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Application of Support Vector Machine in Predicting the Market's Monthly Trend Direction

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Application of Support Vector Machine in Predicting the Market's Monthly Trend
Direction

by

Ali Alali

A thesis submitted in partial fulfillment of the
requirements for the degree of

Master of Science
in
Electrical and Computer Engineering

Thesis Committee:
Richard Tymerski, Chair
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Xiaoyu Song

Portland State University
2013

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Abstract

In this work, we investigate different techniques to predict the monthly trend direction of the S&P 500 market index. The techniques use a machine learning classifier with technical and macroeconomic indicators as input features. The Support Vector Machine (SVM) classifier was explored in-depth in order to optimize the performance using four different kernels; Linear, Radial Basis Function (RBF), Polynomial, and Quadratic. A result found was the performance of the classifier can be optimized by reducing the number of macroeconomic features needed by 30% using Sequential Feature Selection. Further performance enhancement was achieved by optimizing the RBF kernel and SVM parameters through gridsearch. This resulted in final classification accuracy rates of 62% using technical features alone with gridsearch and 60.4% using macroeconomic features alone using Rankfeatures.

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Chapter 1 Introduction

Appearing in *The New Palgrave: A dictionary of Economics*, it was described that “The Efficient Markets Hypothesis (EMH) maintains that market prices fully reflect all available information. Developed independently by Paul A. Samuelson and Eugene F. Fama in the 1960s, this idea has been applied extensively to theoretical models and empirical studies of financial securities prices, generating considerable controversy as well as fundamental insights into the price-discovery process. The most enduring critique comes from psychologists and behavioral economists who argue that the EMH is based on counterfactual assumptions regarding human behavior, that is, rationality. Recent advances in evolutionary psychology and the cognitive neurosciences may be able to reconcile the EMH with behavioral anomalies [1].” Another financial theory is called the Random Walk Hypothesis (RWH) which supports the EMH. The RWH proposes the market prices change randomly which results in it being unpredictable.

Recently, studies show that the ability to predict market movement based on macroeconomic and technical analysis is possible. Macroeconomic analysis measures the health of a certain company and decides the value for a given business in order to predict if in the future the price will change in a certain direction. Technical analysis on the other hand uses the markets’ historical prices and volume in order to create an interpretation of the market’s state. With use of technical analysis, an analyst can convert the prices into various

indicators in order to understand the market state better and possibly make better prediction decisions.

The purpose of this work was to explore the techniques used to predict the market's monthly trend direction using macroeconomic and technical analysis. Using this data, an in-depth investigation using machine learning techniques was performed in order to create a model for predicting the market's movement. The result of this thesis shows that macroeconomic and technical information can be used as input to a machine learning classifier to create a prediction model that predicts if the market's movement for the following month is 'up' or 'down'.

1.1 Problem Statement

Predicting the monthly direction of the market is a problem faced by many investors. The work presented in this thesis develops a prediction model that can be used to help trading securities safer and cause less risk involved when making an investing decision.

1.2 Objective

The objective of this work was to develop a market prediction model that can successfully predict the monthly returns on a market to gain profit and reduce the risk involved. This was achieved by constructing a market prediction simulator with exploration of many different techniques to optimize the model's

performance. This model was evaluated by noting the monthly in-sample and out-of-sample classification accuracy.

1.3 Thesis Format

The following includes a literature of background information and related techniques of market data classification (Chapter 2); a description of goals, hypothesis and evaluation methods (Chapter 3); an explanation of design (Chapter 4); and a thorough description of all experimental prediction strategies with results (Chapter 5).

Chapter 2 Background Information and Literature Overview

The potential use of different data types and systems to predict the market's trend direction has increased in the recent years with many different techniques available. This thesis provides an explanation and overview of macroeconomic and technical data used with machine learning techniques to predict the direction of the market's monthly trend.

2.1 Macroeconomic Data

Macroeconomic data are measurements and indicators used to describe the current or previous economy's state of a country [2]. The macroeconomic data measures the overall health of an economy. Ability to obtain the macroeconomic data is not as simple as obtaining technical data, the other source of data used to analyze the state of the market and economy.

Macroeconomic Indicators [3]:

2.1.1 Dividend Price Ratio

The dividend per share paid to the share on a stock exchange paid previously, used as a measure of the potential investment of a certain stock.

2.1.2 Dividend Yield

It is a ratio of the dividends to the price per index that explains how much the pay out in dividends relative to the index price.

2.1.3 Earnings to Price Ratio

Earnings are the amount of profit that a company produces in a specific period which shows the company's profitability. An Earnings to Price is the valuation of an index's earnings to its price.

2.1.4 Stock Variance

Stock Variance is a measure of volatility from an average which is used to measure the risk when purchasing a certain index.

2.1.5 Book-to-Value

Book-to-Value is a ratio of a company's historical cost to the company's market value which can be found through its market capitalization. It helps to identify if the index is overvalued or undervalued. A ratio above 1 indicates the index is undervalued while less than 1 is overvalued.

2.1.6 Net Equity Expansion

Net Equity Expansion is "the ratio of 12-month moving sums of net issues by NYSE listed stocks divided by the total end-of-year market capitalization of NYSE stocks."

2.1.7 Treasury-bill

Treasury bill is a short-dated government security that yields no interest but is offered at discounted prices on its redemption price.

2.1.8 Long Term Yield

It is the percentage of return of investment on the debt responsibilities of the U.S. government.

2.1.9 Long Term Return

2.1.10 Term Spread

2.1.11 Default Yield Spread

Default yield spread is the difference between the quoted rates of return on two different investments. In our case, it is used between AAA and BAA-rated bonds.

2.1.12 Default Return Spread

2.1.13 Inflation

Inflation is the rate at which the general level of prices for goods and services increases and a fall in the purchasing power.

2.2 Technical Data

Technical analysis is the study of financial markets behavior. Technical analysis consists of evaluating historical prices in order to create technical indicators which indicate the current or past state of a certain security in market [4]. In this

work, we use some of the many common technical indicators as input features to the classifier.

Technical Indicators used in this work:

2.2.1 Relative Strength Index

An indicator attempts to identify if it is an overbought or oversold market by comparing the magnitude of recent gains to losses [6]. It is calculated as the following:

$$RSI = 100 - \left(\frac{100}{RS} \right)$$

$$RS = \frac{\textit{Average Gain}}{\textit{Average Loss}}$$

2.2.2 Bollinger Bands

Bollinger Bands are volatility bands based on standard deviation which are placed above and below a moving average. They are used to determine the strength of the trend [7]. They're calculated by the following formulas:

1. Middle Band = t-day simple moving average (SMA).
2. Upper Band = t-day SMA + (t-day standard deviation of price x 2)
3. Lower Band = t-day SMA – (t-day standard deviation of price x 2)

2.2.3 Stochastic

It is an indicator to tell if the market is oversold or overbought by comparing the price of a certain security over a given period of time. This is done by:

$$\%K = 100 \left[\frac{C(t) - L(14)}{H(14) - L(14)} \right]$$

$$\%D = 3 - \text{period moving average of \%K}$$

C = the most recent closing price.

L(14) = the low of the 14 previous trading sessions.

H(14) = the highest price traded during the same 14-day period.

2.2.4 Simple Moving Average

This indicator is formed by computing the average index price over a given period. In other words, it is defined as the N day's sum of closing price divided by N [9].

2.2.5 Momentum

It is an indicator that measures the change of a security's price over a given time period. It is defined by:

$$Momentum = \frac{Price(N)}{Price(N - t)} * 100$$

2.3 Classifier

Classifiers are machine learning algorithms that can be used to classify a problem given a set of data. This work uses and investigates the Support Vector Machine (SVM) classifier closely to classify up or down periods given two different types of data sets as inputs; Macroeconomic and technical data.

2.3.1 Support Vector Machine

A Support Vector Machine is a supervised learning algorithm that can use given data to solve certain problems by attempting to convert them into linearly separable problems [11]. The SVM is given input data called training data sets that are linked to binary outputs in order to classify new observation to one of the two classes by creating a separating hyperplane [12]. Through the created hyperplane, the algorithm then labels new examples. In this work, we perform SVM training and classification using Matlab with functions 'svmtrain' and 'svmclassify'. Four different kernels are used in this work; Linear, Radial Basis Function (RBF), Polynomial, and Quadratic. These functions are provided in the Statistics Toolbox as of the Matlab version 2013a. The mathematical formulation for each kernel is shown here [14]:

- Linear: $K(x, y) = w(x \cdot y) + b$. The vector w is known as the weight vector and b is called the bias.
- Radial basis function – RBF: For some positive number σ :

- $K(x, y) = \exp\left[-\frac{\|x_i - x_j\|^2}{2\sigma^2}\right]$.
- x_i and x_j will have either one becoming the support vector and the other will be the testing data point.
- Polynomial: For some positive integer d :
 - $K(x, y) = (1 + \langle x, y \rangle)^d$. Where d is the polynomial's degree
- Quadratic: $K(x, y) = (\langle x, y \rangle)^2$.

2.4 A Literature Overview

This work performs a study on techniques used to predict the market's trend direction using macroeconomic and technical data and feeding this data to a machine learning classifier such as the SVM in our case.

2.4.1 SVM Prediction System

In the paper "Predicting S&P 500 Returns Using Support Vector Machines: Theory and Empirics," the author mentions the use of macroeconomic data as input to the SVM classifier to predict the S&P 500 monthly trend direction [24]. We created a set of data called technical features in the aim of predicting the S&P 500 monthly trend direction. Using Relative Strength Index, Bollinger Bands, Stochastic, Simple Moving Average, and Momentum, a total of 17 different technical features were constructed. 15 other inputs were constructed using macroeconomic features. The data provided is broken into two periods for training (in-sample period) and test (out-of-sample period). A comparison

between the efficacy of using macroeconomic and technical features was performed. The next step was to optimize the SVM for both sets of data and compare the results.

2.4.2 Normalizing

Because data can be calculated differently and result in different representation to the data, certain data will have high numbers compared to the rest while others may be small. In data mining or machine learning, it is best practice to have the data pre-processed or normalized before the models are built and make use of the data. In this work, we perform normalization by use of the 'zscore', 'normc', and 'normalize' functions with Matlab. Unless turned off, SVM will normalize the data automatically using the zscore method. The way to control this is by setting 'autoscale' from its default value of 'true' to 'false', thus turning off the normalization done internally by the SVM function.

```
svmStruct = svmtrain(Training, Group, 'autoscale', true);
```

Zscore is a very useful statistical tool because it allows us to compare two different values from different normal distributions. Zscore is a function provided by Matlab and computed as follows:

$$Z(n) = \frac{Y(n) - M}{S}$$

Where M is the mean, S is the standard deviation and Yn is the value we are normalizing in the vector. A simple example is shown next where we have two

vectors to normalize, X and Y. The results show the zscore normalizes each column vector separately and independently.

X	Y	Zscore X	Zscore Y
1	2	-1.1619	-1.1619
2	4	-0.3873	-0.3873
3	6	0.3873	0.3873
4	8	1.1619	1.1619

Table 2.1 Example for normalizing simple data with zscore

The function 'normc' normalizes the data to the length of 1 [15]. This function is also provided by Matlab. The normalized vector is computed by:

$$N(n) = \frac{X(n)}{\|X\|}$$

Where $\|X\|$ is the norm of the vector and computed as the following:

$$\|X\| = \sqrt{X_1^2 + X_2^2 + \dots + X_n^2}$$

The following table is a simple example for using normc. The same values used for zscore are used here to show the difference. We see normc scales the data to the length of 1. Using normc, the column data is normalized independently.

X	Y	Normc X	Normc Y
1	2	0.18257	0.18257
2	4	0.36515	0.36515

3	6	0.54772	0.54772
4	8	0.7303	0.7303

Table 2.2 Example for normalizing simple data with normc

The function 'normalize' normalizes the data in the vector to become between 0 and 1 and scales the rest of the values appropriately. This function appears not to be provided by Matlab. However, its Matlab implementation is given in an appendix. The normalized vector is computed as the following:

$$N(n) = \frac{X(n) - Xmin}{Xmax - Xmin}$$

The same example for normc and zscore is done again to compare the results and show how 'normalize' works.

X	Y	Normalize X	Normalize Y
1	2	0	0
2	4	0.33333	0.33333
3	6	0.66667	0.66667
4	8	1	1

Table 2.3 Example for normalizing simple data with normalize

2.4.3 Gridsearch

The classifier's hyperplane can be adjusted based on the model presented by adjusting the parameters that affect the learning algorithm. This is called hyperparameter optimization or model selection and it will ensure that optimizing the model will be done during the in-sample period to not result in overfitting and make sure the out-of-sample classification procedure is not

affected [16]. There are two parameters for the RBF kernel SVM: C and sigma. A common way of performing this hyperparameter optimization is through gridsearch. The method consists of an in-depth searching through a chosen interval of the parameters. The grid search algorithm is guided by the performance and evaluation of the out-of-sample data. This process can be done by generating a range of values for C and sigma to search through first. The way used in this paper to generate the values is:

$C = 2^{-1}, 2^{-0.9}, 2^{-0.8}, 2^{-0.7}, \dots, 2^0, 2^{0.1}, 2^{0.2}, 2^{0.3}, \dots, 2^1$ and this is done for sigma as well. Once we find the best parameters, we do another exhaustive search for a very small range where our best parameters are in. The range -1 to 1 is an example to show how it works. This range in this paper was started from 0.001 to 2^5 with increment of 0.001 for the search. Next, we do comprehensive search for all possible pairs of C and sigma in order to obtain the best classification accuracy of the in-sample data with the optimized parameters [17].

