined by a 479 material point in space and time; in Maxwell's theory, by the field in space and time. In quantum 480 mechanics it is not so easily seen."

481 Einstein's critique had pointed out that Newton's physics tacitly presupposed absolute 482 simultaneity, entailing that everything happens at the same time. However, this is only possible if 483 everything happens in the same place, thus – Newtonian reality is a 'material point in space and 484 time'. In Maxwell's physics reality is the idealized field completely distributed in space and time. 485 Newtonian reality is ideally completely local and Maxwellian reality is ideally completely non-local. 486 I have argued previously that the Newtonian space-time framework and the Maxwellian space-time 487 framework are complementary. If correct, then Einstein's preference for the Maxwellian space-time 488 framework in Relativity reflects a 'useful' bias to a mechanical framework, away from the more 489 general indeterminate action framework [7]. Per hypothesis, both quantum theory and relativity 490 share the same foundation and they are more completely understood as one theory from an 491 engineering thermodynamics point of view.

Wolfgang Pauli begins to articulate the characteristics of the new more general, post-mechanicalframework of quantum theory (page 36) [37]:

494 "The relation of indeterminacy, which is inherent in the laws of nature, just makes mutually 495 exclusive the experiments which serve to check the wave properties of an atomic object, and the other 496 experiments which serve to check its particle properties. The significance of this development is to 497 give us insight into the logical possibility of a new and wider pattern of thought. This takes into 498 account the observer, including the apparatus used by him, differently from the way it was done in499 classical physics, both in Newtonian mechanics and in Maxwell-Einstein field theories.

500 "In the new pattern of thought we do not assume any longer the *detached observer*, occurring in 501 the idealizations of this classical type of theory, but an observer who by his indeterminable effects 502 creates a new situation, theoretically described as a new state of the observed system. In this way 503 every observation is a singling out of a particular factual result, here and now, from the theoretical 504 possibilities, therefore making obvious the discontinuous aspect of physical phenomena."

505 In the early days of quantum theory Pauli worked out the mathematics of Werner Heisenberg's 506 initial insightful theory. In presenting the results to Heisenberg, Pauli comments: 'You can investigate 507 in the p-way or you can investigate in the q-way, but if you try to do both at the same time it will 508 drive you crazy [37].'

Quantum pioneer Louis de Broglie made the point that in the quantum worldview, in all idealizing particle experiments there is an irreducible wave aspect and in all idealizing wave experiments there is a quantized particle aspect [38]. In Newton's original particle mechanics there are no waves and in Maxwell's original wave mechanics there are no particles (viz. no discontinuities or localizations). Quantum theory is post-mechanical subsuming and superseding all possible mechanics in conjugate, complementary pairs.<sup>15</sup>

# 515 3.5. Quantum Theory as Engineering Thermodynamics

516 In the early 20th century, from a mechanical point of view, something completely unexpected 517 and enigmatic happened. Quantum theory gradually emerged and matured. Central to my bold 518 hypothesis is that what connects the engineering origin of thermodynamics with quantum theory is 519 the concept of action. Maupertuis's original indeterminate, dualistic notion of action, that was 520 mechanically idealized in Lagrange's analytic mechanics, reappears in Max Planck's quantum of 521 action.

Many modern portrayals of quantum theory emphasize the ontological enigma of particles and waves associated with the two-slit experiment. These depictions have unintentionally served to deemphasize that quantum theory is a theory concerned with thermodynamic phenomena. Planck's research into black body radiation was thermodynamic research both practically and theoretically. His research was funded by the new German electric light industry seeking the optimum relationship between power input and light output. Planck himself was hoping to overturn Boltzmann's introduction of statistical mechanical concepts into thermodynamics (viz. into physics) [39].

