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AN ABSTRACT OF THE THESIS OF S. N. Muthukrishnan for the Master of Science in Mechanical Engineering presented December 21, 1990.

Title: Computer Aided Optimal Design of Helical Gears.

APPROVED BY THE MEMBERS OF THE THESIS COMMITTEE:

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Roy Koch			

A random search method for optimum design of a pair of helical gears has been developed. The sequence of optimization consists of two principal components. The first is the selection phase, where the output is the starting solution for the design variables - module, facewidth, helix angle and number of teeth on the pinion. The input for the selection phase includes the application environment, approximate center distance, minimum helix angle, desired values of gear ratio, pinion speed and the power to be transmitted. The limits on each of the design variables and the constraints are imposed interactively during the first phase. A standard tooth form is assumed for the design. Standards published by the American Gear Manufacturers Association are employed for the design process.

The second phase consists of the implementation of the optimization procedure to find the minimum weight. The method employs a random number as the search direction with the step size being altered based on the value of the constraints. A number of random directions are generated and a minimum in each of those directions are determined to form a set of feasible solutions. The optimum solution is then determined from the set of feasible solution. Graphs are presented during optimization to create a user interactive environment. The program generates a complete set of manufacturing data for the designed gear.

COMPUTER AIDED OPTIMAL DESIGN OF

HELICAL GEARS

by

S. N. MUTHUKRISHNAN

A thesis submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE in MECHANICAL ENGINEERING

Portland State University 1991

TO THE OFFICE OF GRADUATE STUDIES:

The members of the committee approve the thesis of

S. N. Muthukrishnan presented December 21, 1990.



APPROVED:



C. William Savery, Interim Vice Provost for Graduate Studies and Research

This work is dedicated to the doyens of Engineering, who by virtue of their sincere and meticulous effort have helped me reap the fruits of their hardwork.

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CONTENTS

ACKNO	WLEI	GEMENT	5	••	•	•	•	•••	•	•	•	•	•	•	•	•	•	•	•	•	•	iv
LIST	OF 1	ABLES	•	•••	•	•	•	•••	•	•	•	•	•	•	•	•	•	•	•	•	7	/i i
LIST	OF F	IGURES	•	••	•	•	•	••	•	•	•	•	•	•	•	•	•	•	•	•	vi	Lii
LIST	OF S	SYMBOLS	•	•••	•	•	•	••	•	•	•	•	•	•	•	•	•	•	•	•	•	ix
CHAPI	ſER																				PA	AGE
I	BACH	GROUND	•	•••	•	•	•		•	•	•	•	•	•	•	•	•	•	•	•	•	1
	1.1	Optim	iza	tio	n	•	•		•	•	•	•	•	•	•	•	•	•	•	•	•	1
	1.2	Optim	iza	tio	n :	in :	Mec	cha	nic	cal	D)es	ig	'n	•	•	•	•	•	•	•	5
	1.3	Comput	ter	s i	n (Opt	ima	al	Des	sig	n	•	•	•	•	•	•	•	•	•	•	6
	1.4	Defin	iti	on	of	Pr	ob]	lem	f	or	Op	oti	mi	za	ti	or	1	•	•	•	•	7
	1.5	Optima	al I	Des	igı	n o	f(Gea	rs	•	•	•	•	•	•	•	•	•	•	•	•	9
	1.6	Object	tiv	e o	f	ſhi	s]	Pro	jea	ct	•	•	•	•	•	•	•	•	•	•	•	10
II	RANI	OM SEAL	RCH	AL	GOI	RIT	HM	FO	RC	OPT	IM	ΙIΖ	АТ	ΊΟ	N	•	•	•	•	•	•	12
	2.1	Numer	ica	l M	etł	nod	s i	in	Opt	im	iz	at	io	n	•	•	•	•	•	•	•	12
		(Opt	imi D	zat es:	zio ign	n i : /	in An	Mec Exa	cha amp	ni le	.ca	1	En	gi	.ne	er	ir.		•	•	14
	2.2	Termin	nol	ogi	es	an	d 1	Not	ati	Lon	L	•	•	•	•	•	•	•	•	•	•	16
	2.3	Randor	n Se	ear	ch	Me	tho	ods	•		•	•	•	•	•	•	•	•	•	•	•	16
		1	Adaj Adaj Coml	oti oti oin	ve ve ato	Ra: St ori	ndo ep al	om Si He	Sea ze uri	rc Ra Ist	h nd ic	om	s et	ea ho	rc d	h	•	•	•	• •	• •	17 18 18
	2.4	The Mo	odi:	fie	d A	Ada	pti	ive	st	cep	S	iz	e	Ra	nd	on	ı S	lea	rc	h	•	19
		ŗ	ſhe ſhe	Ap Al	pro goi	oac it	h . hm	•••	•	•	•	•	•	•	•	•	•	•	•	•	•	19 20

			Mat Gra	hem: S phi	atic earc cal	cal ch In	Re ter	pre fac	ese .e	nta	ati	Lor •	n c	of •	Th •	ie •	Ra •	ind •	lon	1 • •	23 25
III	APPL	ICATIO	ON O	FR	ANDO	M S	SEA	RCI	ΙT	0 0	OPI	CIN	1AI	ן ר	DES	SIG	SN				
		OF HE	ELIC	AL	GEAF	รร	•	•	•	•	•	•	•	•	•	•	•	•	•	•	28
	3.1	Helic	al	Gea	r Op	oti	miz	at	lon	•	•	•	•	•	•	•	•	•	•	•	31
	3.2	Probl	em	of	Heli	lca	1 G	ear	c D	es	igr	ı	•	•	•	•	•	•	•	•	32
			Obj Con Des	ect str	ive aint Var	s ial	ble	• • S	•	• •	• •	• •	• •	• •	• •	• •	• •	• •	• •	• •	32 33 34
	3.3	Desig	n E	xam	ple	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	34
	3.4	Resul	t a.	nd	Disc	cus	sio	n.	•	•	•	•	•	•	•	•	•	•	•	•	35
IV	CONC	LUSION	ι.	••		•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	41
REFE	RENCE	s	•			•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	42
APPE	NDICE	S																			
А	HELI	CAL GE	EAR	DES	IGN	PR	OCE	DUI	RE	٠	•	•	•	•	•	•	•	•	•	•	45
В	RAND	OM SEA	RCH	I ME	THOI) A	S A	US	SER	C	ALI	LAI	3LE	: 1	PRC	GF	RAN	1	•	•	51
с	TABL	ES USE	DI	N H	ELIC	CAL	GE	AR	DE	SIC	GN	•	•	•	•	•	•	•			55

vi

LIST OF TABLES

TABLE	PAGE
I	Discrete values represented continuously 6
II	Solution for the non-linear minimization
	problem
III	Solution for the three bar truss problem 31
IV	Solution for the helical gear problem 37
v	Gear design details for manufacturing 40
VI	A broad classification of applications 56
VII	Application and suggested quality numbers for
	spur, helical, herringbone, bevel and hypoid
	gears, racks and worm gearing 57
VIII	Minimum number of teeth required on pinion for
	different helix and pressure angles 62
IX	Recommended hardness values for steel gears for
	different ranges of number of pinion teeth 62
х	Table of K-factor values for different
	applications 63
XI	Allowable contact stress values for different
	steel gears
XII	Allowable bending stress values for different
	steel gears
XIII	Application factors K_a and C_a for various
	applications

LIST OF FIGURES

FIGURE		PA	GE
1.	Optimum design process	•	3
2.	Conventional design process	•	3
3.	Design space	•	9
4.	A circular ring in tension	•	15
5.	Flowchart for the modified adaptive step size		
	random search technique	•	22
6.	Graphs presented to user as a part of		
	interactive optimization	•	26
7.	Three bar truss problem	•	29
8.	Graphs showing minimum of each design		
	variable with every random number	•	38
9.	Graphs showing behaviour of design variables		
	for a given random number	•	39

.

LIST OF SYMBOLS

A	Cross-sectional area in mm ²
A _i	Area of member i in mm ²
с	Operating center distance in mm
C _a	Application factor for pitting
C _c	Curvature factor at pitch line
C _f	Surface condition factor for pitting
Cg	Constraint set for the design process
C _m	Load distribution factor for pitting
C _p	Elastic coefficient in $[MPa]^{\frac{1}{2}}$
C _s	Size factor for pitting
C _v	Dynamic factor for pitting resistance
C _x	Contact height factor
C _y	Helical overlap factor
d	Operating pinion pitch diameter in mm
d,	Diameter of member i in mm
d _m	Mean diameter of ring in mm
d _p	Pitch diameter of pinion in mm
E	Modulus of Elasticity in MPa
E _p ,E _g	Modulus of elasticity of pinion and gear
	respectively
F	Value of function evaluated in each epoch
Ft	Force in N
f	Facewidth in mm

- f(X) Objective function
- g(X) Inequality constraint
- h(X) Equality constraint and
- I Geometry factor for pitting
- i Represents the number of design variable and takes values 1,2,3,...,n
- J Geometry factor for bending
- jitr Total number of epochs to be performed before an optimum solution is determined
- K, Application factor for bending
- K_b Rim thickness factor
- K_f Stress concentration factor
- K_m Load distribution factor for bending
- K Size factor for bending
- K, Dynamic factor for bending
- L Length of member i in mm
- m Metric module in mm
- m_{g} Gear ratio (greater than 1.0)
- m_n Normal module in mm
- N Number of teeth
- n Number of design variables in the equation
- n_n Speed of pinion in rpm
- P Power to be transmitted in kW
- Q Accuracy level number determined from application,
- R The direction of search a random number between
 - -1 and +1

S	Value of design variables in iteration [itr-1]
s _c	Contact stress in MPa
s _t	Bending stress in MPa
s _y	Permissible yield strength of member i in MPa
s'	Value of design variables in iteration [itr]
t	Diameter of wire in mm
v	Volume in mm ³
vt	Pitch line velocity at operating pitch diameter in
	m/s
W	Weight in kg
Wt	Transmitted load in N
x _i	Design variable
x _{li}	Lower bound design variable x _i
x _{ui}	Upper bound on design variable x _i
Y	Tooth form factor
Y _{max}	Maximum allowable deflection in the horizontal and
	vertical directions in mm
α_{itr}	The step size in the itr th iteration in a particular
	epoch
δ	The magnitude of change associated with step size
	in a particular iteration
δ _i	A small value
$\mu_{p}^{}$, $\mu_{g}^{}$	Poisson's ratio for pinion and gear respectively
ρ	Density of material in kg/mm ³
[σ]	Maximum allowable stress in MPa
σ	Calculated stress in MPa

xi

Ψ

CHAPTER I

BACKGROUND

1.1 OPTIMIZATION

Optimization is essentially a branch of applied mathematics dealing with techniques of achieving the "best" or the "most favorable" solution for a problem. Optimization techniques involve analytical, experimental and numerical tools [Arora,1]. All three techniques have been successfully incorporated in the design of structural elements. Of late, optimization techniques are being used in almost all fields of engineering, however aerospace engineering has been predominant in using optimization techniques.

With the concept of modern manufacturing techniques and the growing awareness about the limitation in the availability of raw materials and other resources, it has become essential for design engineers to work with design constraints for an efficient and cost effective system. Conventionally design processes have depended upon the "expertise" and intuition of the individual designer. Lack of ability to "search" for the optimum or the best design manually, led to the use of mathematical techniques. Optimization involves the use of a wide range of linear algebra and differential calculus techniques. Typically, an optimization method would involve the determination of the change in value of a function, step size and the direction of search, besides problem formulation and identification constraints and design variables which are discussed in detail later.

The earliest optimization techniques that were used for searching the best solution were of the partitioning or the sectioning method, where search was conducted for the best solution in small segments, in a given domain. For a given objective, the variables in the problem are manipulated mathematically, within a specific region. The classical method that uses this technique of partitioning, for solving one dimensional problem to achieve an optimum is the golden section search [Arora,1].

Overwhelming use of human element in the design process has led to dangerous and erroneous results in the synthesis of complex systems. The conventional design process involves the use of information gathered from one or more trial designs along with the intuitive knowledge and experience of the designer. In contrast, optimum design process involves not only the benefits that could be obtained from "intuitive knowledge and experience, but also the advantages of analysis, simulation and optimization" [Arora,1]. The above contrast between the conventional and optimum design process is true only when the complete sequence of design has been implemented on a computer. Figures 1 and 2 [Arora,1] highlight the sharp contrast between the conventional and optimum design





Figure 1. Optimum Design Process. Source: [Arora, 1]

Figure 2. Conventional Design Process. Source: [Arora,1] 3

processes.

Conventional and optimum design processes could be used at different stages of design. For example, consider the design of a transit system between areas of Portland metropolitan and the neighboring west side of Portland. To choose among a diesel powered railroad, an electric train or a magnetic levitation rail system is at the discretion of the system designer. However when it comes to the design of details such the dampers, the wheels, the brakes and other components, the designer does not choose them at his/her own discretion. A series of formulas to design and analyze the system are used for this purpose. The design usually starts with the selection of a few parameters, generally obtainable from previous records or experience. Following the design stage, the analysis stage would involve the use of several complex equations, usually non-linear of higher order to determine whether the design is acceptable or not. The use of optimization techniques in such instances would prove to be effective, as against any human activity to achieve the goal, especially due to the fact that it is more organized and methodical in achieving a solution.

In conventional design process no effort is made to minimize or maximize any of the functions of the system as it would be a very tedious computational process. Optimum design methods are likely to reduce lead times sizably due to the absence of human element in the process of maximizing or minimizing a function.