Chapter 3 Goals Hypothesis and Evaluation Method

3.1 Goals

The main goal of this work was to create a prediction method for the direction of the monthly trend using an appropriate set of data.

The second goal of this work was to learn about the techniques used with Support Vector Machine in computational finance. With all the analysis tools available and the market volatility, it is a hard task to achieve accurate prediction, especially with different kinds of market data that is available. Learning how to classify the data to perform more accurate prediction to the trend direction was an important objective due to unexpected movement of the market.

3.2 Hypothesis

The hypothesis of this work was the following:

The financial markets are complex, evolutionary, and non-linear dynamic systems. The market's trend direction can be identified by different type of large data sets. Therefore, predicting and forecasting the market trend is a difficult task. Given the right technical and/or macroeconomic data to a machine learning classifier, such as the Support Vector Machine, it is possible to classify the direction of the market's trend and make accurate investing choices regarding the market and reduce the risk involved.

3.3 Evaluation Method

A simulated predicting system will be constructed using Matlab to test this hypothesis. This system designed will give the option between which features will be used to the SVM classifier and the ability of editing the parameters provided by the classifier in order to maximize the performance. The system will simulate the prediction over a given time period for testing and evaluation. The performance will be measured by the classification accuracy during the in-sample and out-of-sample. The classification accuracy is the evaluation results of the total number of correctly classified targets compared to the total number of targets.

Chapter 4: Design

The tool selected to design the prediction simulator was Matlab because of its power and simplicity at the same time. The features used are available mostly in the internet from reliable sources. The prediction simulator was designed to be simple enough and flexible to change the testing period, classifier's kernel, and data selection and reduction.

4.1 Prediction Model

In this work, using different type of features and kernels for classification, a model was created in order to find the direction of the trend for the following month.

4.1.1 Data Construction

The input data used in this work are separated into two types; macroeconomic and technical data of the S&P 500 (symbol: SPY). The macroeconomic data was prepared by Amit Goyal and Ivo Welch [18]. The data provided are: DY, EP, DE, SVAR, BM, NTIS, TBL, LTY, LTR, TMS, DFY, DFR and INFL. One extra input was added from the list which is EQ, Equity Premium, as follows: The equity risk premium is the difference between the compound market return and the log return on a risk-free Treasury bill. From the previous statement, we concluded $EQ = \text{Compound Return} - \log(1+R_{\text{free}})$. The index price was provided by [18] which open, close, high, low were obtained from the

index price itself. Close price is the index current month's price while open is the previous month's index price. High is defined as the maximum index price over the last 12 months. Low is defined in the same way as high, the lowest index price over the last 12 months. Since we were looking at monthly data with no volume provided, volume indicators were excluded. The data available is from January 1871 to December 2011, which is total of 1680 months of data. The index's monthly price is the closing price of the last trading day of the month. The time period investigated in this work was from June 1938 through December 2010 with the out-of-sample starting in January 1975. Out of 883 trading months used in this work, 439 were used as training data and the remaining 444 used as testing data. The training period was 49.71% while the testing period was 50.29%. The total features constructed in this work were 27. 14 of the total features were macroeconomic while the 13 left were technical features. The construction of the features in Matlab was done through TA-Lib: Technical Analysis Library which is available as an open-source [19]. The macroeconomic inputs are:

1. Dividend price-ratio, DP, is the log of dividends minus the log of prices.
2. Dividend Yield, DY, is the log of dividends minus the log of lagged prices.
3. Earnings are 12-month moving sums of earnings on the S&P 500 index.
Earning Price Ratio, EP, is the log of earnings minus the log of prices.
4. Dividend Payout Ratio, DE, is the log of dividends minus the log of earnings.

5. Stock Variance, SVAR, is the sum of the monthly return on the S&P 500.
6. Book-to-Market, BM, is the ratio of book value to market value for the Dow Jones Industrial Average.
7. Net Equity Expansion, NTIS, is the ratio of 12-month moving sums of net issues by NYSE listed stocks divided by the total end-of-year market capitalization of NYSE stocks.
8. Treasury Bills, TBL, is the interest rate on a three-month Treasury bill.
9. Long term yield, LTY, is the long-term government bond yield.
10. Long term return, LTR, is the long-term government bond yield.
11. The Term Spread, TMS, is the long term yield on government bonds minus the Treasury-bill.
12. Default Yield Spread, DFY, is the difference between BAA and AAA-rated corporate bond yields.
13. Default Return Spread, DFR, is the difference between long-term corporate bond and long-term government bond returns.
14. Inflation, INFL, is the Consumer Price Index calculated from All Urban Consumers.
15. DY12 calculated as the difference between log dividends from P_{t-12} to P_t at time t .

When constructing the compound return using the given index price from the data in [18] and Yahoo! Finance, there is a mismatch. However, only 9 out of the 1692 data points are not the same when constructing the earnings vector

to use for training and testing. As a result of this, there is a possible error of 0.53% or less. The days we found which mismatched are:

Mismatch Date	Price	Previous Month's Price
April 1974	98.44	98.42
April 1979	101.76	101.59
September 1979	109.32	109.32
April 1984	160.05	159.18
January 1986	211.78	211.28
April 1991	375.35	375.22
June 1996	670.63	669.12
February 2006	1280.66	1280.08
June 2006	1270.20	1270.09

Table 4.1 Dates of mismatched earnings

From the table 4.1, we notice in those mismatched months, the earnings are so small for each that when we take the difference of the earnings and log of the risk-free, the number we get is negative but during our class labeling, those numbers came out as positive (prior to taking the earnings difference with risk-free).

The technical inputs used are shown in Table 4.2.

Input #	Definition
1	$RSI(c, t)$
2	$\frac{c - BBhigh}{BBhigh}$
3	$\frac{c - BBlow}{BBlow}$
4	$\%K(t)$
5	$\%D(t)$
6	$\%K(t) - \%K(t - 1)$
7	$\%D(t) - \%D(t - 1)$

8	$\frac{c(t) - c(t - 1)}{c(t - 1)}$
9	$\frac{c(t) - l(t)}{h(t) - l(t)}$
10	$\frac{SMA(c, 10) - SMA(c(t - 1), 10)}{SMA(c(t - 1), 10)}$
11	$\frac{SMA(c, 21) - SMA(c(t - 1), 21)}{SMA(c(t - 1), 21)}$
12	$\frac{SMA(c, 10) - SMA(c(t - 1), 21)}{SMA(c(t - 1), 21)}$
13	$\frac{c(t) - SMA(c, 21)}{SMA(c, 21)}$
14	$\frac{c(t) - \min(c, 5)}{\min(c, 5)}$
15	$\frac{BBhigh - BBlow}{BBhigh - BBlow}, 5$
16	$\frac{SMA(c, 2) - SMA(c, 12)}{SMA(c, 12)}$
17	$\frac{c(t) - c(t - 12)}{c(t - 12)}$

Table 4.2 Set of Technical Indicators Used

Where:

- BBhigh and BBlow are the upper Bollinger Bands and lower Bollinger Bands.
- c is the monthly price of the index.
- t is the time.

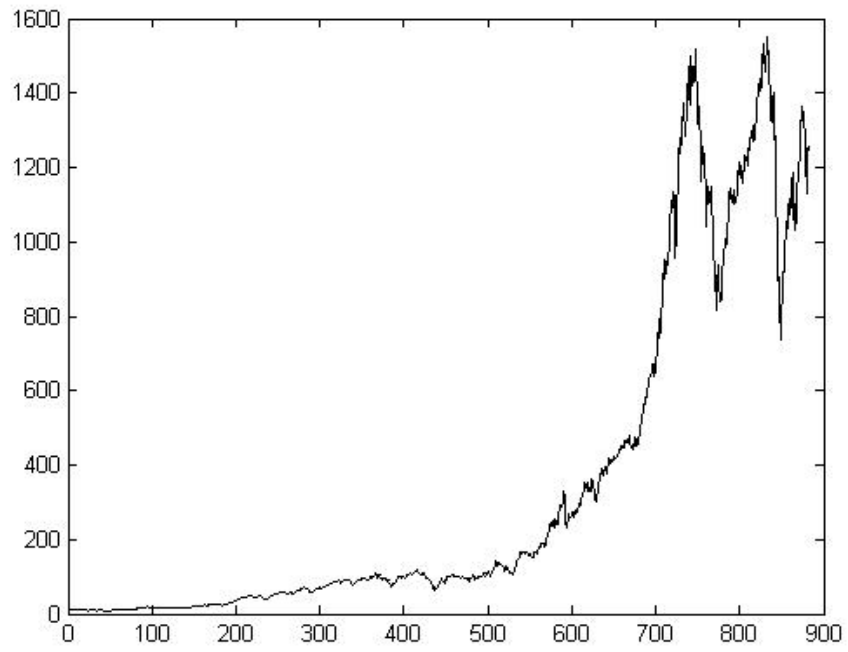


Figure 4.1 S&P 500 Monthly index over the training and testing period

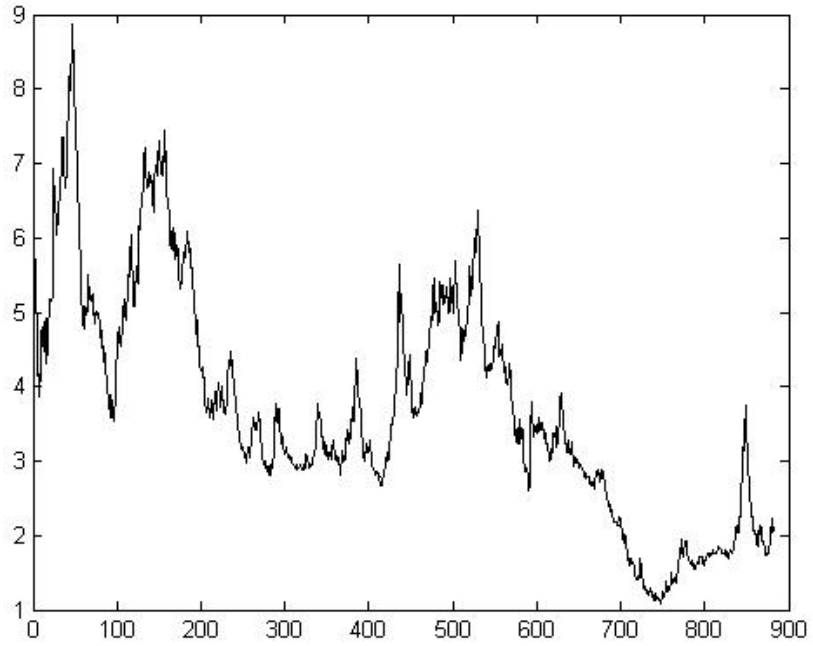


Figure 4.2 S&P 500 DE movements over the training and testing period

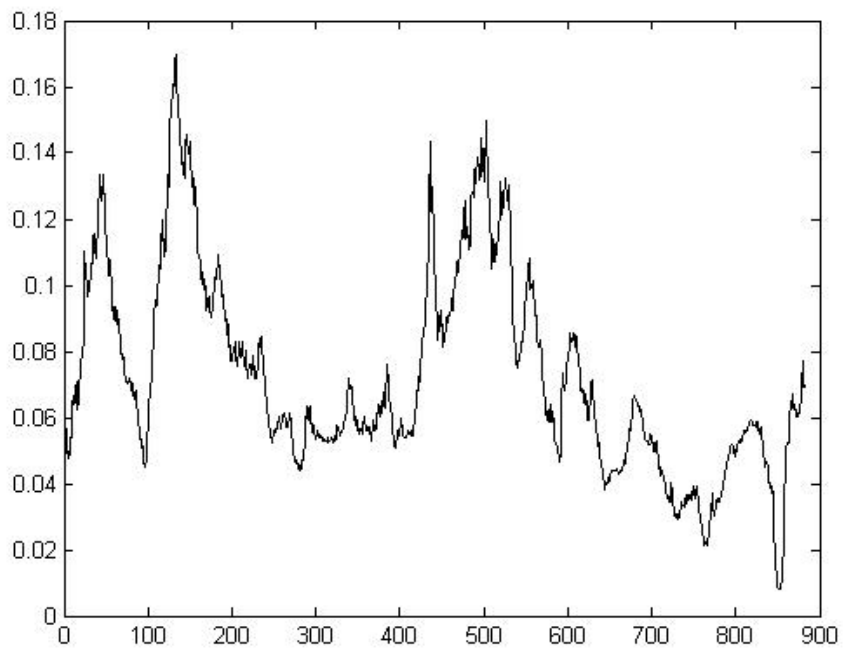


Figure 4.3 S&P 500 EP movements over the training and testing period

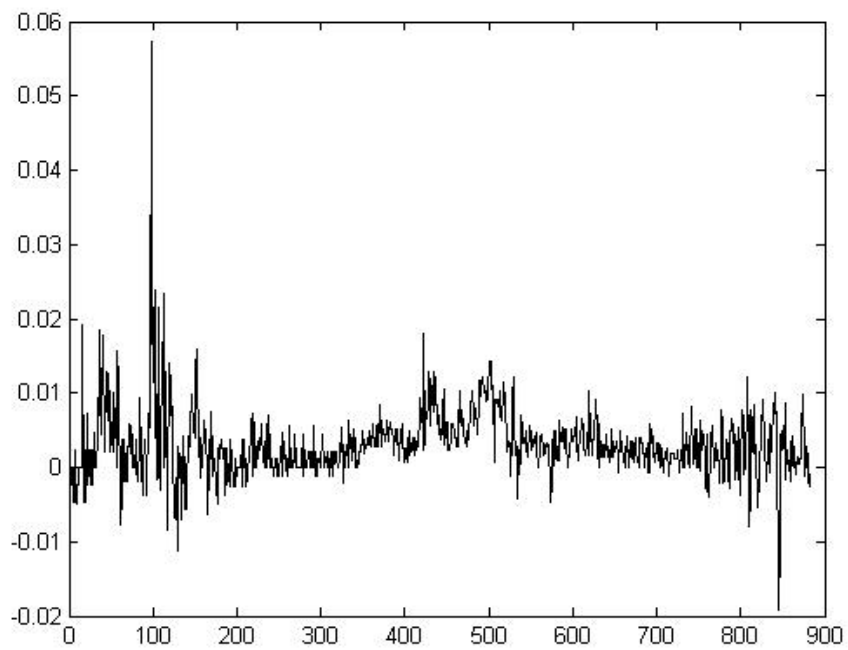


Figure 4.4 S&P 500 INFL movements over the training and testing period

4.1.2 Classification

The price of the S&P 500 is a stock market index represented in dollar value. This work deals with S&P 500 price in time series. A classification method is best to represent the movement of S&P 500 price in a simplified way. The classification was calculated using a simple difference method; the current month's index price – previous month's index price. The classification then would assign a 1 if next month's index price is higher or equal to the current month and 0 if the price is less than the current month.