529 Schrodinger's popular wave function is clearly an 'energy' formula. Schrodinger had originally 530 imagined his approach to quantum theory was a return to 'sensible' wave mechanics [40]. In both 531 Maupertuis's and Planck's action frameworks, prior to making a choice of the appropriate boundary 532 conditions, and how to engage (viz. the choice of experimental setup), the situation facing the 533 observer/agent is indeterminate. Max Born made clear that the 'situations' characterized by 534 Schrodinger's approach were initially indeterminate, prior to the observer's choices [41]. In Lazare's 535 framework the constrained indeterminacy defines the engineer's 'problematic' situation, the 536 constrained range of opportunities to perform work to solve a problem and actualize value [42].

537 3.6. Atkins's Dissymmetry Thesis and Maupertuis's Evolution

<sup>&</sup>lt;sup>15</sup> Of course, in the intellectual milieu of Maupertuis and the Carnots, there was no electromagnetic theory. However, in fact, conjugates are ubiquitous throughout physics and per hypothesis, in all the sciences and mathematics. From ancient times the question of a geometric relation between lines and curves was of central concern (viz. squaring the circle). Newton's famous thought experiment, 'Newton's Bucket', highlighted his concern with the relation between linear and curvilinear motions. See also Euler on lines and curves. I think it is somewhat embarrassing that even in today's mechanics, rotation is accounted for in terms of 'fictional forces'.

538 Peter Atkins dissymmetry thesis is relevant to the question of the proper foundations of 539 thermodynamics [1]. Atkins argues that the historical discovery of the dissymmetric character of 540 thermodynamic phenomena meant that thermodynamics phenomena could never be reduced to 541 mechanical phenomena as defined within symmetric mechanical frameworks. Atkins suggests that 542 the discovery of thermodynamics phenomena constitutes the discovery of an essential, irreducible 543 dissymmetric aspect of the nature reality. If true I take it to be supportive of my bold hypothesis. Per 544 hypothesis, if the dissymmetric characteristic of phenomena is more fundamental than the idealized 545 symmetric characteristics, it means that we need a more general, subsuming, superseding, post-546 mechanical framework to understand the actual thermodynamic character of reality. In such a 547 broader view, the success of any possible mechanics would be understood as a limited special case 548 within the more general, foundational dissymmetric engineering thermodynamic worldview. 549 Similarly, since the more general indeterminate 'action' of quantum theory cannot be reduced to the 550 concepts of classical particle mechanics and/or wave mechanics, a more general post-mechanical 551 framework is required to understand the dissymmetric quantum worldview.

552 There is another important entailment of the dissymmetry thesis. Classically symmetric systems 553 are always conservative – zero-sum games. In a simple Newtonian system every action has an equal 554 and opposite reaction. If the action and the reaction are of *the same type*, then the net change is zero. 555 In closed, isolated mechanical systems with one type of ontology, one uniform type of 'energy', the 556 net change of the ontological quantity must be zero. Cambridge physicist John Barrow, in his The 557 Book of Nothing, develops the implication of a scientific worldview defined by symmetry and 558 conservation principles (viz. where the universe is a closed, isolated mechanical system) [43]. Barrow 559 argues that if you add up all the charge in such a universe it perfectly balances and cancels, so there 560 is no net charge. Similarly, if you add up all the motion (as in  $E = mv^2$ ) it must also balance and add 561 up to zero. The curious implication is that the sum of any symmetric, conservative mechanical 562 universe –is zero, the reality is nothing.<sup>16</sup>

563 Maupertuis had certainly noticed that since the components of all action, of all change are 564 opposites (viz. per hypothesis, complementary), they are not of the same type. As a Consequence, 565 neither the result of any action nor the sum of the actions of a system over time can be net zero. Even 566 though the opposite components form a new type of dynamic equilibrium, it is not 'net zero' 567 symmetric in the classical sense. Therefore, all systems must have an irreducible aspect of net change. 568 They must develop. Because they are different types, the optimizing action-reaction processes in 569 Maupertuis's worldview produce a net, non-zero change. Per hypothesis, since the net change is post-570 mechanical (viz. can't be understood in terms of only one type of mechanics) the change is, plausibly, 571 properly represented as having an irreducible an emergent, quality. In the action framework 572 processes are necessarily generative of a net historical product. What is the product? Per hypothesis, 573 the net product over time is a cumulatively actualizing, historically evolving non-zero-sum universe. 574 It is not coincidental that subsequent to his insights leading to the Principle of Least Action, 575 Maupertuis composed two major works on evolution [44][45]. If the engineering thermodynamic