In order to achieve a prudent problem formulation, it is necessary to limit the domain of the problem to essential factors. For the example above, it would be a futile effort not to consider the effect of rain and hence rusting of several parts while it would also be unnecessary to try and develop a design that would best fit the transit system's schedule. Identification of the constraints and design variables has to be done carefully so that the system is completely defined.

1.2 OPTIMIZATION IN MECHANICAL DESIGN

As discussed earlier in this section, conventional methods can no longer be considered efficient approaches for design. Most of the currently available design procedures for design of mechanical components are based on discrete values and several of the designs have been computerized. Because of the discrete nature of design, it has been regarded that optimization cannot be used in design of mechanical components where continuously differentiable functions are uncommon. However, the advent of computer-aided-design (CAD) has helped in breaking the shell around optimization. Continuously differentiable functions are discretized into a database and assumed to be a sequence of numbers, arranged in the continuous order. For example the module of a gear is a set of discrete values. They can be stored in a database and ordered

5

from 1 to n with an increment of 1. Now the set of modules have been made continuous between 1 to n. As an example, Table I shows how this is done. By doing so, the variable module is assumed to be continuous and whenever the variable is incremented or decremented the corresponding discrete value is read from the database and is used in the optimization process.

TABLE I

Pseudo continuous	Discrete values
values for module	of module
1 2 3 4 5 6 7 8	1.25 1.50 1.75 2.00 2.25 2.50 3.00 3.50

DISCRETE VALUES REPRESENTED CONTINUOUSLY

1.3 COMPUTERS IN OPTIMAL DESIGN

Analysis of mechanical systems have become more detailed with the use of computers. This allows us to understand the behavior of systems to a higher level of detail, more efficiently. Moreover, iterative and repetitive procedures are much simplified with computers. Analysis of a system at each stage during its design process produces only few solutions after several complicated calculations. With the advent of optimization in the design process, the intensity of computation has increased many times. Hence it is judicious to conclude that optimal design could be more efficient with the use of computers. However this should not lead one to conclude that computers are intelligent, while they are still incapable of making any decision! Optimization involves great amount of looping and repetitive calculations.

1.4 DEFINITION OF PROBLEM FOR OPTIMIZATION

It is a generally accepted fact that the correct formulation of a problem takes roughly 50% of the total effort needed to solve the problem [Arora,1]. A typical problem in optimization has an objective function, constraints and design variables. The objective function might define efficiency, volume, weight, power or torque. This function, depending on the use, may be required to be maximized or minimized. The objective function is a mathematical formulation of the desired end result. It is also the criterion function that is used to select the best of the feasible solutions. For example the following are objective function in their own domain, - a pump manufacturer may want to maximize the efficiency of the pump, a machine manufacturer may want to minimize the cost of the equipment, or a truck manufacturer may want to maximize the power of the truck. The objective function is the easiest to formulate in the process of optimization. Identifying the objective is a decision that has to be taken by a responsible person. Once the objective is defined, the factors that could restrain one from achieving the objective - referred to as the constraints are formulated.

The constraints are difficult to identify, in contrast to the objective. Problems should neither be over-constrained nor under-constrained. For example in designing a ball bearing it would be superfluous to formulate a constraint for buckling load. Similarly the whole process of optimization would be a failure if the effect of radial load were to be neglected for its design. Constraints are of two kinds. The first is a limiting equation and (in mechanical design) most often is stress related, temperature related or size related [Arora,1]. The second type of constraints, side constraints, are those that impose bounds on the design variables. The constraints delineate feasible and infeasible solutions which may either be implicit or explicit. Constraints must be represented in terms of variables defined as design variables.

those variables A11 that influence the systems' characteristic during optimization are called design variables. They are also the parameters chosen to describe the design of a system. Once values are assigned to each of these variables, a system design is known and these design variables are required to lie within a range. It may not be necessarily true that all combinations of design variables would yield feasible solution. Figure 3 is a pictorial representation of the design space. The space indicated as feasible design

represents the space in which design is viable.



Figure 3. Design space.

1.5 OPTIMAL DESIGN OF GEARS

Among the class of transmission elements, gears form an important family. Their complex shape, geometry and characteristics, make their detailed design process tedious. Gears are selected based on the application. The dimensions of the gear have thus far been determined based on certain "rule of thumb" expressions. Traditionally, gears have been designed by "experts". A typical gear design would involve computation based on the final shape, form, strength, accuracy, noise and efficiency. To avoid the complexity in calculations, large factors of safety are used which result in bulky gears. The necessity for compact, efficient and safe gears make it necessary for a designer to use optimization techniques.

1.6 OBJECTIVE OF THIS PROJECT

Gear design involves complex, non-linear equations. Usually gears are designed to withstand bending and contact stresses. Depending on the need, design may also include noise reduction, life determination and efficiency. Not much research has been done in the optimal design of machine elements except in the field of kinematics. The first paper on the optimal design of gears was published in 1984 by Carroll and Johnson [2, 3]. There has not been much work that has been reported since then.

The constraints in the process of gear design are nonlinear. Due to the complexity of these equations it is infeasible to implement a sequential linear programming technique or a gradient based method, as the true nonlinearity of the problem is lost. Lee and Freundstein [11, 12] and Schumer and Steiglitz [15] have shown that for problems that are highly non-linear and dimensionally large, random search methods are likely to yield better solution than any of the conventional algorithms.

In this project, a random search strategy is developed and used for the optimal design of helical gears. This work focuses on the capability of random search in producing "acceptably" good solution and at the same time maintaining the non-linearity of the problem. The strategy used in the random search algorithm is to generate as many feasible solutions as possible and to determine the best solution from

10

the set of feasible solutions. An attempt has been made to incorporate the state-of-art techniques in interactive optimization, which is a relatively new field of research. The project also includes the comparison of the random search with a successive quadratic programming (SQP) based algorithm.

CHAPTER II

RANDOM SEARCH ALGORITHM FOR OPTIMIZATION

Like most optimization techniques the random search is also an iterative algorithm. It differs from the rest in that it is not a deterministic numerical method, but an orderly search in random directions. Random search techniques may sometimes be too slow to reach an optimum if one exists. As against the complexity of the deterministic numerical methods like linear programming and gradient descent algorithms, random search is a fairly straightforward technique and is likely to give approximate solution faster than the conventional optimization methods for nonlinear programming problems. The other major difference between the conventional algorithms available for nonlinear problems and the random search is that the latter does not use a linearization strategy to solve the problem.

2.1 NUMERICAL METHODS IN OPTIMIZATION

Numerical optimization techniques offer a logical approach to design automation [Vanderplaats,18]. Numerical methods are widely used to solve nonlinear problems because the analytical methods turn out to be a cumbersome process, involving repeated calculation of the gradient, partial derivative and value of the function and constraint at every iteration. The major reasons why numerical methods are preferred over analytical methods [Arora,1] are,

- The number of design variables and constraints can be larger
- 2. The functions for design variables can be non-linear, and
- Cost and or constraint functions can be implicit in terms of design variables.

Several systematic numerical methods have been successfully programmed to solve optimization problems. A typical optimization problem is represented as shown below,

Minimize	f(X)			
Subject to	h(X)	=	0	and
	g(X)	≤	0	

- where $X = \{x_1, x_2, \dots, x_i\}$, and each x_i is bounded by an upper and lower limit,
 - f(X) objective function,
 - h(X) equality constraint and
 - g(X) inequality constraint

In general, a constrained optimization problem includes the determination of step size and the search direction. Most of the optimization techniques are based on linearization if the problem happens to be nonlinear. Linearization of problems could be interpreted as simplifying the model of the system to be optimized, for the purpose of easier calculation. However, to achieve a good solution it is essential that the problem be treated as defined. When highly non-linear problems, as in the case of gear design, are considered, it becomes a difficult task to perform deterministic numerical optimization. Random search technique is slower in computation than a linearized model. On the other hand, random search method is better than a nonlinear optimization algorithm as it would give a solution faster, and it will be a good approximation for use as a starting solution in the deterministic numerical methods. With such an attribute, random search technique is a good trade off between the linearization method and non-linear method, especially when the problem is of larger dimension and starting solution are difficult to identify. Random search algorithms are not too complex, however the critical point to be borne in mind in developing a random search strategy is to keep the computation clear of any possible incorrect and providing appropriate termination manipulation an criteria. A major advantage with random search methods is that, unlike the deterministic numerical methods they are not dependent on starting solution, in the sense that they would give a solution that would be close to the global optimum. This means that the solution obtained for every starting point will be deviant from one another by some value.

Optimization In Mechanical Engineering Design: An Example

A typical optimization problem in design is shown in figure 4. It is required to design a ring for minimum volume. The ring has a circular cross-section, and is subjected to a force F, equal in magnitude and opposite in direction. It is required to minimize the volume of the ring, subject to constraint of simple stress.

The objective function for the problem is,



Figure 4. A circular ring in tension.

The constraint is,

$$\sigma = \frac{F_t}{A} = [\sigma] \qquad \dots 2.2$$

where,

 $[\sigma]$ is the maximum allowable stress

 σ is the calculated stress

The design variables in this problem are, the wire diameter 't' and the mean radius d_m . Bounds on these design variables are,

d _m ,t	>	0 and	••••	2.3
d _m ∕t	<	8.0	• • • • •	2.4

2.2 TERMINOLOGIES AND NOTATION

The following terminologies are introduced for random search techniques.

Epoch : One complete iteration or search performed for a particular random number.

Iteration : Each time a step size is altered.

Step size : The magnitude by which the value of the variables are changed in every iteration.

Direction of: A random number generated between -1 and +1 search (equivalent to the slope of a straight line). Violation of : The magnitude by which the value of the constraint constraint is away from the permissible value.

2.3 RANDOM SEARCH METHODS

Most random search methods use a random number generated between -1 and +1 as the search direction. By doing so, and adopting a line search, a point can be moved in all 360°. Consider a problem in which f(X) has to be minimized and f(X)is a problem of Π dimensions. This can be considered as a problem in a hyperspace of Π dimensions, where,

 $x_{1i} < x_i < x_{ui}$

and

x, design variable

 \mathbf{x}_{i} lower bound design variable \mathbf{x}_{i}

 \mathbf{x}_{ui} upper bound on design variable \mathbf{x}_{i}

The simplest concept of random search in a hyperspace is

16

to generate a set of random numbers uniformly distributed 0 and 1 in either direction and compute between the corresponding values of design variables using a linear equation [Jacoby, Kowalick and Pizzo,9]. After performing a certain number of iterations using a random number, the search is limited to some neighborhood space of the most successful points in the previous iterations. By doing so the number of function calls are minimized and speed of achieving a solution is increased, but the amount of risk in over shooting the optimum exists due to the large step size. In order to avoid such a situation, a series of searches with different random numbers is conducted and a set of solutions called the set of feasible solutions is generated. The set includes the optimum solution obtained in each of the random directions. The best among the set of feasible solutions is likely to be the optimum for the problem.

Three of the commonly used random search techniques in solving kinematics problem, and their deficiencies for the present problem are briefly discussed below.

Adaptive Random Search

This method uses a certain "bias" factor from previous experience besides the random number and the step size. Starting with a known "bias" factor, subsequent "bias" factors are computed as a linear combination of the previous step size and "bias"[25]. Due to lack of any prior knowledge of best "bias" factors this method is not used for the present problem.

Adaptive Step Size Random Search

This method is an enhancement of the adaptive random search and was developed by Schumer and Steiglitz [15]. This method uses an "optimized" step size that is obtained as a "exploratory" searches result of conducted in random directions. Step sizes that seem to achieve the objective are used as optimized step sizes for the next iteration till a termination criterion is reached. Several such searches are conducted and the best solution is obtained from a set of feasible solutions. This kind of random search is more systematic and by using sufficiently large iterations it is likely that an optimum would be found. The authors of this algorithm have shown for their problem that, random search methods is superior to conventional nonlinear problem solving methods. Although this algorithm has no major drawback, memory requirements are very high.

Combinatorial Heuristic Method

This method was primarily developed for problems in control engineering at AT&T laboratory. Lee and Freundstein [11] have successfully implemented this algorithm for their kinematic analysis problem [12]. This method uses the discrete nature of design variables and then carries out a random search over a resulting finite grid of possible solutions. Variables are selected one at a time and their feasibility is checked, which makes the technique a tedious process requiring large amounts of memory. Based on the adaptive step size random search and the combinatorial heuristic method a new algorithm called the modified adaptive step size random search has been developed and implemented by this author. The current algorithm differs from the rest, in that it uses the value of the gradient to determine the direction and magnitude of change of step size.

2.4 THE MODIFIED ADAPTIVE STEP SIZE RANDOM SEARCH

The Approach

For problems of larger dimension there are generally a substantial number of feasible solutions. However there is no set procedure or method that would help in achieving a unique solution. To avoid any discrepancy of optimum solution it is therefore best to find as many feasible solutions as possible, and each of those solutions would be a good approximation of the optimal solution. Determining a number of solutions means more time is required for determining the best solution. The random search algorithm that has been developed decreases the time required for reaching an optimal solution by using a step size that is adaptively varied by determining the value of the constraint. By stepping over or stepping less, violation of the constraint is determined and the step size is altered to minimize the violation. This method proves to be effective for problems of large dimension where it might be cumbersome to conventional optimization, using Hessian perform а and

gradient.