4.1.3 Data Normalization

It is essential to normalize the data when using a classifier such Support Vector Machine because of features computed may have different value ranges between minimum that is below 0 and maximum to higher than thousands [20]. If features dimensions have fewer variations, it will take less time for SVM to learn and no certain feature that is dominating due to features having fewer dimensions which could impact the behavior over the test data. Normalization is done using the functions 'zscore', 'normc', and 'normalize'.

4.1.4 Proper Data Handling

Handling the data improperly to the classifier can result in inaccurate classification. When handling all the data at once (in-sample and out-of-sample), the SVM classifier will normalize both periods in a one-time operation. The

classifier at this point will realize the maximum value in the out-of-sample and this will affect the accuracy of the classification process. First, normalize the in-sample training data and train the classifier. Normalize the first subset of out-of-sample data as it will be known at this point and the classifier will not be considered looking at the future. Test the classifier for the current out-of-sample data and store the classification result in an array. Next, include the new subset of the out-of-sample data for new normalization (this subset is known at this point) and retrain the classifier for testing. Store the result in the classification array and redo the steps until the out-of-sample data is complete [21].

4.1.5 Data reduction and selection

The features used in this work were a total of 15 for macroeconomic and 17 for technical. High dimension problems cause difficulty in classification because of creating many noise features which does not result in contribution to the classification system rather reduces the classification accuracy [22]. Two different methods were used separately in this work in effort to reduce the unnecessary features used while maintaining the robustness of the classification system; Sequential Feature Selection and Rankfeatures. By reducing the features used, the classifier will be dealing with fewer features to learn from. Reducing the features to the minimum useful while improving the performance in this work was done by looking at the criterion values and the in-sample accuracy

only, excluding out-of-sample during this procedure. This was done this way because it is not considered looking at future data to take off the data that wasn't useful in out-of-sample.

4.1.6 Frequent Index's Price Oscillation

The index's price frequent oscillation in a short period and the ability of the classifier to follow up with changes was an important factor in this work. For example, when in 4 consecutive months, the actual classification records for price movement 1, 0, 1, 0, the classifier needed to follow those short term price oscillation rather than long term price movement (i.e., 6 months in a row classification is 1 and then another 4 months classification is 0).

4.2 Classifier Data Processing Kernel

In this work, four different SVM kernels were investigated. The goal was to find the best kernel to classify the data and have a good separation hyperplane between the data sets. Not in all cases the data can be separated, SVM in this case tends to soften the margin in order to separate as much as possible of the data. The kernels used are linear, RBF, quadratic, and polynomial. Finding the best parameters for RBF classifier to soften the margin was done using gridsearch method [23].

Chapter 5: Experiments and Results

5.1 SVM Classification

We were drawn to do this work by the paper: “Predicting S&P 500 Returns Using Support Vector Machines: Theory and Empirics” [24] in which a claim was made of achieving an 86% classification accuracy (we will later show that this claim is unsubstantiated). The model used the given data sets for testing period to predict the direction of the next month’s closing price of the S&P 500. We explore different kernels for the SVM to find the best kernel to classify the data effectively. The features used were macroeconomic and technical. They were each used separately and then combined together with the aim of possibly achieving the highest accuracy in prediction. The same macroeconomic features introduced in [24] were used as an input for the SVM classifier. The technical features used in [25], the same features in Table 4.2, were used as input to the SVM classifier. A combination of both macroeconomic and technical features then was used. The data were normalized using functions, ‘zscore’, ‘normc’, and ‘normalize’ in Matlab.

5.1.1 Macroeconomic Features

The results for the macroeconomic data test with zscore data normalizing can be seen in Table 5.1. The average in-sample accuracy was 82.92% for the four different kernels. The average out-of-sample prediction accuracy was 50.92%. The out-of-sample performance for both RBF and quadratic kernels are

the best with 55.79% accuracy with the RBF kernel and 54.86% with quadratic. The polynomial kernel performed the best during the in-sample period but had a lower out-of-sample accuracy with 47.22% compared to the 100% accuracy performance during the in-sample period which leads one to conclude that the polynomial was nothing more than a guess work in this case. The RBF kernel was similar in performance to the polynomial in the out-of-sample but has less accuracy during the in-sample period. The RBF has a better success rate compared to the rest of the kernels when considering both the in-sample and out-of-sample accuracy.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	59.23%	50.46%
RBF	94.76%	55.79%
Polynomial	97.95%	52.08%
Quadratic	79.73%	54.86%

Table 5.1 Results for SVM classifier using Macroeconomic data and zscore normalization

Changing the data normalizing method from 'zscore' to 'normc', the out-of-sample accuracy was improved and became overall better than the zscore. The in-sample period accuracy was not as good as with 'zscore' when gaining 59.23% accuracy for all kernels. The average accuracy for the out-of-sample period was 55%. Classifying resulted in good results using 'normc' during the out-of-sample for all kernels.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	59.23%	56.02%
RBF	59.23%	55.56%

Polynomial	59.23%	56.02%
Quadratic	59.23%	55.79%

Table 5.2 Results for SVM classifier using Macroeconomic data and normc normalization

The function ‘normalize’ performed slightly better than ‘zscore’ during the out-of-sample period but featured less accuracy using quadratic kernel when compared to normalization with zscore in the out-of-sample. The RBF kernel responded well to the normalization with ‘normalize’ to gain 53.47% accuracy in the out-of-sample period which was close to the best performing quadratic kernel.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	59.68%	50.23%
RBF	66.51%	53.47%
Polynomial	72.67%	53.70%
Quadratic	66.51%	53.94%

Table 5.3 Results for SVM classifier using Macroeconomic data with ‘normalize’ function

Based on our results obtained during the experiment with SVM classification with macroeconomic data and the promotion of the RBF kernel in the paper “Active Learning with Support Vector Machines” [26], we decided to choose RBF kernel and zscore data scaling to investigate the results presented in this paper and compare it with the results in [24]. All of the out-of-sample SVM predictions are presented in Table 5.3. Overall, 241 out of 432 predictions were correct, yielding to 55.79% accuracy. One thing we notice from the SVM performance was the response to following the long term trend.

yyyymm	Prediction	Actual			
197501	1	1	197803	1	1
197502	1	1	197804	1	1
197503	1	1	197805	1	0
197504	1	1	197806	1	1
197505	1	1	197807	1	1
197506	1	0	197808	1	0
197507	1	0	197809	0	0
197508	1	0	197810	1	1
197509	0	1	197811	1	1
197510	1	1	197812	1	1
197511	1	0	197901	1	0
197512	0	1	197902	1	1
197601	1	0	197903	1	1
197602	0	1	197904	1	0
197603	1	0	197905	1	1
197604	0	0	197906	1	1
197605	0	1	197907	1	1
197606	0	0	197908	1	1
197607	0	0	197909	1	0
197608	0	1	197910	1	1
197609	0	0	197911	1	1
197610	0	0	197912	1	1
197611	0	1	198001	1	0
197612	0	0	198002	1	0
197701	0	0	198003	1	1
197702	0	0	198004	1	1
197703	0	1	198005	1	1
197704	0	0	198006	1	1
197705	0	1	198007	1	1
197706	0	0	198008	1	1
197707	0	0	198009	1	1
197708	0	0	198010	1	1
197709	0	0	198011	0	0
197710	0	1	198012	0	0
197711	0	1	198101	0	1
197712	1	0	198102	1	1
197801	1	0	198103	1	0
197802	0	1	198104	1	0

198105	1	0	198408	0	0
198106	1	0	198409	0	0
198107	1	0	198410	0	0
198108	1	0	198411	0	1
198109	1	1	198412	0	1
198110	1	1	198501	0	1
198111	1	0	198502	0	0
198112	1	0	198503	0	0
198201	1	0	198504	0	1
198202	1	0	198505	0	1
198203	1	1	198506	0	0
198204	1	0	198507	0	0
198205	1	0	198508	0	0
198206	1	0	198509	0	1
198207	1	1	198510	0	1
198208	1	1	198511	0	1
198209	1	1	198512	0	1
198210	0	1	198601	0	1
198211	0	1	198602	0	1
198212	0	1	198603	0	0
198301	0	1	198604	0	1
198302	0	1	198605	0	1
198303	0	1	198606	0	0
198304	1	0	198607	0	1
198305	0	1	198608	0	0
198306	0	0	198609	0	1
198307	0	1	198610	0	1
198308	0	1	198611	1	0
198309	0	0	198612	0	1
198310	0	1	198701	0	1
198311	0	0	198702	1	1
198312	0	0	198703	1	0
198401	0	0	198704	0	1
198402	0	1	198705	1	1
198403	0	1	198706	1	1
198404	0	0	198707	1	1
198405	0	1	198708	1	0
198406	0	0	198709	1	0
198407	0	1	198710	0	0

198711	0	1	199102	1	1
198712	0	1	199103	1	1
198801	0	1	199104	1	1
198802	0	0	199105	1	0
198803	0	1	199106	1	1
198804	0	1	199107	1	1
198805	0	1	199108	1	0
198806	0	0	199109	1	1
198807	0	0	199110	1	0
198808	0	1	199111	1	1
198809	0	1	199112	1	0
198810	0	0	199201	1	1
198811	0	1	199202	1	0
198812	0	1	199203	1	1
198901	0	0	199204	1	1
198902	0	1	199205	1	0
198903	0	1	199206	1	1
198904	0	1	199207	1	0
198905	0	0	199208	1	1
198906	0	1	199209	1	1
198907	0	1	199210	1	1
198908	0	0	199211	1	1
198909	0	0	199212	1	1
198910	0	1	199301	1	1
198911	1	1	199302	1	1
198912	1	0	199303	1	0
199001	1	1	199304	1	1
199002	1	1	199305	1	1
199003	1	0	199306	1	0
199004	1	1	199307	1	1
199005	1	0	199308	1	0
199006	1	0	199309	1	1
199007	1	0	199310	1	0
199008	1	0	199311	1	1
199009	1	0	199312	1	1
199010	1	1	199401	1	0
199011	1	1	199402	1	0
199012	1	1	199403	1	1
199101	1	1	199404	1	1

199405	1	0	199708	1	1
199406	1	1	199709	1	0
199407	1	1	199710	1	1
199408	1	0	199711	1	1
199409	1	1	199712	1	1
199410	1	0	199801	1	1
199411	0	1	199802	1	1
199412	0	1	199803	1	1
199501	0	1	199804	1	0
199502	1	1	199805	1	1
199503	0	1	199806	1	0
199504	1	1	199807	1	0
199505	1	1	199808	1	1
199506	1	1	199809	1	1
199507	1	0	199810	1	1
199508	1	1	199811	1	1
199509	1	0	199812	1	1
199510	1	1	199901	1	0
199511	1	1	199902	1	1
199512	1	1	199903	1	1
199601	1	1	199904	1	0
199602	1	1	199905	1	1
199603	1	1	199906	1	0
199604	1	1	199907	1	0
199605	1	1	199908	1	0
199606	1	0	199909	1	1
199607	1	1	199910	1	1
199608	1	1	199911	1	1
199609	1	1	199912	1	0
199610	1	1	200001	1	0
199611	1	0	200002	1	1
199612	1	1	200003	1	0
199701	1	1	200004	0	0
199702	1	0	200005	0	1
199703	1	1	200006	0	0
199704	1	1	200007	0	1
199705	1	1	200008	0	0
199706	1	1	200009	0	0
199707	1	0	200010	0	0