<sup>16</sup> Atkins (page 9) [1]: "In 1851 Kelvin adopted that, after all, physics was the science of energy. Although forces could come and go, energy was here to stay. This concept appealed deeply to Kelvin's religious inclinations: God, he could now argue, endowed the world at the creation with a store of energy, and that divine gift would persist for eternity, while the ephemeral forces danced to the music of time and spun the transitory phenomena of the world.\*"

"\*A mischievous cosmologist might now turn this argument on its head. One version of the Big Bang, *the inflationary scenario*, can be interpreted as meaning that the total energy of the Universe is indeed constant, but constant at zero! The positive energy of the Universe (largely represented by the energy equivalent of the mass of the particles present, that is, by the relation  $E = mc^2$ ) might exactly balance the negative energy (the gravitational attractive potential energy), so that overall the total might be zero. Thus, Kelvin's God may have left a nugatory legacy."

576 framework turns out to the more general, post-mechanical foundation for understanding reality, it 577 seems plausible that Maupertuis's contribution to the theory of biological evolution will subsume 578 and supersede the mechanistically-based Darwinian, and neo-Darwinian approaches.

All this is completely consistent with various post-mechanical, participant representations of
quantum theory, for instance, by Princeton's John Archibald Wheeler [46], Berkeley's Henry Stapp
[47] and Harvard's Alfred North Whitehead [48].

582 The hypothesis that the evolution of the universe is a qualitative, cumulatively emergent, 583 recursively enabling engineering enterprise requiring an experimental research and development, 584 requiring a concomitant evolving engineering intelligence is certainly not new. It is the theme of 585 Plato's dialogue, Timaeus [49], where the question being explored is: How did the universe come to 586 be as it is? The answer suggested by Timaeus is that the evolution is an engineering enterprise of an 587 architekton (viz. master craftsman (engineer) and/or a demiurge (the public worker) [50]. Timaeus 588 assures us that the 'plan' is never analytically, deterministically pre-specifiable. Yet the recursively 589 enabling path of development is constrained, always seeking a more desirable future

590 3.7. Reflection on Current Thinking

591 Physicist Jim Baggott, in his excellent review of the current situation in his book, *Farewell to* 592 *Reality: How Modern Physics Has Betrayed the Search for Scientific Truth,* emphasizes that the questions 593 of quantum realism remain unresolved [51].

594 Despite expressions of serious misgivings current prominent physicists continue to move to the 595 default mechanical framework (viz. defined by symmetry and conservation principles) in their 596 representations of thermodynamics. Columbia University physicist Brian Greene, in his book, *The* 597 *Fabric of the Cosmos*, relates his experience on learning of Loschmidt's critique of Boltzmann's 598 mechanical representation of thermodynamics (page 168) [4]:

599 "When I first encountered this idea many years ago, it was a bit of a shock. Up until that point, 600 I had thought I understood the concept of entropy fairly well, but the fact of the matter was that, 601 following the approach of textbooks I'd studied, I'd only ever considered entropy's implications for 602 the future. And, as we've just seen, while entropy applied toward the future confirms our intuition 603 and experience, entropy applied toward the past just as thoroughly contradicts them. It wasn't quite 604 as bad as suddenly learning that you've been betrayed by a longtime friend, but for me, it was pretty 605 close."

String Theory was initially conceived as a more enlightened physics based firmly in taking
thermodynamics as foundational [52]. String Theory's all-important beta-function comes directly
from thermodynamics. Yet Greene, endorsing String Theory, assured me [Personal Communication]
that it is fully deterministic, keeping it within the mechanical paradigm.