The Algorithm

The random search method that is developed does not use any calculation of derivatives. Therefore the method is strictly a non-deterministic numerical one. The basic approach is that, given a starting solution, a search is conducted in several random directions, in the feasible region. If the starting solution is outside the feasible region, the variable is brought into the feasible space by changing the step size and continuing the search. Depending on the random direction a minimum may be achieved. All such solutions form the set of feasible solutions. By performing a large number of searches, a global minima might be determined. The best of the set of feasible solutions is presented as the optimum.

The steps below indicate the sequence of the modified adaptive step size random search algorithm.

- Generate a set of starting solution for n variables. The starting solution S, need not be in the feasible region.
- 2. Generate a random search direction, R and obtain a new set of solution S' such that it minimizes the constraint violation. If the solution is not found and if the constraints are not violated increase the stepping size α_{itr} and continue to search until a solution is determined or a constraint C_g is violated. Upon violation of the constraint, the magnitude of stepping size is reduced by δ and the direction of stepping is reversed. This process

of determining an improved solution S' over S is continued until the constraints fall within acceptable values, as specified by the design requirements. The value of the objective function at the best S' (with minimum value of objective function) is determined as F. Generate a new random search direction and repeat step 2. Until a stopping criteria 'jitr' is reached, feasible solutions are generated in every possible direction. The best of the set of feasible solution is the optimum solution. This is determined by finding the minimum or the maximum of the value of the objective function during each "epoch", as necessary.

where,

3.

4.

n	number of design variables in the equation
S	value of design variables in iteration [itr-1]
s'	value of design variables in iteration [itr]
F	value of function evaluated in each epoch.
R	the direction of search - a random number between
	1 and +1
$\pmb{\alpha}_{itr}$	the step size in the itr th iteration in an epoch

C_a constraint set for the design process

- jitr total number of epochs to be performed before an optimum solution is determined
- δ the magnitude of change associated with step sizein a particular iteration

21


<u>Figure 5.</u> Flowchart for the Modified Adaptive Step Size Random Search Technique.

The set of feasible solutions is actually a set of minima achieved in each random search direction. Hence, as one can quess the solution is dependent on the random search direction each of and the number of searches conducted in the directions. Figure 5 shows the flow chart of the random search technique developed. Random search techniques do not require memory capacities due the large to absence of any deterministic numerical method, and thus do not impose a limitation on the number of constraints that can be used for the design process.

The critical factor in the use of a random search algorithm is the definition of the stopping criterion. The stopping criteria is usually the number of random directions generated and the number of searches conducted in each direction. If no optimum is found, the number of iterations to be performed to yield an optimum has to be increased. Or, if only very few optimum are found it is again necessary to increase the number of iterations to ensure that a global minimum is reached.

Mathematical Representation Of The Random Search

The random search is a line search in a given random direction. The random direction is given by R, the design variables are given as x_i and the step size is α_{itr} . To begin with, the design variables are checked against their bounds. If the variables are not within the bounds then one of the following steps is adopted.

Case(a)

If the design variable is less than the lower bound,

 $x_i = x_i + \alpha_{itr} R$, if R is positive,

else, $x_i = x_i - \alpha_{itr} R$, if R is negative.

Case(b)

If the design variable is greater than the upper bound,

 $x_i = x_i - \alpha_{itr} R$, if R is positive,

else, $x_i = x_i + \alpha_{i+r} R$, if R is negative.

All four variables need not necessarily undergo the above mentioned changes simultaneously.

Once the variables are within bounds the constraint is evaluated. Based on the value of constraint one of the following steps is adopted. δ is a value causing change in step sizes.

Case(a)

If the constraint is not violated and is lower than the permissible value,

 $\alpha_{itr+1} = \alpha_{itr} - \delta, \text{ if } R \text{ is positive}$ else, $\alpha_{itr+1} = \alpha_{itr} + \delta, \text{ if } R \text{ is negative.}$

Case(b)

If atleast one constraint is violated,

 $\alpha_{itr+1} = \alpha_{itr} + \delta, \text{ if } R \text{ is positive}$ else, $\alpha_{itr+1} = \alpha_{itr} - \delta, \text{ if } R \text{ is negative.}$

If constraint violation changes sign, the design variables are assigned the values from the previous iteration and the step size is halved, until the constraints are satisfied. The function values are calculated only when the constraints are satisfied, and is added to a set of feasible solutions. The complete process described above is repeated for different random numbers until either the termination criteria is satisfied or the process is interrupted by the designer. The optimal solution is that set of design variables for which the function has minimum value.

Graphical Interface

In order for the optimization to be effective it is necessary that the user or the designer continuously monitor the behavior of each of the design variables so that suitable variations like changing a design variable to a constant, or removing a constraint after certain iterations, can be accomplished during the optimization process. A graphical interface to optimization is still a field of active research.

In the present work, an interactive graphical interface has been provided to a limited extent. The user can monitor the design process, can interrupt the design process and change the input parameters or can interrupt the optimization to exit to get the results achieved until the optimization interrupted. The interface between the process was optimization process and the designer is a set of graphs plotted between the epoch number and the value of each design variable when the constraint violation is minimum during that epoch. Figure 6 shows the graphs that are presented to the user.



a part of interactive optimization. as Graphs presented to user Figure 6.

26

One of the major problems with random search methods is that they would minimize the problem fully, i.e., to an extent where design may not be practically possible. In order to help the designer change the value of a variable at a particular point i.e., to either make a variable constant or change its value, interactive optimization is essential. Although this level of implementation, where the user can stop the optimizing process or change the state of one or more of the variables, has not been achieved, some amount of this aspect of interactiveness has been incorporated in the algorithm.

The random search method is also available as a user callable program. Appendix B gives a brief listing of how to use this method by just defining the functions and constraints separately. There is no graphical interface to this module.

CHAPTER III

APPLICATION OF RANDOM SEARCH TO OPTIMAL DESIGN OF HELICAL GEARS

The random search algorithm has been tested on two different problems, before being implemented for the design of Helical gears. A generic constrained non-linear optimization problem was tested against known results and were found to be satisfactory. Eq 3.1 defines the objective function for the problem and eq 3.2, 3.3 are the constraints. The bounds on the variables are simple and are given in eq 3.4. Table II shows a comparison of the values of design variables obtained by the random search and those obtained by a gradient based algorithm, available in the IMSL library of optimization routines [24].

> Minimize $f(x) = (x_1 - 2)^2 + (x_2 - 1)^2$ 3.1 Subject to $g_1(x) = x_1 - 2x_2 + 1 = 0$ 3.2 $g_2(x) = -x_1^2/4 - x_2^2 + 1 \ge 0$ 3.3 -1E 06 < x_1 , x_2 < 1E 06 3.4

The random search technique was also tested for a threebar truss problem with the objective of achieving minimum weight. Figure 7 shows the structure and the associated parameters. Eq 3.5 gives the objective function and Eq. 3.6 to 3.8 are the constraints. The random search was implemented for two different sets of constraints - one, for two elements 1

and 3 with identical properties and the other for all elements

29

TABLE II

SOLUTION FOR THE NONLINEAR MINIMIZATION PROBLEM

		Gradient based Algorithm	Random search Algorithm	
Starting	Variable x1	2.00	2.00	
Solution	Variable x2	2.00	2.00	
	Variable x1	0.8229	0.8317	
Solution	Variable x2	0.9114	0.9201	
Value of Objective fn.		2.1700	2.0033	
Approximat	te time	40 seconds	8 minutes	

Specifications for the three bar truss problem

- Permissible stress for members is 80 MPa
- Area of member 1 and 3 are equal
- Modulus of Elasticity for 1,2 and 3 = 210 MPa
- Member 1,2 and 3 are of the same material
- Objective is to minimize the diameter of the members



Figure 7. Three bar truss problem.

having different properties. The result of the optimization are shown in Table III. The three bar problem could not be implemented with the gradient based technique as the starting solution could not be defined within the feasible region. The result for the three bar optimization using the random search method was obtained by a fellow Graduate Student for a class project [8]. The problem was defined as follows,

Objective: To minimize the volume of the three bar truss,

$$V = \Sigma$$
 Area_i L_i 3.5

Subject to,

Yield:

$$S_{yi} - \frac{f_i}{A_i} = \delta_i \qquad \dots \qquad 3.6$$

Deflection:

$$Y_{max} - U = \delta_2 \qquad \dots \qquad 3.7$$

and Buckling:

$$\frac{\pi^2 E y A_i^2}{L} + f_i = \delta_3 \qquad \dots \qquad 3.8$$

where,

i = 1 to 3 V = Volume in mm³ A_i = Area of member i in mm² L = Length of member i in mm d_i = Diameter of member i in mm S_y = Permissible yield strength of member i in MPa Y_{max} = Maximum allowable deflection in the horizontal and vertical directions in mm E = Modulus of Elasticity in MPa

 $\delta_i = a \text{ small value}$

The design variable in the problem is the diameters of the members in the truss.

TABLE III

SOLUTION FOR THE THREE BAR TRUSS PROBLEM

	Starting Solution	Final Solution		
Dia. of member 1	18.00 mm	4.05 mm		
Dia. of member 2	12.00 mm	4.05 mm		
Dia. of member 3	18.00 mm	4.05 mm		
Minimized volume in cubic mm. = 4678.3				

Several researchers have used the random search technique. particularly for solving problems in kinematics. The combinatorial heuristic random search was used by Lee and Freundstein [12] for the analysis of linkages. An approach, to design of gear boxes using a random search technique has been reported by Cleghorn, Fenton and Fu [4].

3.1 HELICAL GEAR OPTIMIZATION

The problem of optimal design of helical gears has been dealt with by only one group of researchers [Jog and Pande,10]. In their optimum design process, they had linearized their problem and implemented the optimization sequence using the simplex method. This method does a good job only as long as the constraints are linear. It would only produce an approximate solution, especially when the problem assumes larger dimensions and the number of constraints increase. Also the simplex method is starting solution dependent, and the initial design should itself lie within the feasible region. Vanderplaats [19] has reported the use of a nonlinear optimization strategy for the design of helical gears but no documentation is available for this work. Work on optimal design for spur gears has been reported by several researchers (Carroll and Johnson [2, 3] and Zarak [20]).

In the current project the objective is to reduce the weight of a pair of steel helical gears, subject to the constraints of bending and contact stresses. The standard gear form with 20° pressure angle is considered.

3.2 PROBLEM OF HELICAL GEAR DESIGN

Objective

The objective of the problem is to minimize the weight of a pair of helical gears. The volume of the gear is approximated to the volume of a cylinder with the pitch diameter as the outer diameter. The objective function is, $W = V \rho$ 3.9

and,

substituting for d_n with,

$$d_p = \frac{m_n N}{\cos \Psi} \qquad \dots \qquad 3.11$$

$$V = \frac{\pi \left(\frac{m_n N}{\cos \psi}\right)^2 f}{4} \qquad \dots \qquad 3.12$$

where,

W = Weight in kg
V = Volume in mm³

$$d_p$$
 = Pitch diameter of pinion in mm
f = Facewidth in mm
 m_n = Normal module in mm
N = Number of teeth on pinion
 Ψ = Helix angle in degrees
 ρ = Density of material in kg/mm³

<u>Constraints</u>

The contact stress and the bending stress are modelled as constraints for the problem, although as many constraints as necessary can be included in the problem.

<u>Contact Stress.</u> The contact stress due to loading is determined using the AGMA equation [AGMA,21]

$$S_{c} \leq C_{p} \sqrt{\frac{W_{t}C_{a}C_{s}C_{m}C_{f}}{C_{v}dfI}} \qquad \dots \qquad 3.13$$

using the AGMA equation [AGMA,21].

Appendix A details the steps required in the determination of the different factors used in the calculation of S_c and S_t .

Design Variables

The design variables in this problem are

- 1) module,
- 2) helix angle,
- 3) number of teeth on pinion and
- 4) facewidth.

The boundary conditions on these variables are determined based on the operating condition of the gear.

In order to accomplish the design process the inputs indicated in Appendix A are received from the designer.

3.3 DESIGN EXAMPLE

The random search algorithm was tested with a problem from Shigley and Mitchell [16]. The problem is presented below.

Transmitted Power = 74.6 kW Pinion Speed = 1120 rpm Gear Ratio = 4 Pressure Angle = 20° Permissible Bending Strength = 155 MPa Permissible Contact Strength = 530 MPa

The strength values are read from the tables and correction factors applied to it, to result in

values shown above.

Maximum permissible Helix angle = 35°

3.4 RESULT AND DISCUSSION

The results are tabulated in Table IV. The results show that all the four design variables have changed significantly. The graphs of all four variables seem to be similar, which is because of the uniform change in the value of the variables. The results are compared with those from a gradient based approach.

The gradient based approach failed to give a solution within 100 iterations. Even with increased number of iterations the solution was not as good as the one achieved with the random search. The values from random search and gradient based approach are shown in Table IV.

As a side note on the use of an effective interactive environment for interactive optimization, as could be seen in the example, from the graphs presented, the facewidth could be held at the constant value of about 34.3 mm after the 56th iteration and allowing the other variables to change. This way the process of optimization could be speeded up and could be efficient with the use of human intelligence. The graphs generated by the program, are shown in figure 8. Figure 9 shows the behavior of the design variables during each epoch. In this case the graphs are plotted for epoch number 7.