200011	0	1	200402	1	0
200012	0	1	200403	1	0
200101	0	0	200404	1	1
200102	0	0	200405	1	1
200103	0	1	200406	1	0
200104	0	1	200407	1	1
200105	0	0	200408	1	1
200106	0	0	200409	1	1
200107	0	0	200410	1	1
200108	0	0	200411	1	1
200109	0	1	200412	1	0
200110	0	1	200501	1	1
200111	0	1	200502	1	0
200112	1	0	200503	1	0
200201	0	0	200504	1	1
200202	0	1	200505	1	0
200203	0	0	200506	1	1
200204	0	0	200507	1	0
200205	0	0	200508	1	1
200206	0	0	200509	1	0
200207	0	1	200510	1	1
200208	0	0	200511	1	0
200209	0	1	200512	1	1
200210	0	1	200601	1	1
200211	0	0	200602	1	1
200212	0	0	200603	1	1
200301	0	0	200604	1	0
200302	0	1	200605	1	1
200303	0	1	200606	1	1
200304	0	1	200607	1	1
200305	0	1	200608	1	1
200306	1	1	200609	1	1
200307	1	1	200610	1	1
200308	1	0	200611	1	1
200309	1	1	200612	1	1
200310	1	1	200701	1	0
200311	1	1	200702	1	1
200312	1	1	200703	1	1
200401	1	1	200704	1	1

200705	1	0	200909	1	0
200706	1	0	200910	0	1
200707	1	1	200911	1	1
200708	1	1	200912	1	0
200709	1	1	201001	1	1
200710	1	0	201002	1	1
200711	1	0	201003	1	1
200712	1	0	201004	1	0
200801	1	0	201005	1	0
200802	1	0	201006	1	1
200803	1	1	201007	1	0
200804	1	1	201008	1	1
200805	1	0	201009	1	1
200806	1	0	201010	1	0
200807	1	1	201011	1	1
200808	1	0	201012	1	1
200809	0	0			
200810	0	0			
200811	0	1			
200812	1	0			
200901	0	0			
200902	0	1			
200903	0	1			
200904	1	1			
200905	1	1			
200906	1	1			
200907	1	1			
200908	1	1			

Table 5.4 Out-of-sample SVM predictions vs. actual realization

5.1.2 Technical Features

The work in [24] indicates the use of macroeconomic variables will tend to lead to superior prediction rates compared to the use of technical features. The next step in this work was to substitute the macroeconomic features with the technical features presented in [25]. The first test was to use technical features with zscore. The accuracy of the classification can be seen in Table 5.5.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	60.59%	51.16%
RBF	95.90%	59.26%
Polynomial	99.32%	49.77%
Quadratic	77.68%	49.54%

Table 5.5 Results for SVM classifier using technical features and zscore normalization

The RBF and Polynomial kernels performed better during the in-sample with technical features as well. The polynomial kernel was able to perform the best during the in-sample period but not as well during out-of-sample to result in classification accuracy below 50%. Compared to the macroeconomic features, the classification accuracy of the RBF was the best at 59.26% to outperform the best performance made using macroeconomic features. The quadratic kernel had better results using the macroeconomic features compared to using technical features during the out-of-sample test.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	56.04%	48.15%
RBF	56.04%	48.15%
Polynomial	55.58%	46.99%

Quadratic	56.04%	46.99%
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Table 5.6 Results for SVM classifier using technical features and normc normalization

Next, the data scaling was tested using normc function and the results can be seen in Table 5.6. Normc shows very similar performance during the in-sample and out-of-sample periods. Classification with technical data showed similar behavior when using the normc to classifying with macroeconomic features. All kernels had similar results for the in-sample and out-of-sample

The next step was to perform data normalization use the 'normalize' function. The polynomial kernel made a noticeable improvement in comparison with its performance using the normc and zscore functions. It outperformed the normc function and was able to achieve higher than 50% classification accuracy during the out-of-sample test period. From Table 5.7, the best performing kernel was the RBF with 55.56% accuracy during the out-of-sample period.

Kernel	In-Sample Accuracy %	Out-Of-Sample Accuracy %
Linear	61.73%	52.55%
RBF	61.96%	55.56%
Polynomial	69.25%	51.39%
Quadratic	64.24%	54.63%

Table 5.7 Results for SVM classifier using technical features and normalize function

The classification results using zscore are still the best even when using technical features which are simple to obtain compared to macroeconomic data. Looking closely at classification results of the best overall performing kernel with technical features, the RBF with zscore data normalizing, the classifier predicted

256 out-of-sample data correctly out of 432. The classifier with technical features responded well to the short trend oscillation and making classification accuracy close to 60%. The following table shows detailed results of classification with technical features and RBF kernel:

yyymm	Prediction	Actual			
197501	1	1	197707	0	0
197502	1	1	197708	1	0
197503	1	1	197709	0	0
197504	1	1	197710	0	1
197505	1	1	197711	1	1
197506	1	0	197712	1	0
197507	1	0	197801	0	0
197508	1	0	197802	0	1
197509	1	1	197803	1	1
197510	0	1	197804	1	1
197511	0	0	197805	1	0
197512	1	1	197806	0	1
197601	1	0	197807	1	1
197602	1	1	197808	1	0
197603	1	0	197809	1	0
197604	1	0	197810	1	1
197605	1	1	197811	0	1
197606	1	0	197812	1	1
197607	1	0	197901	0	0
197608	1	1	197902	1	1
197609	1	0	197903	0	1
197610	1	0	197904	1	0
197611	1	1	197905	1	1
197612	1	0	197906	1	1
197701	1	0	197907	1	1
197702	0	0	197908	0	1
197703	0	1	197909	1	0
197704	1	0	197910	1	1
197705	1	1	197911	0	1
197706	0	0	197912	0	1

198001	1	0	198304	1	0
198002	0	0	198305	0	1
198003	1	1	198306	1	0
198004	1	1	198307	1	1
198005	1	1	198308	1	1
198006	1	1	198309	1	0
198007	1	1	198310	0	1
198008	0	1	198311	1	0
198009	0	1	198312	0	0
198010	1	1	198401	0	0
198011	1	0	198402	1	1
198012	1	0	198403	0	1
198101	1	1	198404	1	0
198102	1	1	198405	1	1
198103	1	0	198406	0	0
198104	0	0	198407	1	1
198105	0	0	198408	1	0
198106	0	0	198409	1	0
198107	0	0	198410	0	0
198108	0	0	198411	1	1
198109	1	1	198412	1	1
198110	1	1	198501	1	1
198111	0	0	198502	1	0
198112	1	0	198503	0	0
198201	0	0	198504	0	1
198202	1	0	198505	1	1
198203	1	1	198506	0	0
198204	1	0	198507	0	0
198205	0	0	198508	1	0
198206	1	0	198509	0	1
198207	0	1	198510	1	1
198208	1	1	198511	1	1
198209	0	1	198512	1	1
198210	1	1	198601	1	1
198211	1	1	198602	1	1
198212	1	1	198603	0	0
198301	1	1	198604	0	1
198302	1	1	198605	0	1
198303	1	1	198606	0	0

198607	1	1	198910	1	1
198608	0	0	198911	1	1
198609	1	1	198912	1	0
198610	1	1	199001	1	1
198611	0	0	199002	0	1
198612	0	1	199003	1	0
198701	1	1	199004	0	1
198702	1	1	199005	1	0
198703	1	0	199006	1	0
198704	1	1	199007	0	0
198705	1	1	199008	0	0
198706	0	1	199009	0	0
198707	0	1	199010	1	1
198708	0	0	199011	1	1
198709	1	0	199012	0	1
198710	1	0	199101	1	1
198711	1	1	199102	1	1
198712	1	1	199103	1	1
198801	1	1	199104	1	1
198802	1	0	199105	1	0
198803	1	1	199106	1	1
198804	0	1	199107	1	1
198805	0	1	199108	0	0
198806	1	0	199109	1	1
198807	0	0	199110	0	0
198808	0	1	199111	1	1
198809	1	1	199112	1	0
198810	1	0	199201	0	1
198811	1	1	199202	0	0
198812	0	1	199203	0	1
198901	1	0	199204	1	1
198902	1	1	199205	1	0
198903	0	1	199206	1	1
198904	0	1	199207	0	0
198905	1	0	199208	1	1
198906	0	1	199209	1	1
198907	1	1	199210	1	1
198908	1	0	199211	1	1
198909	0	0	199212	1	1

199301	1	1	199604	1	1
199302	1	1	199605	1	1
199303	1	0	199606	1	0
199304	0	1	199607	1	1
199305	1	1	199608	1	1
199306	1	0	199609	0	1
199307	1	1	199610	0	1
199308	0	0	199611	1	0
199309	1	1	199612	1	1
199310	1	0	199701	1	1
199311	1	1	199702	1	0
199312	1	1	199703	1	1
199401	0	0	199704	1	1
199402	1	0	199705	1	1
199403	0	1	199706	1	1
199404	1	1	199707	1	0
199405	1	0	199708	1	1
199406	0	1	199709	0	0
199407	0	1	199710	1	1
199408	1	0	199711	0	1
199409	1	1	199712	0	1
199410	0	0	199801	0	1
199411	0	1	199802	1	1
199412	0	1	199803	1	1
199501	0	1	199804	0	0
199502	1	1	199805	1	1
199503	1	1	199806	0	0
199504	0	1	199807	1	0
199505	0	1	199808	1	1
199506	1	1	199809	1	1
199507	1	0	199810	1	1
199508	0	1	199811	1	1
199509	0	0	199812	1	1
199510	1	1	199901	1	0
199511	0	1	199902	1	1
199512	0	1	199903	1	1
199601	1	1	199904	1	0
199602	1	1	199905	1	1
199603	1	1	199906	1	0

199907	0	0	200210	1	1
199908	0	0	200211	1	0
199909	1	1	200212	1	0
199910	1	1	200301	0	0
199911	0	1	200302	0	1
199912	1	0	200303	1	1
200001	1	0	200304	1	1
200002	1	1	200305	1	1
200003	1	0	200306	1	1
200004	0	0	200307	1	1
200005	1	1	200308	1	0
200006	0	0	200309	1	1
200007	1	1	200310	0	1
200008	0	0	200311	1	1
200009	1	0	200312	0	1
200010	0	0	200401	0	1
200011	0	1	200402	0	0
200012	0	1	200403	1	0
200101	1	0	200404	1	1
200102	1	0	200405	1	1
200103	1	1	200406	0	0
200104	1	1	200407	1	1
200105	0	0	200408	1	1
200106	0	0	200409	1	1
200107	0	0	200410	1	1
200108	0	0	200411	0	1
200109	0	1	200412	0	0
200110	0	1	200501	1	1
200111	1	1	200502	0	0
200112	1	0	200503	1	0
200201	0	0	200504	0	1
200202	0	1	200505	1	0
200203	1	0	200506	1	1
200204	0	0	200507	1	0
200205	1	0	200508	1	1
200206	1	0	200509	1	0
200207	1	1	200510	0	1
200208	1	0	200511	1	0
200209	1	1	200512	1	1

200601	1	1	200808	1	0
200602	1	1	200809	0	0
200603	1	1	200810	1	0
200604	0	0	200811	1	1
200605	0	1	200812	1	0
200606	0	1	200901	1	0
200607	1	1	200902	1	1
200608	0	1	200903	1	1
200609	1	1	200904	1	1
200610	0	1	200905	1	1
200611	0	1	200906	1	1
200612	0	1	200907	1	1
200701	0	0	200908	1	1
200702	0	1	200909	1	0
200703	1	1	200910	1	1
200704	0	1	200911	0	1
200705	0	0	200912	1	0
200706	0	0	201001	1	1
200707	1	1	201002	1	1
200708	1	1	201003	1	1
200709	1	1	201004	1	0
200710	0	0	201005	1	0
200711	0	0	201006	1	1
200712	0	0	201007	1	0
200801	1	0	201008	1	1
200802	1	0	201009	1	1
200803	1	1	201010	1	0
200804	1	1	201011	1	1
200805	0	0	201012	1	1
200806	1	0			
200807	1	1			

Table 5.8 Technical Out-of-sample SVM predictions vs. actual realization

5.2 SVM RBF Kernel Parameters Selection and Optimization

The next step was to adjust the width of SVM RBF classifier using parameters C and sigma which will control the margin of classification. One way to do this is with a grid search method as mentioned in the previous chapters and papers [27] and [28]. The goal of this search was to find the best pair of parameters during the in-sample period to maximize the out-of-sample accuracy as much as possible. The default values for both parameters in Matlab were “1” for parameters, C and sigma. At the end of our work, the parameter C was not modified, because once we optimized for the best value of sigma for the RBF kernel, if we were to modify the parameter C further, it would have resulted in a softer margin for classification. This will result in slow response of the classifier (i.e. keeping the classification rate at 1 or 0 for a long period of time).

From Figure 5.1 we notice during optimizing the RBF sigma parameter, setting the sigma parameter slightly higher than the default, the higher the accuracy we get. The optimal sigma parameter using macroeconomic features was $\text{Sigma} = 0.45$ which increased the performance for the out-of-sample period from 55.79% to 59.25% with zscore data normalizing.