610 Cal Tech physicist Sean Carroll, in his book, *From Eternity to Here* offers a number of penetrating
611 critiques of the standard mechanical Boltzmannian representation of thermodynamics. In his course
612 The Mysteries of Physics: Time, Carroll offers (page 220) [53]:

613 "What Boltzmann had bequeathed was a set of machinery that didn't have an arrow of time 614 built in. It could explain entropy going up toward the future, but it also explains entropy going up 615 toward the past, which nobody thought was true. The challenge was could you use these time-616 symmetric underlying laws of physics to derive a time asymmetric conclusion. The answer is no. 617 Loschmidt was right. It was not that he was making some mistake or that Boltzmann wasn't careful 618 enough. Loschmidt's reversibility objection is absolutely valid.

619 "If all you have to work with are underlying laws of physics that are symmetric with respect to 620 past and future, you do not derive a different behavior for the future than you do for the past. You 621 need to add something to that machinery, you need to add an extra assumption, and you need to add 622 an extra assumption that is explicitly asymmetric with respect to past and future. That extra 623 assumption is what we call the past hypothesis."

624 Columbia University philosopher of physics, David Albert, has offered still the best presentation
625 of the past hypothesis [54]. Although the introduction of an essential asymmetry (viz. dissymmetry)
626 would seem to entail the need for a post-mechanical framework, in his latest contribution Carroll

reassures us that the 'real', hidden, underlying reality has no participants, is completely symmetricand 'energy' is conserved [55].

Perimeter Institute physicist Lee Smolin in his 2006 book, *The Trouble with Physics: The Rise of String Theory, The Fall of Science, and What Comes Next* [56], expressed the growing dissatisfaction with the state of physics of many within the physics community. However, in his recent attempt to explore 'what's next', *Time Reborn: From the Crisis in Physics to the Future of the Universe,* he has been unable to find a way out of the tradition of the mechanical paradigm [57]. Smolin offered the following personal reflection to an incoming class of physics graduate students [58]:

"When my generation entered physics in the 1960s and 1970s, we were enthusiastic and quite
hopeful about our prospects of resolving the questions of quantum reality. The founders of quantum
physics and the subsequent generation had simply given up. – – It's now 2010, and it has become
rather Kafkaesque that we have made no progress whatsoever."

639 Philosopher of physics Craig Callender, at UC San Diego, originally one of best and most
640 prominent critics of the mechanical interpretations of thermodynamics has most recently taken a turn
641 to the dark side (viz. deterministic mechanics) explicitly abandoning any role for participant agency
642 [5].

643 On a more hopeful note, leading Los Alamos particle physicist, Geoffrey West having morphed
644 to become the President of the Santa Fe Institute, the leading edge think tank founded by Nobel
645 Laureate physicist Murray Gell-Mann, expresses what I take to be a more enlighten view [59]:

646 "All the laws of physics can be derived from the principle of least action which, roughly 647 speaking, states that, of all the possible configurations that a system can have or that it can follow as 648 it evolves in time, the one that is physically realized is the one that minimizes its action. Consequently, 649 the dynamics, structure, and time evolution of the universe since the Big Bang, everything from black 650 holes and the satellites transmitting your cell phone messages to the cell phones and messages 651 themselves, all electrons, photons, Higgs particles, and pretty much everything else that is physical, 652 are determined from such an optimization principle.

653 "Optimization principles lie at the very heart of all of the fundamental laws of nature, whether 654 Newton's laws, Maxwell's electromagnetic theory, quantum mechanics, Einstein's theory of 655 relativity, or the grand unified theories of the elementary particles. Their modern formulation is a 656 general mathematical framework in which a quantity called the action, which is loosely related to 657 energy, is minimized." <sup>17</sup>

#### 658 4. Discussion and Conclusions

Following the hints from Peter Atkins that there were two distinct historical paths in the development of modern thermodynamics, and that both approaches and corresponding formulations are still alive and well, I considered the relation between them. Atkins postulated that they are complementary. I offered a bold hypothesis that engineering thermodynamics (viz. properly understood) is more general than any mechanical formulation of thermodynamics.