In the present problem, optimization is done with the

constraints of bending and contact. However any number of constraints could be added to the system. The program also generates a complete set of design details, required for the manufacturing process. These data are shown in Table V. TABLE IV

Solution using Gradient based Technique 16.00 36.3 21.1 0.329 38 Solution using Random Search Method 34.30 22.3 12.0 0.202 35 Starting Solution 4.00 14.00 26.5 25 Minimized Weight (in kg) Helix Angle (degrees) on pinion Facewidth (in mm) of teeth Variable Module (in mm) Design Number

SOLUTION FOR THE HELICAL GEAR PROBLEM



Graphs showing minimum of each design variable with every random number. Figure 8.

38



Graphs showing behaviour of design variables for a given random number. Figure 9.

39

TABLE V

GEAR DESIGN DETAILS FOR MANUFACTURING

Normal module		=	2.0 mm
Traverse module		=	2.1 mm
Normal pressure	angle	=	20 degrees
Traverse pressu	re angle	=	0.4 degrees
Helix angle		=	14.0 degrees
Number of teeth	(pinion)	=	26
Pitch diameter	(pinion)	=	51.0 mm
Base diameter	(pinion)	=	47.0 mm
Helix lead		=	12.7 mm
Major diameter	(pinion)	=	56.0 mm
Root diameter	(pinion)	=	47.0 mm
Addendum	(pinion)	=	2.5 mm
Facewidth		=	26.0 mm
Quality number		=	10
Volume	(pinion)	=	53054.46 mm ³
Weight	(pinion)	=	2.02e-001 kg
Material	(pinion)	=	Steel Through hardened
			tempered (AGMA Class 5)
Number of teeth	(gear)	=	102
Material (gear)		=	Steel Carburised & case
			hardened
Weight	(gear)	=	8.24e-001 kg

CHAPTER IV

CONCLUSION

This project was intended to show the use of optimization techniques for the design of machine elements. The focus of this project was on the use of non-linear constraints in optimization without linearizing them, which was achieved by using a robust random search algorithm. The helical gear design problem which has complex constraints has been satisfactorily optimized using the random search method. With increase in computational power it is hoped that faster and more accurate solutions could be achieved. The results of the random search method have been compared to the gradient based approach and the results are better for this problem.

Finally it is the objective of this work to set a trend in optimization, as it is a very vital component of design. A new dimension to optimization - user interactiveness, has been incorporated to a limited extent. A possible extension of this project will be to develop optimization strategies specifically for the domain of design of other machine like springs and fasteners and elements also for the optimization of structure and shape of machineries, with a better implementation of user interactiveness.

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APPENDIX A

HELICAL GEAR DESIGN PROCEDURE

APPENDIX A

HELICAL GEAR DESIGN PROCEDURE

The following parameters are required as input for the design process.

- 1) Power to be transmitted
- 2) Speed of pinion in rpm
- 3) Gear Ratio
- 4) Maximum Helix Angle
- 5) Permissible center distance and
- 6) Area of application of the gear pair.
- All the parameters are to be entered in the SI units.

The application of the gear is also received as input. A set of data representative of the areas is collected and is stored as a data file. Table VI shows the listing of this data.

The following process is used for selecting the upper and lower bound for each of the variables. These values and tables are extracted from the AGMA standards and other texts.

- 1. Select the AGMA number and the value of application factors, C_a and K_a using the area of application [Table VII].
- Based on the maximum helix angle select the minimum number of teeth on the pinion [Table VIII].

- 3. Using the AGMA number the maximum permissible module for the pair of gears is determined. Usually the highest module is 48.
- Based on the minimum number of teeth, select the minimum hardness of pinion [Table IX].
- 5. Select a value for 'K'-factor based on the application [Table X]. Using the same table, also select the hardness for the gear material.
- Based on hardness of pinion and gear, select a steel material. Also select the corresponding Upper and lower limits of contact and bending stresses [Table XI, XII].

This completes the selection phase, where the upper and lower bounds on each of the variables are determined. The next phase of design is optimization, where the constraints are to be satisfied.

The constraints are,

$$S_{c} = C_{p} \sqrt{\frac{W_{t}C_{a}C_{s}C_{m}C_{f}}{C_{v}dfI}}$$

$$S_t = \frac{W_t K_a K_s K_m K_b}{K_v f m J}$$

where,

$$d = \frac{2C}{m_g + 1}$$

and,

 S_c = contact stress in MPa S_t = bending stress in MPa C_p = elastic coefficient in [MPa]³

Wt	= transmitted load in N
Ca	<pre>= application factor for pitting</pre>
C _s	<pre>= size factor for pitting</pre>
C _m	= load distribution factor for pitting
C _f	= surface condition factor for pitting
C_v	= dynamic factor for pitting resistance
f	= net face width of narrowest member in mm
I	= geometry factor for pitting
d	= operating pinion pitch diameter in mm
С	= operating center distance in mm
m _g	= gear ratio (greater than 1.0)
K _a	= application factor for bending
ĸ	= rim thickness factor
K _s	= size factor for bending
ĸ	= load distribution factor for bending
ĸ	= dynamic factor for bending
J	= geometry factor for bending
m	= metric module in mm

and

$$I = \frac{C_c C_x C_{\psi}}{m_n}$$

where,

 C_c = curvature factor at pitch line C_x = contact height factor C_{ψ} = helical overlap

$$J = \frac{YC_{\psi}}{K_{f}m_{n}}$$

Y = tooth form factor

 K_f = stress concentration factor

The transmitted load is determined as,

$$W_t = \frac{1.91 \times 10^7 \times P}{n_p d}$$

where,

P = power to be transmitted in kW $n_p = speed of pinion in rpm$ The pitch line velocity is,

$$v_t = \frac{\pi n_p d}{60000}$$

where,

vt = pitch line velocity at operating pitch diameter in
 m/s

The dynamic factors $K_{\!_{V}}$ and $C_{\!_{V}}$ are determined using the equation given below

$$C_{v} = K_{v} = \left(\frac{A}{A + \sqrt{200 v_{t}}}\right)^{B}$$

where,

$$A = 50 + 56(1.0 - B)$$

and

$$B = \frac{(12 - Q_v)^{0.667}}{4}$$

 Q_v =accuracy level number determined from application, refer Table VII.

The application factors C_a and K_a are obtained during the selection process itself, depending on the application [Table XIII].

The elastic coefficient is calculated using the formula,

$$C_{p} = \sqrt{\frac{1.0}{\pi \left[\frac{(1.0 - \mu_{p}^{2})}{E_{p}} + \frac{(1.0 - \mu_{g}^{2})}{E_{g}}\right]}}$$

where,

 C_p = elastic coefficient in MPa³ μ_p, μ_g = Poisson's ratio for pinion and gear respectively E_p, E_g = Modulus of elasticity of pinion and gear respectively.

Since only steel pairs are considered, $Cp = 191 \text{ MPa}^{\frac{1}{2}}$. Surface condition factor is unknown and hence a value of 1 is assumed.

For further information see AGMA standards [21,22].

APPENDIX B

RANDOM SEARCH METHOD AS A USER CALLABLE PROGRAM

APPENDIX B

RANDOM SEARCH METHOD AS A USER CALLABLE PROGRAM

The Random Search method can be used as a user callable program. A listing of the non-linear problem discussed in Chapter 3, eq 3.1 through 3.4 are presented. The user has to define the variables global to the function. Any number of design variables may be used in the problem.

The Random search algorithm is coded in Microsoft C, version 6.00. All the information below will hold good for Microsoft C compilers.

For The Objective function

The objective function has to be stored as OBJECTIV.C objectiv(y,cfval)

```
float y[5],*cfval;
```

```
{
```

```
*cfval=(y[1]-2)*(y[1]-2)+(y[2]-1)*(y[2]-1);
```

return;

```
}
```

```
where,
```

objectiv is the calling name for objective function
y[5] are the variables representing the design

variables in the problem and

cfval is the value of the objective function.

```
<u>Note:</u> The use of '*' before cfval is essential in the C programming environment.
```

For The Constraints

```
The constraints should be stored as CONSTRNT.C
constrnt(y)
float y[5];
{
  cg[0]=y[1]-2*y[2]+1;
```

```
cg[1]=-(y[1]*y[1])/4-(y[2]*y[2])+1;
```

```
return;
```

```
}
```

```
where,
```

- constrnt is the calling name for the constraint set
- y[5] are the design variables and
- cg[0],cg[1] are the constraint equations.
- Note: The user can add any number of constraints to the problem. The number of constraints used in the problem can be accommodated by a user input to a query in the main program. The user may also wish to add design details here.

How to link and run ?

<u>Linking</u>

Once the functions are defined, they are compiled using the following format, preferably adhering to the upper and lower

case alphabets as shown below.

cl /c random.c

The program is then linked as,

link random /ST:4112

where, /ST:4112 sets the stack size to be used to 4112 bytes.

Input and Output

The user has to input the following information.

- 1) Number of design variables, 'n',
- 2) Starting solution for 'n' design variables,
- 3) Upper and lower bound for the design variables,
- 4) Number of iterations to be performed and
- 5) The number of constraints to be used.

The program would produce the final optimized value as the solution. The output contains the minimized function value and the corresponding design variables.

APPENDIX C

TABLES USED IN HELICAL GEAR DESIGN

APPENDIX C

TABLES USED IN HELICAL GEAR DESIGN

TABLE VI

A BROAD CLASSIFICATION OF APPLICATIONS

Aerospace	 Control and Instrumentation gears Engine and Transmission gears Accesories
Industrial and Machine Tool	 4) Transmission (powered) gears 5) Accesories 6) Precision indexing and positioning
	7) Vehicle gears (in transmission)
Turbine and Generator	8) Transmission gears 9) Accesories
Others	10) Agricultural accesories 11) Low precision machines 12) Low quality gears