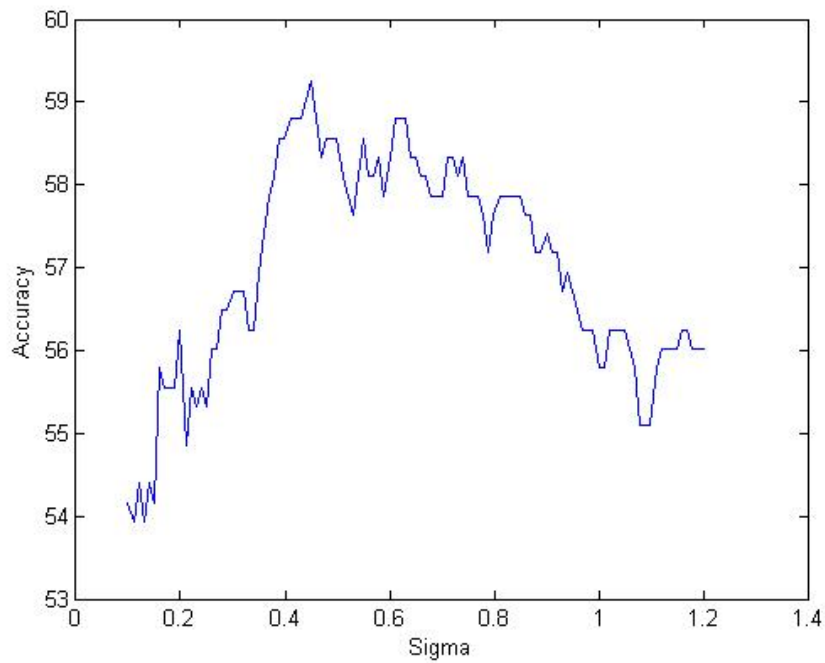


Figure 5.1 Out-of-sample accuracy using macroeconomic data vs. parameters change

Optimizing the RBF parameters to the classifier using technical features input showed noticeable improvement. From figure 5.2, the parameter sigma increased the out-of-sample accuracy to 62.03% with the parameter $\text{Sigma} = 0.425$. This change increased the out-of-sample classification accuracy by 2.77% from 59.26% to 62.03%. The data normalization method used was zscore. Technical features made a better out-of-sample accuracy with the optimized parameters than macroeconomic features.

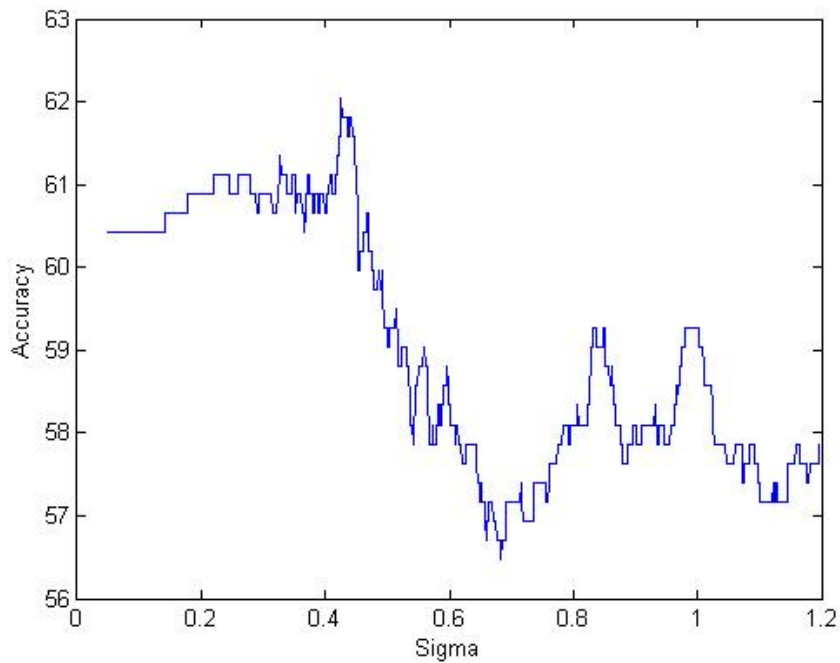


Figure 5.2 Out-of-sample accuracy using technical data vs. parameters change

5.3 Feature Selection and Dimensionality Reduction

The goal of feature reduction was to reduce the problem dimensionality by reducing the dataset in order to exclude irrelevant features and at the same time not have the dataset too small to cause the classifier to be over fit [29].

Sequential Feature Selection and Rankfeatures tests were performed in order to find the minimum possible features needed. The tests were performed to linear and RBF kernels since they are used mostly in this kind of work.

5.3.1 Sequential Feature Selection

5.3.1.1 Sequential Feature Reduction with Macroeconomic Features

Linear Kernel:

Sequential Feature Selection was performed using the most widely used two kernels in this sort of application from section 5.1 to both, macroeconomic and technical features. Table 5.9 shows the features significance using linear kernel and 'zscore' data scaling.

Feature Rank	Feature #
1	14
2	4
3	5
4	7
5	1
6	3
7	15
8	2
9	8
10	10
11	6
12	9
13	13
14	11
15	12

Table 5.9 Macroeconomic Features Significance Ranking using Sequential Feature and linear kernel

Table 5.10 shows the results of Sequential Feature Selection test using macroeconomic data, zscore data scaling, and linear kernel.

# of Features	Out-of-Sample Accuracy
1	60.42%
2	40.50%
3	40.50%
4	40.27%
5	42.13%
6	46.29%
7	45.83%
8	45.83%
9	53.93%
10	53.24%
11	51.15%
12	50.92%
13	50.69%
14	51.38%
15	50.46%

Table 5.10 Sequential Feature Selection for macroeconomic data with Linear Kernel

From the Table 5.10, we notice that only one feature, namely inflation, out of 15 resulted in the best performance for linear kernel.

RBF Kernel:

Using an RBF kernel gave us different results from the linear kernel.

Using 'zscore' when reducing the number of features, we were able to obtain the best result for macroeconomic with sequential feature reduction where the best out-of-sample accuracy was 58.33% using 3 features only (TBL, DFR, and DFY) as seen in Table 5.12. Table 5.11 shows the features significance using RBF kernel.

Feature Rank	Feature #
1	8
2	13
3	12
4	15
5	5
6	10
7	14
8	4
9	7
10	6
11	11
12	3
13	2
14	1
15	9

Table 5.11 Macroeconomic Features Significance Ranking using Sequential Feature and RBF kernel

# of Features	Out-of-Sample Accuracy
1	55.09%
2	55.55%
3	58.33%
4	53.70%
5	54.16%
6	53.93%
7	53.70%
8	53.47%
9	53.70%
10	52.54%
11	52.31%
12	54.39%
13	56.25%
14	55.79%
15	55.79%

Table 5.12 Sequential Feature Selection accuracy for macroeconomic data and 'zscore normalization and RBF Kernel

5.3.1.2 Sequential Feature Reduction with Technical Features

Linear Kernel:

The significance and ranking of each of the technical features can be seen in Table 5.13.

Feature Rank	Feature #
1	9
2	15
3	1
4	2
5	3
6	6
7	14
8	10
9	5
10	7
11	4
12	17
13	8
14	16
15	11
16	12
17	13

Table 5.13 Sequential Feature Selection for technical data and linear kernel

Feature reduction with linear kernel and technical features showed an improvement in the out-of-sample classification that can be seen in Table 5.13.

To achieve the best performance for the classifier, less features was given to the classifier. Using only 2 features (please refer to Table 4.2,) we were able to get 57.87% accuracy. The more features we add, the worse the performance became.

# of Features	Out-of-Sample Accuracy
1	55.78%
2	57.87%
3	56.71%
4	57.17%
5	55.32%
6	54.16%
7	53.70%
8	53.70%
9	54.63%
10	53.24%
11	55.78%
12	53.93%
13	54.63%
14	52.77%
15	52.54%
16	51.62%
17	51.15%

Table 5.14 Sequential Feature Selection for technical data and 'zscore' normalization and Linear Kernel

RBF:

Another test of feature reduction was performed to the technical features but this time using an RBF kernel. Using technical features with RBF kernel, the more features we added, the better the accuracy we achieved. Classifying using all features resulted in the best accuracy than classifying with a reduced number

of features. The best accuracy achieved was 59.26%. We got the second best results with only 9 features achieving an accuracy of 58.33%. Table 5.15 shows the significance features using RBF kernel.

Feature Rank	Feature #
1	1
2	14
3	2
4	8
5	12
6	7
7	3
8	6
9	15
10	17
11	10
12	4
13	9
14	5
15	11
16	16
17	13

Table 5.15 Sequential Feature Selection for technical data and RBF kernel

# of Features	Out-of-Sample Accuracy
1	50%
2	50.46%
3	51.85%
4	53.70%
5	54.39%
6	54.16%
7	54.63%
8	58.10%
9	58.33%

10	54.63%
11	55.09%
12	54.39%
13	55.55%
14	55.78%
15	57.63%
16	58.33%
17	59.26%

Table 5.16 Sequential Feature Selection for technical data and 'zscore' normalization and RBF Kernel

5.3.2 Rankfeatures

A simpler approach to identify the significant features was to assume all values are independent and compute a two-way t-test. Computing this test will return the index with features ranked in order of their effectiveness ranked with criterion absolute value. This test was used to relate whether the average difference between two groups was really significant or if it was due instead to data being random and not associated with each other [30]. We used the Matlab Rankfeatures function available in the bioinformatics toolbox.

Macroeconomic Features:

Feature Rank	Feature #
1	14
2	11
3	8
4	9
5	10
6	15
7	7

8	4
9	2
10	1
11	6
12	13
13	3
14	5
15	12

Table 5.17 Macroeconomic features significance with Rankfeatures

Table 5.17 shows the features significance in order using Rankfeatures.

Feature Rank	Out-of-Sample Accuracy
1	60.42%
2	53.24%
3	52.54%
4	52.31%
5	51.85%
6	53.24%
7	53.47%
8	53.24%
9	52.31%
10	53.47%
11	55.78%
12	56.02%
13	56.02%
14	56.02%
15	55.79%

Table 5.18 Rankfeatures Accuracy with macroeconomic features

Table 5.18 shows the accuracy of the classifier with Rankfeatures reducing the input features with RBF kernel and 'zscore' normalizing. Rankfeatures showed an improvement with the reduced features compared to using all features with

macroeconomic by improving the out-of-sample accuracy to 60.42% using the inflation feature.

Technical Features:

Table 5.19 shows the ranking of features significance for the technical features.

Ranking	Feature
1	3
2	7
3	9
4	16
5	14
6	4
7	5
8	6
9	17
10	2
11	10
12	13
13	1
14	15
15	8
16	12
17	11

Table 5.19 Technical features significance with Rankfeatures

# of Features	Out-of-Sample Accuracy
1	50.23%
2	55.79%
3	55.56%
4	56.48%
5	55.56%
6	55.09%

7	54.86%
8	56.02%
9	54.86%
10	52.55%
11	54.17%
12	55.79%
13	54.86%
14	56.25%
15	56.48%
16	55.32%
17	59.26%

Table 5.20 Rankfeatures Accuracy with technical features

Table 5.20 shows how technical features did not respond well to Rankfeatures. Rankfeatures did not identify the significant features in comparison with Sequential Feature Selection for the technical features. Most of the out-of-sample accuracies were not close to the best classification result when including all features. Overall, Rankfeatures worked better with macroeconomic features compared to technical features.

5.4 Combining Macroeconomic with Technical Features

One of the conclusions in the paper “A Comparison of PNN and SVM for Stock Market Trend Prediction using Economic and Technical Information,” was that predicting the market using macroeconomic data was more accurate when compared to technical indicators [31]. It also contends that the addition of both macroeconomic and technical features does not improve the classification accuracy. After running the set of technical features and feature reduction, we found that the best classification accuracy is achieved when all features are

used. Since the more features we add to the RBF classifier, we decided to expand the initial set of features by combining both the macroeconomic and technical features. The next step of this work after combining macroeconomic and technical features was to do a feature reduction to find the best classification accuracy. When combining all macroeconomic and technical features together, we were able to obtain 59.72% classification accuracy. This is only marginally better than using technical features alone.

Procedure	Out-of-Sample Accuracy	# of Features	C	Sigma
Combining Macroeconomic with Technical Features	59.72%	32	1	1

Table 5.21 Combination of macroeconomic and technical features

5.5 Summary of Results

Tables 5.22 and 5.23 are a summary of the best performing results and show a comparison between the experiments using macroeconomic and technical features alone. Improved accuracies were further obtained optimizing the SVM RBF parameters. The optimized parameter values are shown in the tables.

Procedure	Out-of-Sample Accuracy	# of Features	C	Sigma
All features	56.48%	15	1	1
Sequential Feature Reduction	60.41%	1	1	NA (linear)
Rankfeatures	60.42%	1	1	1
RBF Parameters Optimization	59.25%	15	1	0.45

Table 5.22 Summary of the performance results using macroeconomic features

Procedure	Out-of-Sample Accuracy	# of Features	C	Sigma
All features	59.26%	17	1	1
Sequential Feature Reduction	58.33%	9	1	1
Rankfeatures	56.48%	4	1	1
RBF Parameters Optimization	62.04%	17	1	0.425

Table 5.23 Summary of the performance results using technical features

From the above results, we can conclude the overall performance of the technical features was better than macroeconomic features in contrast to the result given in [31].

5.6 Comparison between Predictions Based on Basic Assumptions and SVM

The overall trend of the market over the long term is in the up direction. The next step was to evaluate and compare the classifier prediction performance during 3 different periods. The first period was the overall out-of-sample period from January 1975 – December 2010. The two other periods were when the US economy was hit by financial crisis. The first financial crisis period considered was from October 2000 – September 2002. This period represents the period of the bursting of the dot com bubble. The second period

was from October 2007 – July 2009, which was during the credit crisis. The classification was performed using zscore, RBF kernel and technical features. The first procedure was a comparison of the prediction which assumes a monthly trend of ‘up’ for all months considered during the out-of-sample period. Then we did the opposite by comparing the prediction results with down only during the out-of-sample period. The next procedure was to compare the results with a naïve prediction where if the previous month was up (or down), then the next month is predicted to be up (or down). The last procedure was to do the reverse of the previous procedure where if the previous month was up (or down), then the next month is predicted to be down (or up).