I argued that engineering thermodynamics is post-mechanical and formally subsumes and supersedes all possible mechanical formulations of thermodynamics. The limited successes of the mechanical formulations are to be explained as based on idealizations and understood in a new way, more generally, in the context of optimizing engineering action. I concluded that engineering thermodynamics is the true foundation of thermodynamics.

Accordingly, the true history of thermodynamics is the history of engineering thermodynamics.
 I argued in support of Donald Cardwell contention that most modern historians misrepresent the
 history of thermodynamics. Because they reason from mechanical presuppositions they generate

<sup>&</sup>lt;sup>17</sup> In mechanical frameworks the ontology (viz. 'energy') is of only *one uniform homogeneous type*. There is no need to optimize – just calculate the unique determinate future from the present. Per hypothesis, optimization of qualitatively distinct conjugate (viz. complementary) components is characteristic of both post-mechanical engineering thermodynamics and quantum theory understandings of reality.

misguided 'rational reconstructions' of the history of thermodynamics. Cardwell's proposed research
 program is to reconsider both the history and proper understanding of thermodynamics from a post mechanical perspective. I reaffirmed his thesis that thermodynamics should be understood as part of
 the engineering tradition that reaches back to ancient times.

I argued that engineer Lazare Carnot, the father of Sadi Carnot, is a crucial contributor in the history of engineering thermodynamics. Lazare Carnot differentiates his engineering research program by emphasizing the inadequacy of any rational mechanical worldview to account for what 'everybody knows' – that we always lose in time or in velocity what we gain in power. Lazare sought a more general, empirical engineering framework that would provide a coherent understanding of the place of engineers and engineering in reality. His engineering framework is overtly postmechanical, intended to subsume and supersede all possible rational mechanical frameworks.

683 Per hypothesis, Lazare's engineering mechanics is, literally, engineering thermodynamics. The
684 history and foundations of thermodynamics makes sense only from within a self-referentially
685 coherent engineering understanding of reality.

686 Lazare identifies Pierre Maupertuis's resolution of the vis-viva debate and his post-mechanical 687 Principle of Least Action as a key intellectual antecedent. Although Maupertuis formulation was 688 'somewhat vague' Lazare realized that he had proposed a post-mechanical theory of change. In 689 Maupertuis's new action framework, the present is both constrained and enabled and does not 690 uniquely determine the future. The present is indeterminate and the future emerges through the 691 optimizing choices of the embedded agency (viz. quantum observers or constructive engineers). In 692 quantum theory and Lazare Carnot's engineering framework it is the choices, always involving 693 uncertainty, that actualize the future. Since the choices could have been different, within the 694 constrained range of possible actions, it must be that the narrative history might have evolved 695 differently.

696 Unexpectedly, Maupertuis's inclusive resolution of the complementary mechanical frameworks 697 involved in the vis-viva debate, followed by Lazare's clarifications, suggested a link to modern 698 quantum theory. In keeping with Cardwell's initial suspicion, I argued that the deep link could be 699 understood in terms of their common concept of 'action'. Dominated historically by the fully 700 determinate, mechanical idealization of action in Lagrangian mechanics, Maupertuis's original 701 dualistic, indeterminate conception finally re-emerges in Planck's quantum of action. Since quantum 702 theory arose from Planck's thermodynamic research and both quantum theory and engineering 703 thermodynamics require an embodied agent to actualize an otherwise indeterminate future I 704 reasoned, per hypothesis, that they share, in some fundamental, foundational sense, the same post-705 mechanical framework.

706 I argued that Atkin's thesis, that the discovery of thermodynamic phenomena constituted the 707 discovery of an irreducible, post-mechanical dissymmetric aspect to reality, is further support for the 708 bold hypothesis. The classical mechanical principles of symmetry and conservation are valid but 709 limited special cases to be understood in a new way within the more general, foundational 710 dissymmetric engineering thermodynamic worldview. I argued that the action-reaction dissymmetry 711 of complementary types of action entails that reality is not historically zero-sum in the mechanical 712 sense. The engineering thermodynamic worldview must have a naturally generative aspect resulting 713 in an irreducible cumulative, historical, qualitatively emergent aspect of reality.

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