TABLE VII

APPLICATION AND SUGGESTED QUALITY NUMBERS FOR SPUR, HELICAL, HERRINGBONE, BEVEL AND HYPOID GEARS, RACKS AND WORM GEARING

ApplicationNumbers'ApplicationNumbers'Aerospace7-11Cast gear3Aerospace7-11Cast gear3-6Control geating10-12Plant operation5-6Engine power10-13Air separator5-6Loading boist7-11Converoy emill5-6Aerospace10-13Ball mill5-7Engine power10-13Compeb mill5-6Loading boist7-11Converoy mill5-6Aericulture12-13Elevator5-6Small engines12-13Elevator5-6Bet harvester5-7Klin slurty agiator5-6Com picker5-7Verstead crane5-6Com picker5-7Puy, rod, and tube mills5-6Coton picker5-7Puy, rod, and tube mills5-6Field harvester5-7Roaty dyret5-6Field harvester5-7Roaty dyret5-6Potator digger5-7Roaty dyret5-6Automotive industry10-11Cabeving gum industry6-1Automotive industry10-11Cabeving gum industry6-3Bailing machine5-7Coater6-3Barding machine5-7Coater6-3Barding machine6-7Mixer, mill6-3Barding machine6-7Coater6-3Bard washer6-8Capper6-8Copping6-7Coater, milk7-9Bridge machines<		0 11		
ApplicationNumbersApplicationNumbersAccospaceCat gear3AccospaceCat gear5-6Control gearing10-12Plant operationEngine accessories10-13Ball mill5-6Engine accessories10-13Compete mill5-6Engine statistics7-11Conveyor mill5-6Propeller fathering10-13Elevator5-6Small engines12-13Elevator5-6Agriculture5-7Killa slury agriator5-6Baler3-7Filter5-6Beer barvester5-7Killa slury agriator5-6Combine5-7Pug, rod, and tube mills5-6Compicker5-7Pug, rod, and tube mills5-6Compicker5-7Pug, rod, and finish mill5-6Compicker5-7Ruwa finish mill5-6Compicker5-7Ruwa finish mill5-6Farm elevator3-7Rotary dryer5-6Aitr compressor10-11Chewing gum industryAutomotive idustry10-11Chewing gum industryBailing machine5-7Coater6-8Catigger6-7Mizer-kneader6-8Catigger6-7Glazer, finisher6-8Catigger6-7Glazer, finisher6-8Conter slizer6-8Tampering7-9Patienting6-7Glazer, finisher6-8Catigger6-8Tampering7-9 <t< th=""><th></th><th>Quality</th><th>1</th><th>Quality</th></t<>		Quality	1	Quality
Accustors7-11Cast gear3Actuators7-11Cast gear5-6Engine accessories10-13Air separator5-6Engine power10-13Ball mull3-7Engine power10-13Compeb mill5-6Laading boist7-11Conveyor mill5-6Small engines12-13Cooler5-6Small engines12-13Cooler5-6Baler3-7Kilin stury agitator5-6Baler3-7Kilin stury agitator5-6Baler3-7Kilin stury agitator5-6Baler3-7Puyerizer5-6Baler3-7Nilin stury agitator5-6Com picker5-7Puyerizer5-6Com picker3-7Puyerizer5-6Art compressor10-11Chewing gun industryAutomotive industry10-11Chewing gun industryAutomotive industry10-11Chewing gun industryAutomotive industry10-11Chewing gun industryBailing6-7Molder-collerAgitator6-8Presser, refinerAgitator6-8Presser, refinerAgitator6-8Presser, refinerAgitator6-8Computing and accountingBailing6-7Molder-collerBailing machine5-7Bailing machine5-7Bailing machine6-7Construction6-8Corping industry6-7Mixer, ster	Application	Numbers	Application	Numbers
Activators7-11Cut gear5-6Control gearing10-12Plant operation5-7Engine accessories10-13Ball mill5-7Engine accessories10-13Comped buill5-6Engine struting10-13Comped buill5-6Laading hoist7-11Conveyor mill5-6Propelier fathering10-13Elevator5-6Small engines12-13Elevator5-6Agriculture3-7Filter5-6Baler3-7Filter5-6Combine5-7Ville5-6Compicker5-7Overhead crane5-6Compicker5-7Pulverizer5-6Conton picker5-7Pulverizer5-6Farm elevator3-7Pulverizer5-6Farm elevator3-7Pulverizer5-6Alir compressor10-11Chewing gum industry5-6Alir compressor10-11Chewing gum industry5-6Adire onderssor10-11Chewing gum industry5-6Bailing machine5-7Giazer, finisher6-8Bailing industry6-7Goater6-8Bailing machines6-7Giazer, finisher6-8Bailing machines6-8Presser, refiner6-8Raging machine6-7Giazer, finisher6-8Brewing industry6-7Goater didustry5-7Brewing industry6-7Goater, finisher6-8Brewing indu	Aerospace		Cast gear	3
Control gearing10-12Plant operationEngine accessories10-13Air separator5-6Engine starting10-13Compeb mill5-7Engine starting10-13Conveyor mill5-6Izading boist7-11Cooler 5-6Small engines12-13Cooler 5-6Small engines12-13Cooler 5-6Baler3-7Filter5-6Baler3-7Filter5-6Bet harvester5-7Kin stury agitator5-6Conspicker5-7Pug, rod, and tube mills5-6Conspicker5-7Pug, rod, and tube mills5-6Field harvester5-7Raw and finish mill5-6Potator digget5-7Rotary dryer5-6Automovire industry10-11Cheving gum industry6-6Automovire industry10-11Cheving gum industry6-6Balling machine5-7Cooter6-8Baling industry6-7Mixer-kneader6-8Conspicker6-7Glazer, finisher6-8Balling machine5-7Cooter6-8Balling industry6-7Glazer, finisher6-8Balling industry6-7Glazer, finisher6-8Pareit washer6-8Presser, refiner6-8Cookers6-8Commercial meters7-9Balding industry6-7Glazer, finisher6-8Pareit washer6-8Presser, refiner6-8Cookers6-	Actuators	7-11	Cut gear	56
Engine accessories10-13Air separator5-6Engine power10-13Ball mill5-7Engine starting10-13Compeb mill5-6Laading hoist7-11Converor mill5-6Propelier fathering10-13Elevator5-6Small engines12-13Elevator5-6Agriculture5-7Killn5-6Baler3-7Filter5-6Baler5-7Killn5-6Borb harvester5-7Killn5-6Combine5-7Nilln5-6Compicker5-7Pug. cod, and tube mills5-6Compicker5-7Pug. cod, and tube mills5-6Farm elevator3-7Pulverizze5-6Farm elevator3-7Rotary dryer5-6Air compressor10-11Cheving gum industry5-6Air compressor10-11Cheving gum industry5-6Air compressor10-11Cheving gum industry5-6Builing machine5-7Gazer6-8Brewing industry10-11Cheving gum industry6-8Builing machine5-7Gazer, finisher6-8Bailing machines6-7Wrapper6-8Bailing machines6-8Tampering6-8Master verser6-7Gazer, finisher6-8Brewing industry6-7Gazer, finisher6-8Brewing industry6-7Wrappering6-7Washer6-8Gas	Control gearing	10-12	Plant operation	
Engine power Engine starting10–13 10–13Ball mill5–7 Compeb mill5–6 5–6Loading hoixt7–11 7–11Conveyor mill5–6Propeller feathering10–13 7–11Cooler5–6Small engines12–13 7–7Elerator5–6AgricultureFeeder5–6Baler3–7 7Kiln slury agitator5–6Compicker5–7Kiln slury agitator5–6Compicker5–7Neither state5–6Farm elevator3–7Pulyerizer5–6Farm elevator3–7Rotary dryer5–6Potator digger5–7Raw and finish mill5–6Potator digger5–7Rotary dryer5–6Potator digger5–7Rotary dryer5–6Bading machine5–7Surry agitator5–6Bording industry10–11Chewing gun industry4Automotive industry10–11Chewing gun industry4Bading machine5–7Coater6–8Bording industry6–7Wataper6–8Bareni washer6–8Presser, refiner6–8Agitator6–3Tampeting6–3Mast mush6–6GasTampeting5–7Pastenrizer6–3Tampeting6–3Bording industry6–7Wataper6–8Baren washer6–8Presser, refiner6–8Baren washer6–8Commercial meters7–9Dicade making machiner	Engine accessories	10-13	Air separator	56
Engine itaring Loading hoist10–13 7–11Compete mill5–6 5–6Propeller feathering Agriculture10–13 10–13Cooler5–6Small engines Agriculture12–13Elevator5–6Bater3–7 FilterFilter5–6Bater3–7 Compete mills5–6Bater3–7 ComplexerS–6Complexer5–7Kiln slurry agitator5–6Complexer5–7Pulyenizer5–6Complexer5–7Pulyenizer5–6Fred harvester3–7Ruw and finish mill5–6Pennt harvester3–7Rotary dryer5–6Potator digger5–7Slurry agitator5–6Air compressor10–11Cheving gun industry4Automotive industry10–11Cheving gun industry5–6Batiling machine5–7Slurry agitator5–6Batiling machine5–7Coater6–3Batiling machine5–7Coater6–3Batiling machine6–7Molder-coller6–3Capping6–7Molder-coller6–3Labeling6–7Glazer, finisher6–3Labeling machines6–3Coamercial mactery5–7Pateurizer6–3Molder-coller6–3Mast nubs6–3Molder-coller6–3Mast nubs6–3Gay working machinery5–7Pateurizer6–3Gay working machinery5–7Dicad-electric locomotive <td< td=""><td>Engine power</td><td>10-13</td><td>Ball mill</td><td>5-7</td></td<>	Engine power	10-13	Ball mill	5-7
Lading hold7-11Conveyor mill5-6Propeller feathering10-13Cooler5-6Small engines12-13Elerator5-6AgricultureFeeder5-6Baler3-7Kiln slury agitator5-6Combine5-7Kiln slury agitator5-6Combine5-7Novehead erane5-6Combine5-7Pug, rod, and tube mills5-6Farm elevator3-7Pug, rod, and tube mills5-6Farm elevator3-7Raw and finish mill5-6Peant harvester5-7Raw and finish mill5-6Pottor digger5-7Slurry agitator5-6Automotive industry10-11Cheving gum industry5-6Automotive industry10-11Cheving gum industry5-6Bailing machine5-7Coater6-8Bailing machine5-7Coater6-8Bailing machine5-7Chocolate industry6-8Labeling6-7Wrapper6-8Barewing industry6-8Tampering6-8Mastney sterilizer6-8Tampering6-8Barewing industry6-8Tampering6-8Mastney6-7Wrapper6-8Baref washer6-8Commercial maters7-9Pattering machines6-8Tampering6-3Conster6-8Gas7-9Barde washer6-6GasGas7-9Pattering machinery5-7<	Engine starting	10-13	Compeb mill	56
Propeller feathering 10–13 Cooler 5-6 Small engines 12–13 Elevator 5-6 Agriculture Feder 5-6 Baler 3–7 Filter 5-6 Beet harvester 5–7 Kill slurry agitator 5-6 Combine 5–7 Kill slurry agitator 5-6 Combine 5–7 Puig rod, and tube mills 5-6 Conton picker 5–7 Puig rod, and tube mills 5-6 Fram elevator 3–7 Puigrester 5–6 Potator digger 5–7 Row and finish mill 5–6 Air compressor 10–11 Cheving gun industry 6–6 Automotive industry 10–11 Cheving gun industry 6–8 Bailing machine 5–7 Nolder-roller 6–8 Bailing machine 5–7 Coater 6–8 Bailing machine 5–7 Coater 6–8 Bailing machine 5–7 Molder-roller 6–3 Bailing machine 6–7 Washer, sterilizer 6–3 Barrel washer 6–8 Presser, refiner 6–8 Barrel washer 6–8 Casy working machinery 5–7 Pasteurizer 6–3 Coater	Loading hoist	7-11	Conveyor mill	S6
Small engines12–13Elevator5–6Agriculture7–7Filter5–6Baler3–7Kiln5–6Combine5–7Kiln alury agitator5–6Combine5–7Nuterizer5–6Combine5–7Pug rod, and tube mills5–6Combine3–7Pulyerizer5–6Farm elevator3–7Pulyerizer5–6Peanut harvester3–7Raw and finish mill5–6Potator digger5–7Slurry agitator5–6Automotive industry10–11Cheving gum industry6–8Automotive industry10–11Cheving gum industry6–8Baling machine5–7Goater - deas6–8Botling industry6–7Wizer-kneader6–8Capping6–7Glazer, finisher6–8Filling6–7Glazer, finisher6–8Masher, sterilizer6–3Miker, mill6–6Washer, sterilizer6–4Miker, mill6–4Agitator6–8Tampering6–3Agitator6–8Contercial meters7–9Pasteurizer6–3Warpper6–3Covicers6–4GasTamperingPasteurizer5–6Adding machinery5–7Pasteurizer6–3Computing and accounting7–9Bridye machines5–7Parking7–9Dicade lectric locomotive8–6Computing and accounting7–9Dicading machine5–	Propeller feathering	10-13 -	Cooler	5-6
ArricultureFeeder:5-6Baler3-7Filter5-6Bater5-7Kiln5-6Combine5-7Kiln sturry agitator5-6Compicker5-7Pug. rod, and tube mills5-6Conton picker5-7Pug. rod, and tube mills5-6Farm elevator3-7Pulverizer5-6Peanut harvester3-7Raw and finish mill5-6Potator digger3-7Rotary dryer5-6Air compressor10-11Cheide grinder6-3Bailing machine5-7Coater6-3Botting industry10-11Cheide grinder6-3Bailing machine5-7Coater6-3Bailing machine5-7Chocolater industry6-3Barding industry6-7Wrapper6-3Iabeling6-7Chocolate industry6-3Barrel washer6-8Presser, refiner6-3Barrel washer6-8Presser, refiner6-3Barder washer6-8Carpering6-3Cookers6-8Carpering6-3Barder washer6-8Carpering6-3Cookers6-3Carmercial meters7-7Pasteurizer6-4GasTamperingPasteurizer6-5Commercial meters7-7Pasteurizer6-6GasCookersPasteurizer6-7Liquid, water, milk7-9Bridge machinery5-7Liquid, water, milk7-9 <td>Small engines</td> <td>12-13</td> <td>Elevator</td> <td>56</td>	Small engines	12-13	Elevator	56
Baler3-7Filter5-6Bet harvester5-7Kiln slurry agirator5-6Combine5-7Kiln slurry agirator5-6Compicker5-7Pug, rod, and tube mills5-6Farm clevator3-7Pulverizer5-6Field harvester5-7Raw and finish mill5-6Peanet harvester3-7Rotary dryer5-6Potator digger5-7Raw and finish mill5-6Automotive industry10-11Chicke grinder6-8Balting machine5-7Coater6-8Botting industry10-11Chicke grinder6-3Balting machine5-7Coater6-8Botting industry6-7Molder-coller6-8Batting industry6-7Wrapper6-8Hiling6-7Chocolate industry6-8Washer, netilizer6-7Glazer, finisher6-8Berwing industry6-8Tampering6-8Mixer, mill6-8Tampering6-8Hiling machines6-8Tampering6-7Agirator6-8Tampering7-9Patcing machines6-8Tampering7-9Bridge machines6-7Laveling machinery5-7Patcing machines6-8Tampering7-9Bridge machinery5-7Parting7-9Bridge machines6-8Tampering7-9Bridge machinery5-7Parting7-9Dicading machines <td< td=""><td>Agriculture</td><td></td><td>Feeder</td><td>56</td></td<>	Agriculture		Feeder	56
Beet harvester5-7Kiln5-6Combine5-7Kiln sturry agitator5-6Com picker5-7Overhead crane5-6Farm elevator3-7Pulverizer5-6Farm elevator3-7Pulverizer5-6Potator digger3-7Rotary dryer5-6Air compressor10-11Cheving gun industry5-6Air compressor10-11Cheving gun industry5-6Balling machine5-7Oater6-3Bottling industry6-7Wixer-kneader6-3Bottling industry6-7Wixer-kneader6-3Barrel washer6-7Ghozer, finisher6-3Barrel washer6-8Presser, refiner6-3Filling machines6-8Gazer, finisher6-3Barrel washer6-8Gazer, finisher6-3Filling machines6-8Gazer, finisher6-3Barrel washer6-8Gazer, finisher6-3Fidling machines6-8Gazer, finisher6-3Barrel washer6-8Gazer, finisher6-3Bride machines6-7Commercial meters7-9Beide machines6-7Commercial meters7-9Beide machines6-7Commercial meters7-9Beide machines6-7Commercial meters7-9Racking machinery5-7Parking machine, calculator7-9Beide machines6-7Commercial meters7-9Racking machines6-6	Baler	3-7	Filter	56
Combine5-7Kill slurry agitator5-6Corton picker5-7Overhead crane5-6Corton picker5-7Puy rod, and tube mills5-6Farm elevator3-7Ruw and finish mill5-6Feant harvester3-7Rotay dryer5-6Potator digger5-7Naray dryer5-6Automotive industry10-11Chewing gum industry5-6Automotive industry10-11Chewing gum industry5-6Bailing machine5-7Coater6-3Bottling industry6-7Mixer-kneader6-3Capping6-7Wrapper6-3Isabeling6-7Glazer, finisher6-3Bewing industry6-7Glazer, finisher6-3Baging machines6-8Presser, refiner6-3Bared washer6-8Presser, refiner6-3Gokers6-8Gas7-9Bidge machines5-7Commercial metersBerewing industry5-7Parking7-9Berewing industry6-3Tampering6-3Bared washer6-8Gas7-9Bidge machines5-7Commercial meters7-9Beidge machines5-7Commercial meters7-9Beidgeter machines5-7Commercial meters7-9Diesel-electric locomotive8-9Bookkeeping9-10Convervor5-6Adding machine, calculator7-9Diesel-electric locomotive8-9Bookkeepi	Beet harvester	5-7	Kiln	5-6
Com picker5-7Overhead crane5-6Conton picker5-7Pug, rod, and tube mills5-6Farm elevator3-7Pulverizer5-6Field harvester3-7Raw and finish mill5-6Potator digger5-7Slurry agitator5-6Air compressor10-11Chick grinder6-3Bailing machine5-7Coatter6-3Botting industry10-11Chick grinder6-3Botting industry6-7Wrapper6-3Capping6-7Wrapper6-3Labeling6-7Glazer, finither6-3Berwing industry6-7Glazer, finither6-3Barrel washer6-8Presser, refiner6-3Gokers6-3Tampering6-3Barrel washer6-8Gas7-9Barding machines6-3Gas7-9Barding machines6-3Gas7-9Beide machines5-7Commercial metters7-9Beide machines5-7Commercial metters7-9Beide machines5-7Commercial metters7-9Convervor5-6Adding machine, calculator7-9Diesel-electric locomotive8-9Bookkeeping9-10Convervor5-6Adding machine, calculator7-9Cat gear6-8Computing and accounting10-11Diesel-electric locomotive8-9Bookkeeping9-10Cat gear6-8Computing10-11 </td <td>Combine</td> <td>5-7</td> <td>Kiln slurry agirator</td> <td>5-6</td>	Combine	5-7	Kiln slurry agirator	5-6
Control picker5-7Pug. rod, and tube mills5-6Farm elevator3-7Puly crizt, and tube mills5-6Field harvester5-7Raw and finish mill5-6Peanut harvester3-7Rotary dryer5-6Potator digger5-7Slurry agitator5-6Automotive industry10-11Chewing gum industry6-8Automotive industry10-11Chewing gum industry6-8Bottling industry10-11Chewing gum industry6-8Bottling industry6-7Molder-roller6-8Bottling industry6-7Wrapper6-3Labeling6-7Chocolate industry6-3Washer, sterilizer6-7Glazer, finisher6-3Barrel washer6-8Presser, refiner6-8Barrel washer6-8Tampering6-3Filling machines6-8Commercial meters7-9Bridge machinery5-7Parking machinery5-7Pasteurizer6-8Commercial meters7-9Bridge machinery5-7Parking7-9Bridge machinery5-77ParkingQuary operation6-8Computing and accountingCarse gear3-7Computing and accountingQuary operation6-8Cash registerQuary operation6-8Computing and accountingCarse gear3-7Computing machine9-10Cats gear3-6Addressograph7Diest electric locomoti	Com nicker	5-7	Overhead crane	5-6