Procedure	Out-Of-Sample Accuracy %
Up Only	60.42%
Down Only	39.58%
Following Previous Month	52.55%
Opposite of Previous Month	47.22%
SVM Prediction	62.04%

Table 5.24 Results for comparing the classification accuracy during the full out-of-sample period

We can see from Table 5.24 that when assuming the index will go up every month, the overall accuracy was 60.4%. That was true for most of the time prior to 2000. After that period, the index direction wasn’t going up only but rather oscillated.

The next step was to compare the results during the first period when the market crashed. Figure 5.3 shows the index price during the first economic crisis we were looking at.

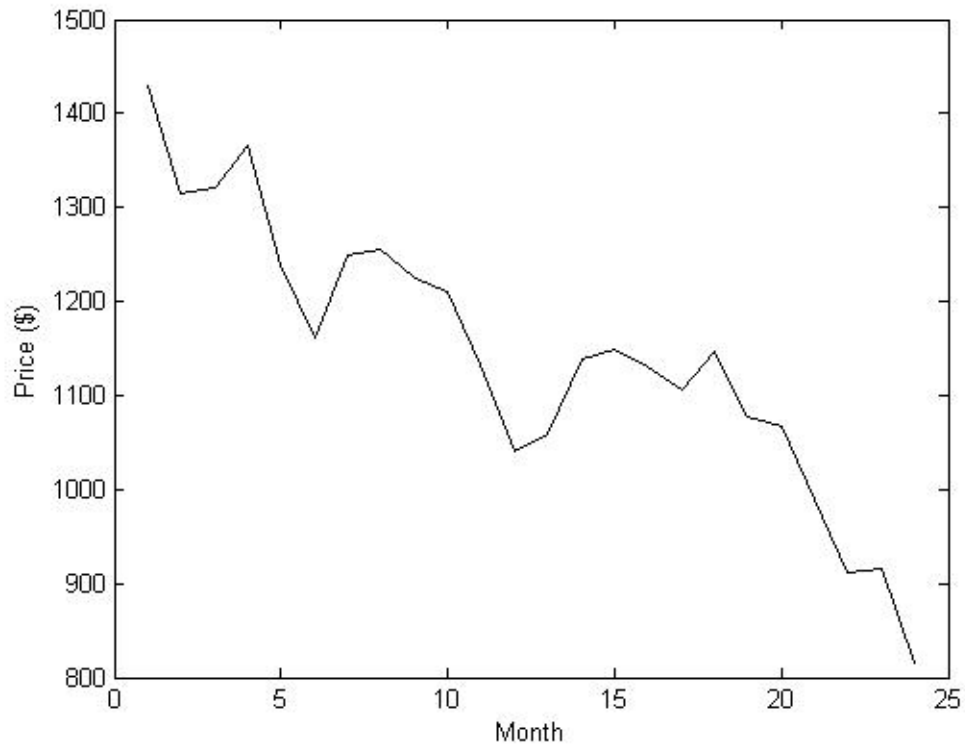


Figure 5.3 S&P 500 Index price over the first economic crisis (October 2000 – September 2002)

The results of the predictions are provided below:

Procedure	Out-Of-Sample Accuracy %
Up Only	41.67%
Down Only	58.33%
Following Previous Month	54.17%
Opposite of Previous Month	50.00%
SVM Prediction	50.00%

Table 5.25 Results for comparing the classification accuracy during the first economic crisis period

From Table 5.25, we can notice if we were to go up only from the beginning of out-of-sample, a big risk was avoided using SVM for prediction

during this economic crisis period if the strategy were to be followed by if the index price will only go up.

The last step was to see the performance during the last economic crisis beginning in late 2007. It was clear from Figure 5.4 that the index was going down during this period.

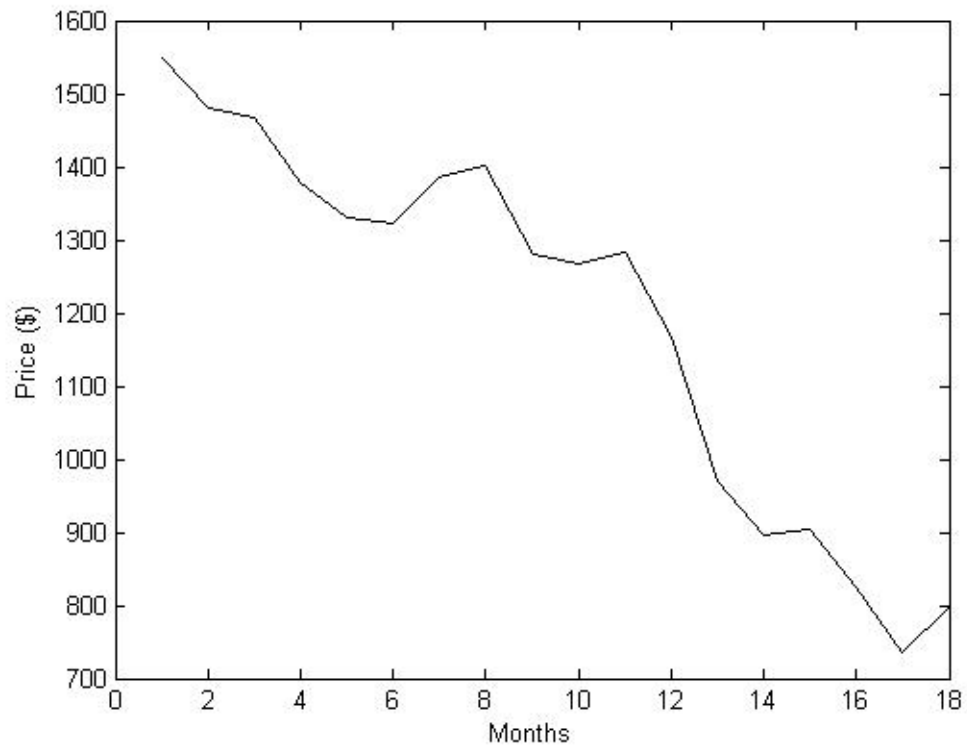


Figure 5.4 S&P 500 Index price during the last economic crisis (October 2007 – July 2009)

Procedure	Out-Of-Sample Accuracy %
Up Only	33.33%
Down Only	66.67%
Following Previous Month	61.11%
Opposite of Previous Month	44.44%
SVM Prediction	61.11%

Table 5.26 Results for comparing the classification accuracy during the last economic crisis period

We see from Table 5.26 that if we were to use the up only prediction, then the accuracy was 33.33%. SVM predicted 61.11% accurately, which as it happens was the same result when following the direction of previous month. This was another test to show the advantage of SVM over if we assumed the market will always go up.

If an investing strategy was implemented during the last two economic crisis period assuming the market will always go up, it would have encountered huge losses. The SVM reduced the risk in the first economic crisis to 50% compared to 58.33% loss when assuming the market will always go up. In the second economic crisis, SVM gave 61.1% accuracy while an up only strategy only had 33.33% accuracy.

Chapter 6: Conclusion and Future Work

6.1 Conclusion

This work performed several prediction models using SVM as a classifying tool in attempt to predict the direction of the market's trend using S&P 500 into 'up' or 'down' months. The first model used 15 inputs for macroeconomic features and 17 for technical features, as inputs to the SVM classifier. Results showed the best accuracy of 56.48% using all macroeconomic features with zscore to normalize the data, 51.39% using normc, and 53.94% using normalize. Classification using technical features showed better results compared to macroeconomic. We were able to obtain the best classification accuracy using all technical features with zscore. With normalizing the data using zscore, we were able to get 59.26% classification accuracy, 49.77% using normc, and 53.94% using normalize.

Optimizing the RBF's parameters further and raised the out-of-sample accuracy from 59.26% to 62.04% using technical features and from 56.48% to 59.25% using macroeconomic features. However, the best result for macroeconomic data was achieved using only the inflation feature giving 60.42%.

Reducing the dimensionality of the input features using Rankfeatures was found to be better in terms of choosing the right features needed and the accuracy to which features to exclude based on the RBF kernel we tested. The

response for reducing the features was better for the macroeconomic data. The linear kernel performs better with fewer features used to classify when using Sequential Feature Selection. We were able to get 60% accuracy with only one feature using macroeconomic data.

From this work, we can conclude that classification using technical features result in better classification accuracy than using macroeconomic features. This may be fortuitous as obtaining the macroeconomic data is generally not an easy task. In contrast, technical features can be easily obtained and since all you need is the index's price to be able to derive the features used in this work.

This work was initially motivated by the result presented by Yuan in [24], where an out-of-sample classification accuracy of 86% was achieved. By the work done in the thesis we believe this rate of accuracy was achieved unfortunately by error. Specifically when labeling the correct target, Yuan's result is shifted by one month which results in looking into the future. When labeling the targets in the same way as [24], our classification rate achieved was also 86% when using technical features and close to 98% with macroeconomic features.

In the future, the parameters of the technical features can be optimized, perhaps using Genetic Algorithm to find better performing features. Also, SVM regression can be used to get a sense of what range the index can be expected to move during prediction period.

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Appendix: Matlab Code

```
% uses Charles Yuan's macro-economic features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

%Prompt User for kernel type
prompt = 'Please enter kernel type (linear/rbf/polynomial/quadratic):
';
kernel = input(prompt,'s');

% Labels in the Goyal spreadsheet
% 1 2 3 4 5 6 7 8 9 10 11 12 13 14
% 15 16 17 18
% yyyyymm Index D12 E12 b/m tbl AAA BAA lty ntis Rfree infl ltr corpr
svar csp CRSP_SPvw CRSP_SPvwx

% From Yuan paper
% 3 4 15 5 10 6 9 13
11 12
% EqPreDir %DP %DY %EP %DE %svar %bm ntis tbl lty ltr TMS
%dfy %dfr infl %MA(2,12) %P(t,t-12)

A = xlsread('PredictorData2011.xls'); % Amit Goyal's spreadsheet

DP = log(A(:,3)) - log(A(:,2)); % 1
DY = [nan;log(A(2:end,3)) - log(A(1:end-1,2))]; % 2
EP = log(A(:,4)) - log(A(:,2)); % 3
DE = log(A(:,3)) - log(A(:,4)); % 4
SVAR = A(:,15); % 5
BM = A(:,5); % 6
NTIS = A(:,10); % 7
TBL = A(:,6); % 8
LTY = A(:,9); % 9
LTR = A(:,13); % 10
TMS = LTY - TBL; % 11
DFY = A(:,8) - A(:,7); % 12
DFR = A(:,14) - LTR; % 13
INFL = A(:,12); % 14
DY12 = [nan(12,1); log(A(13:end,3)) - log(A(1:end-12,2))]; % 15

features=[DP,DY,EP,DE,SVAR,BM,NTIS,TBL,LTY,LTR,TMS,DFY,DFR,INFL,DY12];
```

```

%features = [EP BM TBL]; % 3, 6, 8 Yuan's best features

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);
stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

% In-sample period Normalization Method
    IS_Set = zscore(IS_Set);
%    IS_Set = normc(IS_Set);
%    IS_Set = normalize(IS_Set);

svmStruct = svmtrain(IS_Set, IS_CorrectTargets, 'autoscale', false, ...
                    'kernel_function', kernel, 'method', 'LS');

YY = svmclassify(svmStruct, IS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);
fprintf('inmodel SVM Accuracy: %6.2f %%\n', 100-errRate*100);

[r, ~] = size(IS_Set);
XX = [IS_Set; OOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

% choose the desired normalization method
    XXN = zscore(XX(1:r+n, :));
%    XXN = normc(XX(1:r+n, :));
%    XXN = normalize(XX(1:r+n, :));

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
                        'kernel_function', kernel, 'autoscale', false, 'method', 'LS');

    Results(n, 1) = svmclassify(svmStruct, XXN(end,:));
end

```

```

compare = (Results == OOS_CorrectTargets);
precision = (sum(compare)/length(compare)*100);

% end

%Display Results
fprintf('Out-of-Sample Accuracy: %6.2f %%\n', precision);
Gridsearch.m

% uses Charles Yuan's macro-economic features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

% Labels in the Goyal spreadsheet
% 1 2 3 4 5 6 7 8 9 10 11 12 13 14
15 16 17 18
% yyyyymm Index D12 E12 b/m tbl AAA BAA lty ntis Rfree infl ltr corpr
svar csp CRSP_SPvw CRSP_SPvwx

% From Yuan paper
% 3 4 15 5 10 6 9 13
11 12
% EqPreDir %DP %DY %EP %DE %svar %bm ntis tbl lty ltr TMS
%dfy %dfr infl %MA(2,12) %P(t,t-12)

A = xlsread('PredictorData2011.xls'); % Amit Goyal's spreadsheet

DP = log(A(:,3)) - log(A(:,2)); % 1
DY = [nan;log(A(2:end,3)) - log(A(1:end-1,2))]; % 2
EP = log(A(:,4)) - log(A(:,2)); % 3
DE = log(A(:,3)) - log(A(:,4)); % 4
SVAR = A(:,15); % 5
BM = A(:,5); % 6
NTIS = A(:,10); % 7
TBL = A(:,6); % 8
LTY = A(:,9); % 9
LTR = A(:,13); % 10
TMS = LTY - TBL; % 11
DFY = A(:,8) - A(:,7); % 12
DFR = A(:,14) - LTR; % 13
INFL = A(:,12); % 14
DY12 = [nan(12,1); log(A(13:end,3)) - log(A(1:end-12,2))]; % 15

features=[DP,DY,EP,DE,SVAR,BM,NTIS,TBL,LTY,LTR,TMS,DFY,DFR,INFL,DY12];
%features = [EP BM TBL]; % 3, 6, 8 Yuan's best features

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);

```

```

stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

IS_Set = zscore(IS_Set);

%%%%%%%%%%%%%%

X = (0.1:0.01:1.2);
Y = (0.1:0.01:1.2);

[p,q] = meshgrid(X,Y);
pairs = [p(:) q(:)];

tic
for j= 1:length(X)

j
CurrentSigma = X(j)
CurrentC = Y(j)

svmStruct = svmtrain(IS_Set, IS_CorrectTargets, 'autoscale', true, ...
'kernel_function', 'rbf', 'method', 'LS', 'RBF_Sigma', X(j), 'boxconstraint',
Y(j));

YY = svmclassify(svmStruct, IS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(IS_Set);
XX = [IS_Set; OOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    XXN = zscore(XX(1:r+n, :)); % choose the desired normalization
method

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...