South picts3-7Pulyerize5-6Farm elevator3-7Raw and finish mill5-6Peanut harvester3-7Rotary dryer5-6Potator digger5-7Slurry agitator5-6Air compressor10-11Chewing gum industry6-3Automotive industry10-11Chicle grinder6-3Bottling industry6-7Molder-toller6-3Bottling industry6-7Molder-toller6-3Bottling industry6-7Glazer, finisher6-3Berwing industry6-7Glazer, finisher6-3Barrel washer6-8Presser, refiner6-3Cookers6-8Presser, refiner6-3Barrel washer6-3Charver, milk7-9Bridge machines6-3Gas7-9Bridge machines6-4Gas7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking9-10Converyor5-6Addressograph7Oravery or5-6Addressograph7-9Diesel-dectric locomotive8-9Bookkeeping9-10Cast gear3Comptometer6-8Cut gear6-8Coaputon7-9Diesel-dectric locomotive6-8CoaputonCast gear3Compto	Cotton nicker	5-7	Bug rod and tube mills	5-6
Field harvester5-7Raw and finish mill5-6Pennut harvester3-7Rotary dryer5-6Potator digger5-7Slurry agitator5-6Air compressor10-11Chewing gun industry4Automotive industry10-11Chewing gun industry6-8Bailing machine5-7Coater6-8Batting industry6-7Molder-roller6-3Capping6-7Molder-roller6-3Filling6-7Chocolate industry6-3Labeling6-7Glazer, finisher6-3Berwing industry6-3Molder6-4Masher, sterilizer6-3Mixer-kneader6-3Agitator6-3Molder6-3Cookers6-3Tampering6-3Filling machines6-3Tampering6-3Mash tubs6-8Cas7-9Patientizer6-8Cas7-9Patientizer6-8Gas7-9Beidge machinery5-7Liquid, water, milk7-9Patientizer6-6Gas7-9Beidge machinery5-7Computing and accountingmachinesQuary operationAccounting7-9Conveyor5-6Adding machine, calculator7-9Diedet-enaking machiner5-6Adding machine, calculator7-9Diedet-enaking ser5-6Adding machine, calculator7-9Diedet-enaking ser5-6Addiessograph7Quary op	Farm elevator	37	Pulverizer	56
New Law Law Law3-7Rotary dryer5-6Peanut harvester3-7Slurry agitator5-6Potator digger5-7Slurry agitator5-6Air compressor10-11Chewing gum industry6-8Bailing machine5-7Coater6-3Botting industry0-11Chiele ginder6-3Capping6-7Molder-coller6-3Capping6-7Wrapper6-3Labeling6-7Chocolate industry6-3Washer, sterilizer6-7Glazer, finisher6-3Barrel washer6-8Tampering6-3Gookers6-8Tampering6-3Filling machines6-8Capping6-3Agitator6-8Gas7-9Barrel washer6-8Gas7-9Pasteurizer6-3Commercial meters7Pasteurizer6-3Gas7-9Bridge machines5-7Commercial meters7Pasteurizer6-6Gas7-9Bridge machines5-7Computing and accounting7-9Converor5-6Adding machine, calculator7-9Caury operation6-8Cast register7Cast gear3Comptometer6-8Cut gear6-8Cast register7Cast gear3Comptometer6-8Cut gear6-8Cast processing7-9Electric locomotive8-9Bookkeeping9-10-11El	Field harvester	57	Raw and finish mill	
Portator digger5-7Notaly diper5-4Portator digger5-7Slurry agitator5-6Air compressor10-11Chewing gum industryAutomotive industry10-11Chicle grinder6-3Bailing machine5-7Coater6-3Bottling industryMixer-kneader6-3Capping6-7Molder-coller6-3Fulling6-7Chocolate industry6-3Labeling6-7Chocolate industry6-3Washer, sterilizer6-7Glazer, finisher6-3Barrel washer6-8Presser, refiner6-3Agitator6-8Presser, refiner6-3Barrel washer6-8Gay working machinery5-7Pasteurizer6-8Gas7-9Pasteurizer6-8Gas7-9Bridge machine6-8Gas7-9Bridge machines5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking9Diesel-elec	Descut harvester	3_7	Pomer deres	5-6
Potator alget3-7Safty agator3-8Air compressor10-11Cheving gum industryAutomotive industry10-11Chide grinderBailing machine5-7CoaterBailing machine5-7CoaterCapping6-7Molder-rollerCapping6-7Molder-rollerCapping6-7Chocolate industryWasher, sterilizer6-7Glazer, finisherMixer, mill6-8Glazer, finisherAgitator6-8Presser, refinerAgitator6-8TamperingAgitator6-8Cay working machinerySockers6-8Cay working machineryFilling machines6-8GasFilling machines6-8GasPasteurizer6-8GasRacking machinery5-7Parkenizer5-6Adding machines5-7Parkenizer5-6Adding machinery5-7Parkenizer5-6Adding machinery5-7Parking machinery5	Perma diates	57	Slumm agint an	5-6
Air compressor10-11Clewing gim industryAutomotive industry10-11Child grinder6-3Bailing machine5-7Coater6-3Capping6-7Mixer-kneader6-3Capping6-7Wrapper6-3Labeling6-7Chocolate industry6-3Washer, sterilizer6-7Glazer, finisher6-3Agitator6-8Presser, nill6-3Agitator6-8Presser, refiner6-3Agitator6-8Presser, refiner6-3Cookers6-8Tampering6-3Filling machines6-8Cay working machinery5-7Pasteurizer6-8Cas s7-9Bridge machines6-8Commercial meters7-9Bridge machines5-7Parking7-9Bridge machines5-7Parking7-9Bridge machinery5-7Parking7-9Diedeter machines5-7Commercial meters7-9Custer5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Cast gear3Computing machine9Cast gear3Typewriter6-8Cut gear6-8Data processing7-9Electric shovel5-6Backhoe6-8Cut gear6-8Costruction equipment9Electric shovel5-6Backhoe6-8Cut gear6-8Costruction equipment9 <t< td=""><td>Focator digger</td><td>10 11</td><td>Charries and industry</td><td>50</td></t<>	Focator digger	10 11	Charries and industry	50
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Botting industryHitter-kneader6-3Capping6-7Molder-coller6-3Filling6-7Wrapper6-3Labeling6-7Chocolate industry6-3Washer, sterilizer6-7Glazer, finisher6-3Agizator6-3Molder6-3Barrel washer6-8Presser, refiner6-3Cookers6-3Tampeting6-3Filling machines6-4Tampeting6-3Mash tubs6-3Cay working machinery5-7Pastentizer6-8Commercial meters7-9Bridk-making machinery5-7Pastentizer7-9Bridge machinery5-7Pastenting7-9Bridge machinery5-7Pastenting7-9Bridge machinery5-7Pastenting7-9Bridge machinery5-7Computing and accounting machines7-9Quarry operationAdding machine, calculator7-9Quarry operationCast gear3ComputingCast gear3Comptometer6-3Cast gear3Comptometer6-3Cast gear3Typewriter8Cut gear6-8Constructing machine9Lietzic shorel5-6Bata processing7-9Lietzic shorel6-8Constructing machine9Lietzic shorel6-8Constructing equipment8Cut gear6-8Constructing equipment8Cut gear6-8 <t< td=""><td>Balling machine</td><td>3/</td><td>Coater</td><td>6-8</td></t<>	Balling machine	3/	Coater	6-8
Capping6-7Molder-roller6-8Filling6-7Wrapper6-8Labeling6-7Chocolate industryWasher, sterilizer6-7Glazer, finisherAgitator6-8MolderAgitator6-8Presser, refinerBarrel washer6-8Presser, refinerCookers6-8Presser, refinerFilling machines6-8WrapperMash mbs6-8Casy working machineryFarterizer6-8Casy working machineryRacking machines6-8GasRacking machinery5-7Liquid, water, milkParteurizer6-8GasRacking machinery5-7Bridge machinery5-7Bridge machinery5-7Bridge machinery5-7Source start6-8Quarry operationAccounting, billingConveyor5-6Adding machine, calculator7-9Diesel-electric locomotive8-9Bockkeeping9-10Electric drag lineCash registerCast gear3Cut gear6-8Cut gear6-8Cut gear6-8Cut gear6-8Cut gear6-8Cut gear6-8Construction equipmentElectric locomotive crane6-8Construction equipmentElevator5-6Labeloo6-8Construction equipmentElevator6-8Construction equipment <td>Botting industry</td> <td><i>.</i> -</td> <td>Mixer-kneader</td> <td>6-8</td>	Botting industry	<i>.</i> -	Mixer-kneader	6-8
Hiling6-7Wrapper6-8Labeling6-7Chocolate industryWasher, sterilizer6-7Glazer, finisherBrewing industryMixer, mill6-3Agitator6-8MolderBarrel washer6-8Presser, refinerCookers6-8TamperingFilling machines6-8Cay working machinerySockers6-8Cay working machineryFilling machine6-8GasFilling machinery5-7Liquid, water, milkRacking machinery5-7Liquid, water, milkBridge machinery5-7ParkingBridge machinery5-7ParkingBridge machinery5-7ParkingCement industry5-7ParkingQuarry operationAccounting, billing9-10Conveyor5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Cast gear3Comptometer6-8Cut gear6-8Cast register7Cast gear3Comptometer6-8Cut gear6-8Construction equipment9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Cast gear3Typewriter8Cast gear6-8Construction equipmentElevator5-6Backhoe6-8	Capping	6-/	Molder-roller	6-8
Labeling6-7Chocolate industryWasher, sterilizer6-7Glazer, finisher6-8Brewing industryMixer, mill6-8Agitator6-8Molder6-8Barrel washer6-8Presser, refiner6-8Cookers6-8Tampering6-3Filling machines6-8Wrapper6-3Mash tubs6-8Gay working machinery5-7Pasteurizer6-8Gas7-9Bridk-making machine6-8Gas7-9Bridge machines5-7Parking7-9Bridge machines5-7Computing and accounting7-9Bridge machines5-7Computing and accounting7-9Cement industry5-7Parking9-10Conveyor5-6Adding machines7-9Quarry operationAddiressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Computing machine9Cut gear6-8Coata processing7-9Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Filling	6/	Wrapper	68
Washer, sterilizer6-7Giazer, inisher6-8Brewing industryMixer, mill6-8Agitator6-8Mixer, mill6-8Barrel washer6-8Presser, refiner6-8Cookers6-3Tampering6-8Filling machines6-3Cay working machinery5-7Pasteurizer6-8Gas7-9Racking machine6-8Gas7-9Bridge machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Computing and accounting machines5-7Quarry operation5-6Adding machine, calculator7-9Crusher5-6Adding machine, calculator7-9Diesel-electric locomotive8-9Bookkeeping9-10Cast gear3Comprometer6-8Cut gear6-8Construction equipment9-10Electric shovel9Dictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment9Electric shovel0Dictating machine9Cast gear3-6Construction equipment6-8Elevator5-6Backhoe6-8Cut gear6-8Construction equipment6-8Elevator5-6Backhoe6-8Componetve crane5-6Construction equipment	Labeling	6-7	Chocolate industry	
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Agitator6-3Molder6-8Barrel washer6-8Presser, refiner6-8Cookers6-8Tampering6-3Filling machines6-8Wrapper6-8Mash tubs6-8Clay working machinery5-7Pasteurizer6-8Commercial metersRacking machine6-8GasRacking machinery5-7Liquid, water, milkPasteurizer6-8GasRacking machinery5-7Bridge machines5-7Computing and accountingT-9Bridge machines5-7Quarry operationAccounting, billingQuarry operation5-6Conveyor5-6Cusher5-6Adding machine, calculator7-9Diesel-electric locomotive8-9Bookkeeping9-10Cast gear3Cut gear6-8Cut gear6-8Cut gear3Cut gear6-8Cut gear3Cut gear6-8Cut gear6-6Locomotive crane6-6Locomotive crane6-6	Brewing industry		Mixer, mill	68
Barrel washer6-8Presser, refiner6-8Cookers6-8Tampering6-8Filling machines6-8Wrapper6-8Mash tubs6-8Clay working machinery5-7Pasteunizer6-8Gas7-9Bridke machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking9-10Cement industryMachines5-6Adding machine, calculator7-9Quarry operationAccounting, billing9-10Conveyor5-6Addinessograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric shovel9Dictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment8Cut gear6-8Construction equipment6-8Elevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Agitator	68	Molder	6-8
Cookers6-8Tampering6-8Filling machines6-3Wrapper6-8Mash tubs6-3Clay working machinery5-7Pasteurizer6-8Gas7-9Brick-making machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Computing and accounting7-9Bridge machinery5-7Computing and accounting9-10Cement industry5-6Adding machine, calculator7-9Quarry operation5-6Adding machine, calculator7-9Conveyor5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCast register7Cast gear3Comptometer6-8Cut gear6-8Data processing7-9Electric shovel9Dictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment8Elevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Barrel washer	68	Presser, refiner	68
Filling machines6-8Wrapper6-8Mash tubs6-8Clay working machinery5-7Pasteurizer6-8Gas7-9Brick-making machinery5-7Liquid, water, milk7-9Brick-making machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking9-10Cement industrymachines7-9Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment8Elevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Cookers	68	Tampering	68
Mash tubs6-8Clay working machinery5-7Pasteurizer6-8Commercial metersRacking machine6-8GasBrick-making machinery5-7Liquid, water, milkParking5-7ParkingBridge machinery5-7Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machines5-7Computing and accounting machines9-10Conveyor5-6Conveyor5-6Crusher5-6Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash registerCut gear6-8Cut gear6-8Cut gear6-8Cut gear3Cut gear6-8Cut gear3Cut gear6-8Cut gear6-8Construction equipment9Elevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Filling machines	68	Wrapper	68
Pasteurizer6-8Commercial metersRacking machine6-8Gas7-9Brick-making machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Briquette machines5-7Computing and accounting7-9Cement industrymachines9-10Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovel3Typewriter8Cut gear6-8Construction equipment8Cut gear6-8Construction equipment8Licy at gear6-8Construction equipment6-8Locomotive crane5-6Backhoe6-8	Mash tubs	68	Clay working machinery	5—7
Racking machine6-8Gas7-9Bridk-making machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Computing and accounting7-9Bridge machines5-7Computing and accountingmachinesCement industrymachines7-9Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear6-8Computing10-11Electric shovelData processing7-9Cast gear3Typewriter8Cast gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Pasteurizer	6—8	Commercial meters	
Brick-making machinery5-7Liquid, water, milk7-9Bridge machinery5-7Parking7-9Bridge machinery5-7Parking7-9Briquette machines5-7Computing and accounting machines7-9Cement industrymachines9-10Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Converyor5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment8Elevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Racking machine	6—8	Gas .	7-9
Bridge machinery5-7Parking7-9Briquette machines5-7Computing and accounting machines7-9Cement industryMaccounting, billing9-10Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipment6-8Liceare5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Brick-making machinery	5—7	Liquid, water, milk	7–9
Briquette machines5-7Computing and accounting machinesCement industrymachines9-10Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Bridge machinery	5—7	Parking	7–9
Cement industrymachinesQuarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Briquette machines	5-7	Computing and accounting	
Quarry operationAccounting, billing9-10Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovel0Dictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Cement industry		machines	
Conveyor5-6Adding machine, calculator7-9Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElectric shovel3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Quarry operation		Accounting, billing	910
Crusher5-6Addressograph7Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric showelData processing7-9Electric showelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Backhoe6-8	Conveyor	56	Adding machine, calculator	7–9
Diesel-electric locomotive8-9Bookkeeping9-10Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric shovelData processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive crane5-6Cranes	Crusher	56	Addressograph	7
Electric drag lineCash register7Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranesCranes	Diesel-electric locomotive	8-9	Bookkeeping	910
Cast gear3Comptometer6-8Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranes10-11	Electric drag line		Cash register	7
Cut gear6-8Computing10-11Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranes6-8	Cast gear	3	Comptometer	68
Electric locomotive6-8Data processing7-9Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranesCranes	Cut gear	68	Computing	10-11
Electric shovelDictating machine9Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranesCranes	Electric locomotive	68	Data processing	7-9
Cast gear3Typewriter8Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCranes	Electric shovel		Dictating machine	9
Cut gear6-8Construction equipmentElevator5-6Backhoe6-8Locomotive craneCraines6-8	Cast gear	3	Typewriter	8
Elevator 5-6 Backhoe 6-8 Locomotive crane Cranes	Cut gear	6-8	Construction equipment	
Locomotive crane Cranes	Elevator	56	Backhoe	68
	Locomotive crane		Cranes	
APPLICATION AND SUGGESTED QUALITY NUMBERS FOR SPUR, HELICAL, HERRINGBONE, BEVEL AND HYPOID GEARS, RACKS AND WORM GEARING (continued)

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Application	Quality Numbers	Application	Numbers
Open gearing	3-6	Electronic instrument control	
Enclosed gearing	6—8	and guidance systems	
Ditch digger	3—8	Accelerometer	1012
Transmission	6—8	Airborne temperature recorder	12-13
Drag line	5-8	Aircraft instrument	12
Dumpster	68	Altimeter-stabilizer	9-11
Paver		Analog computer	10-12
Loader	3 -	Antenna assembly	7-9
Transmission	8	Antiaircraft detector	12
Mixer	3–5	Automatic pilot	9-11
Swing gear	3-5	Digital computer	10-12
Mixing bucket	3	Gun-data computer	12-13
Shaker	8	Gyro caging mechanism	10-12
Shovels	-	Gyroscope-computer	12-13
Open gearing	36	Pressure transducer	12-13
Enclosed gearing	6-8	Radar sonar tuper	10-12
Stationary mixer		Recorder, telemeter	10-12
Transmission	8	Servo system component	9_11
Drum gears	3-5	Sound detector	9
Stone crusher		Transmitter receiver	10-12
Tenemission	8	Finding	10-12
Converor	6	Discel semidiecel and internal	
Truck mixer	0	Diese, semidiese, and miterial	
Transfer case	٥	compasion engine	10 17
Trailster case	2 5		10-12
Drum gears	JJ	Supercharger	10-12
Ream haim	5.6	Tuning gearings	10-12
Contract	J-0 5-4	Franknission	S10
Load hoist	5	Milling mechine	6.8
Overhead	5	Minking machine	e 10
Shin	5-7	Separator	a-10
Careboar	5-/	Sweeper	. 4-0
Los food	6 9	Ploor min industry	7 0
Reg lett	6-0	Dicactier Casin desease	/-0
Portable and stationary	00	Grain deaner	/8
KOCK, OFE, COL	00	Grinder	/8
Dairy moustry	< 7	Hulling	/8
bottle washer	6 –/	Muung, scouring	/8
Fiomogenizer	7-7	Pousner	/8
Separator Deserved le des	/9	Separator	/8
	67	Foundry industry	5 (
Dishurshas	3-/	Conveyor) –0
Commental	c -	Elevator	3—0
Commercial Dissiliante in ductore	3-/	Ladie	3-0
Distillery industry	c -	Molding machine	3-0
Remin film	5-/	Overhead cranes	3 - 0
Contract miler)-/ / 7	Sand mixer	3-0 C
Conveyor, clevator	6-/	Sand sunger	3-6 5-6
Grain puiverizer	6-8	lumbling mill	ن –د
Mash tub	S-7	riome appliances	
Mixer	5-7	Blender	6-8
Teast tub	5-7	Mixer	7-9
Electric furnace		limer	8-10

Source: [AGMA 390.03, 23]

APPLICATION AND SUGGESTED QUALITY NUMBERS FOR SPUR, HELICAL, HERRINGBONE, BEVEL AND HYPOID GEARS, RACKS AND WORM GEARING (continued)

Application	Quality Numbers	Application	Quality Numbers•
Machine tool industry		Hoists, skips	78
Hand motion (other than indexing		Loader (underground)	5-8
and positioning)	6-9	Rock drill	5-6
Feed drives	8 and up	Rotary car dump	68
Speed drives	8 and up	Screen, rotary	7-8
Multiple spindel drives	8 and up	Screen, shaking	7-8
Power drives	• <u></u>	Sedimentation	5-6
0_800 FPM	6-8 -	Senarator	5-6
800-2000 FPM	8-10	Shaker	6-8
2000-4000 FPM	10-12	Shovel	3-8
Over 4000 FPM	12 and up	Triple gearing	S-7
Indexing and positioning	r	Washer	6-8
approximate positioning	6-10	Paper and pulp	
Accurate indexing and positioning	12 and up	Bag machines	6-8
Marine industry		Bleacher, decker	
Anchor hoist	6-8	Bor machines	6-8
Cargo hoist	7-8	Building namer	6-8
Converor	5-7	Calender	6-8
Davit gearing	5-7	Chipper	6-8
Flevator	6-7	Coaring	6-8
Small propulsion	• 1	Digester	V-V
Steering gear	10-12	Envelope machines	6-8
Winch	8	Food container	6.8
W LIKEL	يت	Glazing	6-8
Membroching		Grinder	v • v
Bending coll	5_7	Tor converse elevator	5_7
Denving for	6_8.	Mirer agitator	م م
Earre press	5-7	Paper machine	~~
Punch press	5_7	Auviliaer	2_9
Poil inte	5-7	Main drive	10-17
Mining and permantion	J =/	Brees couch deier colle	
Arientor		Save all	
Breaker	5-6	Slitting	10-17
Cardamp	5-6	Steam desen	6-9
Car mother	5-7	Vamiching	64
Centrifuent drier	78	Wallpaper machines	6-8
Clarifier	7_8	Paying inductor	•••
Classifier	7_8	Aggregate drier	5-7
Coal digger	6-10	Aggregate spreader	5-7
Concentrator	ۍ. ۲	Achalt miver	5-7
Continuous miner	6-7	Asphalt enreader	5-7
Outting machine	6-10	Concrete batch mixer	5-7
Converor	5-7	Photographic equipment	• ·
Drag line	• •	Aerial	10-12
Open gearing	36	Commercial	8-10
Enclosed gearing	6-8	Printing industry	
Drier	S-6	Press	
Drills	5-6	Book	9-11
Electric locomotive	68	Flat	9-11
Elevator	5-6	Magazine	9-11
Feeder	6-8	Newspaper	9-11
Flotation	5-6	Roll recis	6-7
	-	•	

APPLICATION AND SUGGESTED QUALITY NUMBERS FOR SPUR, HELICAL, HERRINGBONE, BEVEL AND HYPOID GEARS, RACKS AND WORM GEARING (continued)