```

```

'kernel_function','rbf','autoscale',false,'method','LS',...
    'RBF_Sigma',X(j),'boxconstraint',Y(j));

Results(n, 1) = svmclassify(svmStruct, XXN(end,:));

end

compare = (Results == OOS_CorrectTargets);
precision (j) = (sum(compare)/length(compare)*100);
CurrentPrecision = precision(end)

Pred(j,:) = Results;

end
toc

MaxPrecision = max(precision)

% Find the best pair
Best = find(precision >= max(precision));
Sigma = X(Best)
C = Y(Best)

figure(1)
% hold on
plot(X,precision)
ylabel('Accuracy');
% hold off

%Display Results
fprintf('Out-of-Sample Accuracy: %6.2f %%\n', precision);

```

```

MacroSequentialFeatureReduction.m

% uses Charles Yuan's macro-economic features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

%Prompt User for kernel type
prompt = 'Please enter kernel type (linear/rbf/polynomial/quadratic):
';
kernel = input(prompt,'s');

% Labels in the Goyal spreadsheet
% 1 2 3 4 5 6 7 8 9 10 11 12 13 14
15 16 17 18
% yyyymm Index D12 E12 b/m tbl AAA BAA lty ntis Rfree infl ltr corpr
svar csp CRSP_SPvw CRSP_SPvwx

% From Yuan paper
% 3 4 15 5 10 6 9 13
11 12
% EqPreDir %DP %DY %EP %DE %svar %bm ntis tbl lty ltr TMS
%dfy %dfr infl %MA(2,12) %P(t,t-12)

A = xlsread('PredictorData2011.xls'); % Amit Goyal's spreadsheet

DP = log(A(:,3)) - log(A(:,2)); % 1
DY = [nan;log(A(2:end,3)) - log(A(1:end-1,2))]; % 2
EP = log(A(:,4)) - log(A(:,2)); % 3
DE = log(A(:,3)) - log(A(:,4)); % 4
SVAR = A(:,15); % 5
BM = A(:,5); % 6
NTIS = A(:,10); % 7
TBL = A(:,6); % 8
LTY = A(:,9); % 9
LTR = A(:,13); % 10
TMS = LTY - TBL; % 11
DFY = A(:,8) - A(:,7); % 12
DFR = A(:,14) - LTR; % 13
INFL = A(:,12); % 14
DY12 = [nan(12,1); log(A(13:end,3)) - log(A(1:end-12,2))]; % 15

features=[DP,DY,EP,DE,SVAR,BM,NTIS,TBL,LTY,LTR,TMS,DFY,DFR,INFL,DY12];

```

```

%features = [EP BM TBL]; % 3, 6, 8 Yuan's best features

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);
stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

% In-sample period Normalization Method
    IS_Set = zscore(IS_Set);
%   IS_Set = normc(IS_Set);
%   IS_Set = normalize(IS_Set);

for k = 1:size(features,2)

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% uncomment this section and set NFeatures to limit to top features

maxdev = 0.001;
opt = statset('display','iter','TolFun',maxdev,'TolTypeFun','abs');

inmodel = sequentialfs(@cfun2,IS_Set,IS_CorrectTargets,...
    'cv','none',...
    'options',opt,...
    'NFeatures',k,...
    'direction','forward');

sfsIS_Set = IS_Set(:,inmodel);
sfsOOS_Set = OOS_Set(:,inmodel);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

svmStruct = svmtrain(sfsIS_Set, IS_CorrectTargets,'autoscale',false,...
    'kernel_function',kernel,'method','LS');

YY = svmclassify(svmStruct,sfsIS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(sfsIS_Set);
XX = [sfsIS_Set; sfsOOS_Set];

```

```

YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(sfsOOS_Set)

% choose the desired normalization method
    XXN = zscore(XX(1:r+n, :));
%     XXN = normc(XX(1:r+n, :));
%     XXN = normalize(XX(1:r+n, :));

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
'kernel_function',kernel, 'autoscale',false, 'method', 'LS');

    Results(n, 1) = svmclassify(svmStruct, XXN(end,:));
end

compare = (Results == OOS_CorrectTargets);
precision(k) = (sum(compare)/length(compare)*100);
CurrentPrecision = precision(end)

end

% # Features and precision
[(1:k)' precision']

```



```

Macrorankfeatures.m

% uses Charles Yuan's macro-economic features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

%Prompt User for kernel type
prompt = 'Please enter kernel type (linear/rbf/polynomial/quadratic):
';
kernel = input(prompt, 's');

% Labels in the Goyal spreadsheet
% 1 2 3 4 5 6 7 8 9 10 11 12 13 14
% 15 16 17 18
% yyyymm Index D12 E12 b/m tbl AAA BAA lty ntis Rfree infl ltr corpr
% svar csp CRSP_SPvw CRSP_SPvwx

% From Yuan paper
% 3 4 15 5 10 6 9 13
% 11 12
% EqPreDir %DP %DY %EP %DE %svar %bm ntis tbl lty ltr TMS
%dfy %dfr infl %MA(2,12) %P(t,t-12)

A = xlsread('PredictorData2011.xls'); % Amit Goyal's spreadsheet

DP = log(A(:,3)) - log(A(:,2)); % 1
DY = [nan;log(A(2:end,3)) - log(A(1:end-1,2))]; % 2
EP = log(A(:,4)) - log(A(:,2)); % 3
DE = log(A(:,3)) - log(A(:,4)); % 4
SVAR = A(:,15); % 5
BM = A(:,5); % 6
NTIS = A(:,10); % 7
TBL = A(:,6); % 8
LTY = A(:,9); % 9
LTR = A(:,13); % 10
TMS = LTY - TBL; % 11
DFY = A(:,8) - A(:,7); % 12
DFR = A(:,14) - LTR; % 13
INFL = A(:,12); % 14
DY12 = [nan(12,1); log(A(13:end,3)) - log(A(1:end-12,2))]; % 15

features=[DP,DY,EP,DE,SVAR,BM,NTIS,TBL,LTY,LTR,TMS,DFY,DFR,INFL,DY12];
%features = [EP BM TBL]; % 3, 6, 8 Yuan's best features

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);
stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

```

```

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% uncomment this section and set k to limit to top features

for k = 1:size(features,2)

[inmodel, Z] = rankfeatures(IS_Set', IS_CorrectTargets,
'NumberOfIndices', k);

sfsIS_Set = IS_Set(:,inmodel);
sfsOOS_Set = OOS_Set(:,inmodel);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% Normalization Method
    sfsIS_Set = zscore(sfsIS_Set);
%    sfsIS_Set = normc(sfsIS_Set);
%    sfsIS_Set = normalize(sfsIS_Set);

svmStruct = svmtrain(sfsIS_Set, IS_CorrectTargets, 'autoscale', false, ...
    'kernel_function', 'rbf', 'method', 'LS');

YY = svmclassify(svmStruct, sfsIS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(IS_Set);
XX = [sfsIS_Set; sfsOOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    XXN = zscore(XX(1:r+n, :)); % choose the desired normalization
method
%    XXN = normc(XX(1:r+n, :));
%    XXN = normalize(XX(1:r+n, :));

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
'kernel_function', 'rbf', 'autoscale', false, 'method', 'LS');

    Results(n, 1) = svmclassify(svmStruct, XXN(end,:));

```

```
end

compare = (Results == OOS_CorrectTargets);
precision(k) = (sum(compare)/length(compare)*100);
CurrentPrecision = precision(end)

end

% # of features and precision
[(1:k)' precision']
```

Technicalfeatures.m

```
% uses technical features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

%Prompt User for kernel type
prompt = 'Please enter kernel type (linear/rbf/polynomial/quadratic):
';
kernel = input(prompt,'s');

A = xlsread('PredictorData2011.xls');

stk.d = A(:,1);
stk.c = A(:,2);
stk.h = TA_MAX(stk.c,12);
stk.l = TA_MIN(stk.c,12);

% Calculate Technicals
I1 = TA_RSI(stk.c, 14);
[bBandsHigh, bBandsMid, bBandsLow] = TA_BBANDS(stk.c,9,2,2);
I2 = (stk.c - bBandsHigh)./bBandsHigh;
I3 = (stk.c - bBandsLow)./bBandsLow;
[stochK, stochD] = TA_STOCHF(stk.h,stk.l,stk.c, 14, 3);
I4 = stochK;
I5 = stochD;
I6 = [nan; diff(stochK)];
I7 = [nan; diff(stochD)];
I8 = [nan; diff(stk.c)./stk.c(1:end-1)];
I9 = (stk.c - stk.l)./(stk.h-stk.l);
PMAs = TA_SMA(stk.c,10);
PMAl = TA_SMA(stk.c,21);
I10 = [nan; diff(PMAs)./PMAs(1:end-1)];
I11 = [nan; diff(PMAl)./PMAl(1:end-1)];
I12 = [nan; (PMAs(2:end)-PMAl(1:end-1))./PMAl(1:end-1)];
I13 = (stk.c - PMAl)./PMAl;
I14 = (stk.c - TA_MIN(stk.c,5))./TA_MIN(stk.c,5);
I15 = (stk.c - TA_MAX(stk.c,5))./TA_MAX(stk.c,5);
MA = (((TA_SMA(A(:,2),2) - TA_SMA(A(:,2),12)) ./ TA_SMA(A(:,2),12))); %
16
MOM = [nan(12,1); (A(13:end,2) - A(1:end-12, 2)) ./ A(1:end-12, 2)]; %
17

features=[I1,I2,I3,I4,I5,I6,I7,I8,I9,I10,I11,I12,I13,I14,I15,MA,MOM];

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

% Choose the testing period
```

```

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 200010, 1);
% OOS_End = find(stk.d >= 200209, 1);

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 200710, 1);
% OOS_End = find(stk.d >= 200903, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

svmStruct = svmtrain(IS_Set, IS_CorrectTargets, 'autoscale', true, ...
                    'kernel_function', kernel, 'method', 'LS');

YY = svmclassify(svmStruct, IS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(IS_Set);
XX = [IS_Set; OOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    % choose the desired normalization method
    XXN = zscore(XX(1:r+n, :));
    % XXN = normc(XX(1:r+n, :));
    % XXN = normalize(XX(1:r+n, :));

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
                        'kernel_function', kernel, 'autoscale', false, 'method', 'LS');

    Results(n, 1) = svmclassify(svmStruct, XXN(end,:));
end

compare = (Results == OOS_CorrectTargets);
precision = (sum(compare)/length(compare)*100);
conMat = confusionmat(OOS_CorrectTargets, Results); % the confusion
matrix

%Display Results
fprintf('Out-of-Sample Accuracy: %6.2f %%\n', precision);

```

```

Technical_Gridsearch.m

% uses technical features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

% %Prompt User for kernel type
% prompt = 'Please enter kernel type: ';
% kernel = input(prompt,'s');

%Prompt User for Ticker Symbol
% prompt = 'Please enter number of features you want to reduce to: ';
% no_features = input(prompt);

A = xlsread('PredictorData2011.xls');

stk.d = A(:,1);
stk.c = A(:,2);
stk.h = TA_MAX(stk.c,12);
stk.l = TA_MIN(stk.c,12);

% Calculate Technicals
I1 = TA_RSI(stk.c, 14);
[bBandsHigh, bBandsMid, bBandsLow] = TA_BBANDS(stk.c,9,2,2);
I2 = (stk.c - bBandsHigh)./bBandsHigh;
I3 = (stk.c - bBandsLow)./bBandsLow;
[stochK, stochD] = TA_STOCHF(stk.h,stk.l,stk.c, 14, 3);
I4 = stochK;
I5 = stochD;
I6 = [nan; diff(stochK)];
I7 = [nan; diff(stochD)];
I8 = [nan; diff(stk.c)./stk.c(1:end-1)];
I9 = (stk.c - stk.l)./(stk.h-stk.l);
PMAs = TA_SMA(stk.c,10);
PMAl = TA_SMA(stk.c,21);
I10 = [nan; diff(PMAs)./PMAs(1:end-1)];
I11 = [nan; diff(PMAl)./PMAl(1:end-1)];
I12 = [nan; (PMAs(2:end)-PMAl(1:end-1))./PMAl(1:end-1)];
I13 = (stk.c - PMAl)./PMAl;
I14 = (stk.c - TA_MIN(stk.c,5))./TA_MIN(stk.c,5);
I15 = (stk.c - TA_MAX(stk.c,5))./TA_MAX(stk.c,5);
MA = (((TA_SMA(A(:,2),2) - TA_SMA(A(:,2),12)) ./ TA_SMA(A(:,2),12))); %
16
MOM = [nan(12,1); (A(13:end,2) - A(1:end-12, 2)) ./ A(1:end-12, 2)]; %
17

features=[I1,I2,I3,I4,I5,I6,I7,I8,I9,I10,I11,I12,I13,I14,I15,MA,MOM];

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);

```

```

stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

%%%%%%%%%%%%%%

X = (0.1:0.01:1.2);
Y = (0.1:0.01:1.2);

[p,q] = meshgrid(X,Y);
pairs = [p(:) q(:)];

tic
for j= 1:length(X)

j
CurrentSigma = X(j)
CurrentC = Y(j)

svmStruct = svmtrain(IS_Set, IS_CorrectTargets, 'autoscale', true, ...
'kernel_function', 'rbf', 'method', 'LS', 'RBF_Sigma', X(j), 'boxconstraint',
Y(j));

YY = svmclassify(svmStruct, IS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(IS_Set);
XX = [IS_Set; OOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    XXN = zscore(XX(1:r+n, :)); % choose the desired normalization
method

    svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
'kernel_function', 'rbf', 'autoscale', false, 'method', 'LS', ...

```

```

        'RBF_Sigma',X(j),'boxconstraint',Y(j));

    Results(n, 1) = svmclassify(svmStruct, XXN(end,:));

end

    compare = (Results == OOS_CorrectTargets);
    precision (j) = (sum(compare)/length(compare)*100);
    CurrentPrecision = precision(end)

    Pred(j,:) = Results;

end
toc

MaxPrecision = max(precision)

% Find the best pair
Best = find(precision >= max(precision));
Sigma = X(Best)
C = Y(Best)

figure(1)
% hold on
plot(X,precision)
ylabel('Accuracy');
% hold off

%Display Results
fprintf('Out-of-Sample Accuracy: %6.2f %%\n', precision);

```


TechnicalSequentialFeatureSelection.m

```
% uses technical features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

%Prompt User for kernel type
prompt = 'Please enter kernel type (linear/rbf/polynomial/quadratic):
';
kernel = input(prompt,'s');

A = xlsread('PredictorData2011.xls');

stk.d = A(:,1);
stk.c = A(:,2);
stk.h = TA_MAX(stk.c,12);
stk.l = TA_MIN(stk.c,12);

% Calculate Technicals
I1 = TA_RSI(stk.c, 14);
[bBandsHigh, bBandsMid, bBandsLow] = TA_BBANDS(stk.c,9,2,2);
I2 = (stk.c - bBandsHigh)./bBandsHigh;
I3 = (stk.c - bBandsLow)./bBandsLow;
[stochK, stochD] = TA_STOCHF(stk.h,stk.l,stk.c, 14, 3);
I4 = stochK;
I5 = stochD;
I6 = [nan; diff(stochK)];
I7 = [nan; diff(stochD)];
I8 = [nan; diff(stk.c)./stk.c(1:end-1)];
I9 = (stk.c - stk.l)./(stk.h-stk.l);
PMAs = TA_SMA(stk.c,10);
PMAl = TA_SMA(stk.c,21);
I10 = [nan; diff(PMAs)./PMAs(1:end-1)];
I11 = [nan; diff(PMAl)./PMAl(1:end-1)];
I12 = [nan; (PMAs(2:end)-PMAl(1:end-1))./PMAl(1:end-1)];
I13 = (stk.c - PMAl)./PMAl;
I14 = (stk.c - TA_MIN(stk.c,5))./TA_MIN(stk.c,5);
I15 = (stk.c - TA_MAX(stk.c,5))./TA_MAX(stk.c,5);
MA = (((TA_SMA(A(:,2),2)-TA_SMA(A(:,2),12))./ TA_SMA(A(:,2),12))); % 16
MOM = [nan(12,1);(A(13:end,2) - A(1:end-12, 2))./ A(1:end-12, 2)]; % 17

features=[I1,I2,I3,I4,I5,I6,I7,I8,I9,I10,I11,I12,I13,I14,I15,MA,MOM];

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);
```

```

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 200010, 1);
% OOS_End = find(stk.d >= 200209, 1);

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 200710, 1);
% OOS_End = find(stk.d >= 200903, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

for k = 1:size(features,2)

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% uncomment this section and set NFeatures to limit to top features

maxdev = 0.001;
opt = statset('display','iter','TolFun',maxdev,'TolTypeFun','abs');

inmodel = sequentialfs(@cfun,IS_Set,IS_CorrectTargets,...
                        'cv','none',...
                        'options',opt,...
                        'NFeatures',k,...
                        'direction','forward');

sfsIS_Set = IS_Set(:,inmodel);
sfsOOS_Set = OOS_Set(:,inmodel);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

svmStruct = svmtrain(sfsIS_Set, IS_CorrectTargets,'autoscale',false,...
                    'kernel_function',kernel,'method','LS');

YY = svmclassify(svmStruct,sfsIS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);

[r, ~] = size(sfsIS_Set);
XX = [sfsIS_Set; sfsOOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    % choose the desired normalization method
    XXN = zscore(XX(1:r+n, :));
%     XXN = normc(XX(1:r+n, :));
%     XXN = normalize(XX(1:r+n, :));

```

```

%      XXN = XX(1:r+n, :);

      svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
'kernel_function',kernel,'autoscale',false,'method','LS');

      Results(n, 1) = svmclassify(svmStruct, XXN(end,:));
end

compare = (Results == OOS_CorrectTargets);
precision(k) = (sum(compare)/length(compare)*100);
CurrentPrecision = precision(end)

end

% # Features and precision
[(1:k)' precision']

```

TechnicalRankfeatures.m

```
% uses technical features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

% %Prompt User for kernel type
% prompt = 'Please enter kernel type: ';
% kernel = input(prompt,'s');

%Prompt User for Ticker Symbol
% prompt = 'Please enter number of features you want to reduce to: ';
% no_features = input(prompt);

A = xlsread('PredictorData2011.xls');

stk.d = A(:,1);
stk.c = A(:,2);
stk.h = TA_MAX(stk.c,12);
stk.l = TA_MIN(stk.c,12);

% Calculate Technicals
I1 = TA_RSI(stk.c, 14);
[bBandsHigh, bBandsMid, bBandsLow] = TA_BBANDS(stk.c,9,2,2);
I2 = (stk.c - bBandsHigh)./bBandsHigh;
I3 = (stk.c - bBandsLow)./bBandsLow;
[stochK, stochD] = TA_STOCHF(stk.h,stk.l,stk.c, 14, 3);
I4 = stochK;
I5 = stochD;
I6 = [nan; diff(stochK)];
I7 = [nan; diff(stochD)];
I8 = [nan; diff(stk.c)./stk.c(1:end-1)];
I9 = (stk.c - stk.l)./(stk.h-stk.l);
PMAs = TA_SMA(stk.c,10);
PMAl = TA_SMA(stk.c,21);
I10 = [nan; diff(PMAs)./PMAs(1:end-1)];
I11 = [nan; diff(PMAl)./PMAl(1:end-1)];
I12 = [nan; (PMAs(2:end)-PMAl(1:end-1))./PMAl(1:end-1)];
I13 = (stk.c - PMAl)./PMAl;
I14 = (stk.c - TA_MIN(stk.c,5))./TA_MIN(stk.c,5);
I15 = (stk.c - TA_MAX(stk.c,5))./TA_MAX(stk.c,5);
MA = (((TA_SMA(A(:,2),2)-TA_SMA(A(:,2),12))./TA_SMA(A(:,2),12))); % 16
MOM = [nan(12,1);(A(13:end,2)- A(1:end-12, 2))./ A(1:end-12, 2)]; % 17

features=[I1,I2,I3,I4,I5,I6,I7,I8,I9,I10,I11,I12,I13,I14,I15,MA,MOM];

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

stk.d = A(:,1);
stk.c = A(:,2);
```

```

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 197501, 1);
OOS_End = find(stk.d >= 201012, 1);

IS_Set = features(IS_Start:OOS_Start-1,:);
IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);

OOS_Set = features(OOS_Start:OOS_End,:);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% uncomment this section and set k to limit to top features

for k = 1:size(features,2)

[inmodel, Z] = rankfeatures(IS_Set', IS_CorrectTargets,
'NumberOfIndices', k);

sfsIS_Set = IS_Set(:,inmodel);
sfsOOS_Set = OOS_Set(:,inmodel);
% % feats{inmodel}

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% Normalization Method
%     IS_Set = zscore(IS_Set);
%     IS_Set = normc(IS_Set);
%     IS_Set = normalize(IS_Set);

svmStruct = svmtrain(sfsIS_Set, IS_CorrectTargets, 'autoscale', true, ...
'kernel_function', 'rbf', 'method', 'LS');

YY = svmclassify(svmStruct, sfsIS_Set);
errRate = sum(YY ~= IS_CorrectTargets)/length(IS_CorrectTargets);
fprintf('inmodel SVM Accuracy: %6.2f %%\n', 100-errRate*100);

[r, ~] = size(IS_Set);
XX = [sfsIS_Set; sfsOOS_Set];
YY = [IS_CorrectTargets; OOS_CorrectTargets];

for n=1:length(OOS_Set)

    XXN = zscore(XX(1:r+n, :)); % choose the desired normalization
method
%     XXN = normc(XX(1:r+n, :));
%     XXN = normalize(XX(1:r+n, :));

```

```
svmStruct = svmtrain(XXN(1:end-1, :), YY(1:r+n-1), ...
'kernel_function','rbf','autoscale',false,'method','LS');

Results(n, 1) = svmclassify(svmStruct, XXN(end,:));
end

compare = (Results == OOS_CorrectTargets);
precision(k) = (sum(compare)/length(compare)*100);

end

% # of features and precision
[(1:k)' precision']
```

```

UporDownOnly.m

% uses technical features
clear
close all
addpath '..\misc'
addpath '..\ta-lib-0.0.3_ml2007a-mex_w64'

A = xlsread('PredictorData2011.xls');

stk.d = A(:,1);
stk.c = A(:,2);

CorrectTargets = [stk.c(2:end) >= stk.c(1:end-1); nan];

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 197501, 1);
% OOS_End = find(stk.d >= 201012, 1);

% IS_Start = find(stk.d >= 193806, 1);
% OOS_Start = find(stk.d >= 200010, 1);
% OOS_End = find(stk.d >= 200209, 1);

IS_Start = find(stk.d >= 193806, 1);
OOS_Start = find(stk.d >= 200710, 1);
OOS_End = find(stk.d >= 200903, 1);

IS_CorrectTargets = CorrectTargets(IS_Start:OOS_Start-1);
OOS_CorrectTargets = CorrectTargets(OOS_Start:OOS_End);

% Up only during OOS
UpResults = ones(length(OOS_CorrectTargets),1);
Upcompare = (UpResults == OOS_CorrectTargets);
Upprecision = (sum(Upcompare)/length(Upcompare)*100);

% Down only during OOS
DownResults = zeros(length(OOS_CorrectTargets),1);
Downcompare = (DownResults == OOS_CorrectTargets);
Downprecision = (sum(Downcompare)/length(Downcompare)*100);

% A naive prediction where if it was up (down) last month then the
% next prediction is up (down).

for n=2:length(OOS_CorrectTargets)
    if OOS_CorrectTargets(n-1) == 1;
        FollowResults(n, 1) = 1;
    elseif OOS_CorrectTargets(n-1) == 0;
        FollowResults(n, 1) = 0;
    end
end

Followcompare = (FollowResults == OOS_CorrectTargets);

```

```

Followprecision = (sum(Followcompare)/length(Followcompare)*100);

% The reverse of (iii) where if it was up (down) last month then the
% next prediction is down (up).

for n=2:length(OOS_CorrectTargets)
    if OOS_CorrectTargets(n-1) == 1;
        ReverseResults(n, 1) = 0;
    elseif OOS_CorrectTargets(n-1) == 0;
        ReverseResults(n, 1) = 1;
    end
end

Reversecompare = (ReverseResults == OOS_CorrectTargets);
Reverseprecision = (sum(Reversecompare)/length(Reversecompare)*100);

%Display Results
fprintf('Out-of-Sample Up Only Accuracy: %6.2f %%\n', Upprecision);
fprintf('Out-of-Sample Down Only Accuracy: %6.2f %%\n', Downprecision);
fprintf('Out-of-Sample Following Accuracy: %6.2f %%\n',
Followprecision);
fprintf('Out-of-Sample Reverse Accuracy: %6.2f %%\n',
Reverseprecision);

```


cfun.m

```
function errRate = cfun(X,Y)

% Change to the appropriate kernel

svmStruct = svmtrain(X, Y, 'kernel_function', 'linear');
YY = svmclassify(svmStruct,X);

errRate = sum(YY ~= Y)/length(Y); % mis-classification rate
```

Normalize.m

```
function data = normalize(d)
% the data is normalized so that max is 1, and min is 0
data = (d - repmat(min(d,[],1),size(d,1),1))*spdiags(1./(max(d,[],1)-
min(d,[],1))',0,size(d,2),size(d,2));
```