	Quality		Quality
Application	Numbers	Application	Numbers
Pump industry		Under 800 ft/min	5-6
Liquid	1012	Over 800-1800 fr/min	67
Rotary	68	Over 1800 ft/min	8
Slush, duplex-triplex	68	Nail and spike machine	5–6
Vacuum	68	Piler	5—6
Quarry industry		Plate mill rack and pinion	56
Conveyor-elevator	6-7	Plate mill side guards	56
Crusher	5-7	Plate turnover	56
Rotary screen	78	Preheat furnace pusher	56
Shovel, electric-diesel	78	Processor	67
Radar and missile		Pusher rack and pinion	5-6
Antenna elevating	8-10	Rotary furnace	5-6
Data gear	1012	Shear depress table	5-6
Launch pad azimuth	8	Slab squeezer	5-6
Ring gear	9-12	Slab-squeezer rack and pinion	5-6
Rotating drive	10-12	Slitter, side trimmer	67
Railroads		Tension reel	67
Construction hoist	57	Tilt table, upcoiler	5-6
Wrecking crane	68	Transfer car	5-6
Rubber and plastics	• •	Wire drawing machine	6-7
Boot and shoe machines	68	Blast furnace, coke plant, open-hearth	• •
Drier, press	6-8	and soaking pits, miscellaneous	
Extruder, strainer	68	drives	
Mixer, mber	6-8	Bessemer tilt-car dump	5-6
Refiner, calender	5-7	Coke pusher, distributor	5-6
Rubber mill scrap cutter	5-7	Conveyor, door lift	5-6
Tire building	6-8	Electric-furnace tilt	5-6
Tire channer	5-7	Hot metal car tilt	5-6
Washer, Banhury mixer	5-7	Hot metal charger	5-6
Small nomer mole	5,	lib hoist, dolomite machine	5-6
Bench grinder	6-8		5-6
Drille same	7-9	Mixing hin, mixer filt	5-6
Hair dinner	7-9	Ore crusher, nig machine	5-6
Hedge dinner	7_9	· Pulverizer, quench car	5-6
Sander polisher	8-10	Shaker, stinter converor	5-6
Spraver	6	Stinter machine skip hoist	5-6
Space navigation	0-0	Slag crusher slag shovel	5-6
Sertant and star tracker	13 and up	Primary and scondary rolling mill	•••
Steel industry	10 mil up	drives	
Auxiliary and miscellaneous drives		Blooming and plate mill	5-6
Annealing furnace	5-6	Heavy-duty hot mill drives	56
Bending coll	5-6	Slabbing and strip mill	5-6
Blooming-mill manipulator	5-6	Hor mill drives	
Blooming-mill rack and pinion	5-6	Sendzimer-Stekel	7-8
Blooming-mill side guard	5-0	Tandem-temper-skin	67
Car haul	5-6	Cold mill drives	•
Coil conveyor	5-6	Bar, merchant, rail, rod	5-6
Edger drives	5-6	Stuctural, tube	5-6
Electrolytic line	6-7	Mill gearing	
Flange-machine ingot buggy	5-6	Billet mills	
Leveler	6-7	Free roughing	5-6
Magazine pusher	6-7	Tandem roughing	5-6

Source: [AGMA 390.03, 23]

APPLICATION AND SUGGESTED QUALITY NUMBERS FOR SPUR, HELICAL, HERRINGBONE, BEVEL AND HYPOID GEARS, RACKS AND WORM GEARING (continued)

	Quality		Quality
Application	Numbers [*]	Application	Number
Reversing	7-8	Cinder yard, hot top	5-6
Tandem	7-8	Coal and ore bridges	S—6
Temper	7-8	Electric furnace charger	S6
Foil	7-8	Hot metal, ladle	S6
Hot mills		Hot mill, ladle house	56
Blooming and slabbing mills	S6	Jib crane, motor room	S6
Continuous hot strip mills	S6	Mold yard, rod mill	` S —6
Free reversing roughing	5-6 -	- Ore unloader, stripper	S6
Tandem roughing (including		Overhead hoist	5-6
scalebreaker)	S6	Pickler building	S6
Finishing	6-7	Pig machine, sand house	56
Merchant mills		Portable hoist	S6
Roughing	6-7	Scale pit, shipping	S6
Intermediate	7-8	Scrap balers and shears	S6
Finishing	7_9	Scrap preparation	S6
Plate mills		Service shops	S6
Reversing roughing	S6	Skull cracker	S6
Unidirectional roughing	S6	Slab handling	S6
Unidirectional finishing	56	Precision gear drives	
Rod mills		Diesel-electric gearing	8-9
Roughing	6-7	Flying shear	9-10
Intermediate	7-8	Shear timing gears	9-10
Finishing	10-12	High-speed reels	8-9
High speed	12-14	Locomotive timing gears	9-10
Skelp mills		Pump gears	8-9
Roughing	6-7	Tube reduction gearing	8-9
Intermediate	7-8	Turbine	9-10
Finishing	7-9	Miscellaneous	
Structural and rail mills		Clocks	6
Heavy		Counters	7-9
Reversing rougher	56	Fishing reel	6
Finishing	56	Gages	8-10
Light		IBM card puncher, sorter	8
Roughing	5-6	Metering pumps	7-8
Finishing	5-6	Motion picture equipment	8
Overhead cranes		Popopri machine, commercial	6-7
Billet charger, cold mill	S6	Pumps	5-7
Bucket handling	56	Sewing machine	8
Car repair shop	56	Slicer	7-8
Cast house, coil storage	56	Vending machines	6-7
Charging machine	56		

Source: [AGMA 390.03, 23]

MINIMUM NUMBER OF TEETH REQUIRED ON PINION FOR DIFFERENT HELIX AND PRESSURE ANGLES

	Min. No. of teeth to avoid undercut					
Helix angle, deg	Normal pressure angle, ϕ_n					
	1415	20	221/2	25		
0 (spur gears)	32	17	14	12		
5	32	17	14	12		
10	31	17	. 14	12		
15	29	16	13	11		
20	27	15	12	10		
23	25	14	11	10		
25	24	13	11	9		
30	21	12	10	8		
35	18	: 10	8	7		
40	15	8	7	6		
45	12-	7	5	5		

Nore: Addendum 1/Pe; whole depth 2.25/Pe.

Source: [Dudley, 7]

TABLE IX

RECOMMENDED HARDNESS VALUES FOR STEEL GEARS FOR DIFFERENT RANGES OF NUMBER OF PINION TEETH

Range of No. of pinion teeth	Ratio ma	Diametral pitch P _d	Hardness
19-60 19-50 19-45	1-1.9 2-3.9 4-8	1-19,9	200–240 BHN
19-45 19-38 19-35	1-1.9 2-3.9 4-8	1-19.9	Rockwell C 33-38
19-30 17-26 15-24	1-1.9 2-3.9 4-8	1-19.9	Rockwell C 58-63

Source: [Dudley, 7]

TABLE X

TABLE OF K-FACTOR VALUES FOR DIFFERENT APPLICATIONS

	Minimum of stee	h hardness I gcars	. N		K fac	or	Unit l	oad
Application	Pinion	Gcar	cycl cs	Accuracy	N/mm ²	psi	N/mm ²	psi
Turbine driving a generator	225 HB	210 HB	1010	High precision	0.69	8	45	6,500
	335 HB	300 HB	1010	High precision	1.04	150	53	8,500
	59 HRC	58 HRC	10 ¹⁰	High precision	2.76	§	83	12,000
Internal combustion engine driving	225 HB	210 HB	10°	High precision	0.48	70	31	4,500
a compressor	335 HB 58 HRC	300 HB	10°	High precision High precision	0.76 2.07	300	38 55	5,500 8,000
	006 110	010 110	841		1 30	No.	3.0	2
General-purpose industrial drives,		210 MB		Medium high precision	00-1 1-10-6	82	20 8 4	
for both driving and driven units)	58 HRC	58 HRC	20	Medium high precision	5.52	88	69	10,000
Large industrial drives, spur	225 HB	210 HB	10	Medium precision	0.83	120	24	3,500
hoists, kilns, mills	335 HB	300 HB	10	Medium precision	1.24	180	31	4,500
(moderate shock in driven units)	58 HRC	58 HRC	108	Medium precision	1 3.45	500	41	6,000
Acrospace, helical (single pair)	60 HRC	60 HRC	109	High precision	5.86	850	117	17,000
Acrospace, spur (epicyclic)	60 HRC	60 HRC	10%	High precision	4.14	600	76	11,000
Vchicle transmission, helical	59 HRC	59 HRC	4×10^{7}	Medium high precision	6.20	006	124	18,000
Vchicle final drive, spur	59 HRC	59 HRC	4 × 10 ⁶	Medium high precision	8.96	1300	124	18,000
Small commercial	320 HB	Phenolic	4×10^{7}	Medium precision	0.34	50	-	I
(pitch-line speed less than 5 m/s)	320 HB	laminatc Nylon	10,	Medium precision	0.24	35	l	[
Small gadget	200 HB	Zinc	106	Medium precision	0.10	15	l	1
(pitch-line speed less than 2.5 m/s)	200 HB	alloy Brass or	106	Medium precision	0.10	15	ł	1
		aluminum						

Notes: I. The above indexes of tooth loading assume average conditions. With a special design and a favorable application, it may be possible to go higher. With an unfavorable application and/or a design that is not close to optimum, the indexes of tooth loading shown will be too high for good practice.

2. The table assumes that the controlling load must be carried for the pinion cycles shown.

Source: [Dudley, 7]

TABLE XI

		Minimum	Allowat	ole Contact Stress Num Ib/in ² (MPa)	iber, sac
Material Designation	Heat Treatment	Hardness at Surface ¹	Grade 1 ²	Grade 2 ²	Grade 3 ²
Steel	Through	180 BHN	85 000	95 000	
	Hardened ³	& ·less	(590)	(660)	
		240 BHN	105 000	115 000	
			(720)	(790)	
		300 BHN	120 000	135 000	
			(830)	(930)	
		360 BHN	145 000	160 000	
			(1000)	(1100)	
		400 BHN	155 000	170 000	
			(1100)	(1200).	
	Flame ⁴ or	50 HRC	170 000	190 000	······································
	Induction		(1200)	(1300)	·
•	Hardened ⁴	54 HRC	175 000	195 000	
			(1200)	(1300)	
	Carburized	sée			
	& Case	Table 14-5	180 000	225 000	275 000
	Hardened ⁴	-	(1250)	(1560)	(1910)
AISI 4140	Nitrided ⁴	84.5 15N	155 000	180 000	
			(1100)	(1250)	
AISI 4340	Nitrided ⁴	83.5 15N	150 000	175 000	
			(1050)	(1200)	
Nitralloy 135M	Nitrided ⁴	90.0 15N	170 000	195 000	
•			(1170)	(1350)	
Nitralloy N	Nitrided ⁴	90.0 15N	195 000	205 000	
			(1340)	(1410)	
2.5% Chrome	Nitrided ⁴	87.5 15N	155 000	172 000	
			(1100)	(11000)	
2.5% Chrome	Nitrided ⁴	90.0 15N	192 000	216 000	
			(1300)	(1500)	

ALLOWABLE CONTACT STRESS VALUES FOR DIFFERENT STEEL GEARS

Source: [AGMA 2001-B88, 21]

TABLE XII

ALLOWABLE BENDING STRESS VALUES FOR DIFFERENT STEEL GEARS

Material	Heat	Minimum Hardness at	Allowable Bending Stress Number, s _{at} lb/in ² (MPa)		
Designation	Treatment	Surface ¹	Grade 1 ²	Grade 2 ²	Grade 3 ²
Steel	Through	180 BHN	25 000	33 000	
	Hardened	& less	(170)	(230)	
		240 BHN	31 000	41 000	
			(210)	(280)	
	·	300 BHN	36 000	47 000	
			(250)	(325)	
		360 BHN	40 000	52 000	
			(280)	(360)	
		400 BHN	42 000	56 000	
		:	. (290)	(390)	
	Flame ³ or	see Table	45 000	55 000	
	Induction Hardened ³ with Type	14–10	(310)	(380)	
	A Pattern		aa a a a	00 000	
	Туре В		22 000	22 000	
	Pattern		(150)	(150)	
	Carburized ³	see Table	55 000	65 or 70 000 ⁵	75 000
	& Case Hardened	14–11	(380)	(450) (480)	(520)
AISI 4140	Nitrided ^{3,8}	84.5 15N	34 000 (230)	45 000 (310)	
AISI 4340	Nitrided ^{3,6}	83.5 15N	36 000 (250)	47 000 (325)	
Nitralloy 135M	Nitrided ^{3,8}	90.0 15N	38 000 (260)	48 000 (330)	
Nitralloy. N	Nitrided ^{3,8}	90.0 15N	40 000 (280)	50 000 (345)	
2.5% Chrome	Nitrided ^{3,6}	87.5- 90.0 15N	55 000 (380)	65 000 (450)	

Source: [AGMA 2001-B88, 21]

TABLE XIII

APPLICATION FACTORS K, AND C, FOR VARIOUS APPLICATIONS

	Prime mov	/61	
Turbine	Motor	Internal combustion engine	Driven equipment
1.1 1.3	1.1 1.3	1.3 1.7	Generators and exciters Base load or continuous Peak duty cycle
1.7 1.7 1.8 2.2	1.5 1.5 1.7 2.0	1.8 1.8 2.0 2.5	Compressors Centrifugal Axial Rotary lobe (radial, axial, screw, and so forth) Reciprocating
1.5 2.0 2.0 1.7 1.5 2.0	1.3 1.7 1.5 1.5 2.0	1.7 — 2.0 1.8 2.3	Pumps Centrifugal (all service except as listed below) Centrifugal—boiler feed High-speed centrifugal (over 3600 rpm) Centrifugal—water supply Rotary—axial flow—all types Reciprocating
1.7	1.5	1.8	Blowers Centrifugal
1.7 1.7 2.0	1.4 1.4 1.7	1.8 · 1.8 2.2	Fans Centrifugal Forced draft Induced draft
1.5 1.3	1.5 1.3 1.5		Paper industry Jordan or refiner Paper machine, line shaft Pulp beater
1.5 1.7 1.7	1.5 1.5 1.7	1.8 2.0 2.0	Sugar industry Cane knife Centrifugal Mill
-	1.75 1.75 1.75		Processing mills Autogenous, ball Pulverizers Cement mills
-	1.4 2.0 2.75		Metal rolling or drawing Rod mills Plate mills, roughing Hot blooming or slabbing

Notes: 1. The values given are illustrative. As more experience is gained, new application factors will be established in the gear trade.

The values given may vary in a multistage drive. Experience and study will often show that the first stage needs a different application factor than that needed for the last stage.

5. The power rating and the kind of gear arrangement affect the application factor. The values given here represent somewhat average situations. (Be wary of new gear designs of high power. The old experience on application factors may be wrong for the new situation.)