Spring 6-15-2018

Biomimetic Design and Construction of a Bipedal Walking Robot

Alexander Gabriel Steele
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Biomimetic Design and Construction of a Bipedal Walking Robot

by

Alexander Gabriel Steele

A thesis submitted in partial fulfillment of the requirements for the degree of

Master of Science
in
Mechanical Engineering

Thesis Committee:
Alexander Hunt, Chair
David Turcic
Derek Tretheway

Portland State University
2018
Abstract

Human balance and locomotion control is highly complex and not well understood. To understand how the nervous system controls balance and locomotion works, we test how the body responds to controlled perturbations, the results are analyzed, and control models are developed. However, to recreate this system of control there is a need for a robot with human-like kinematics. Unfortunately, such a robotic testbed does not exist despite the numerous applications such a design would have in mobile robotics, healthcare, and prosthetics.

This thesis presents a robotic testbed model of human lower legs. By using MRI and CT scans, I designed joints that require lower force for actuation, are more wear resistant, and are less prone to catastrophic failure than a traditional revolute (or pinned) joints. The result of using this process is the design, construction, and performance analysis of a biologically inspired knee joint for use in bipedal robotics.

For the knee joint, the design copies the condylar surfaces of the distal end of the femur and utilizes the same crossed four-bar linkage design the human knee uses. The joint includes a changing center of rotation, a screw-home mechanism, and patella; these are characteristics of the knee that are desirable to copy for bipedal robotics. The design was calculated to have an average sliding to rolling ratio of 0.079, a maximum moment arm of 2.7 inches and a range of motion of 151 degrees. This should reduce joint wear and have kinematics similar to the human knee. I also designed and constructed novel, adjustably-damped hip and ankle joints that use braided pneumatic actuators. These joints
provide a wide range of motion and exhibit the same change in stiffness that human joints exhibit as flexion increases, increasing stability, adaptability, and controllability.

The theoretical behaviors of the joints make them desirable for use in mobile robotics and should provide a lightweight yet mechanically strong connection that is resistant to unexpected perturbations and catastrophic failure. The joints also bridge the gap between completely soft robotics and completely rigid robotics. These joints will give researchers the ability to test different control schemes and will help to determine how human balance is achieved. They will also lead to robots that are lighter and have lower power requirements while increasing the adaptability of the robot. When applying these design principles to joints used for prosthetics, we reduce the discomfort of the wearer and reduce the effort needed to move. Both of which are serious issues for individuals who need to wear a prosthetic device.
Dedication

To my Uncle, if I ever became half the man you were I would be proud. Also, to my cats, without whom I would have been able to finish this work in half the time and with far less cat hair everywhere.
Acknowledgements

The author would like to extend a heartfelt thanks to Derek Tretheway. Whom, without his understanding, none of this would have been possible. I cannot even imagine where I would be if he had not taken a chance on me; I will never forget it.

Thanks to Alexander Hunt, for giving me the freedom to create the things I imagine, for giving me a chance to work with and learn from him, and for the opportunity to build something amazing, despite my somewhat embarrassing and awkward first introduction.

Finally, to the rest of the lab and specifically Wade Hilts, may the horses of Nazareth always ride in your favor.
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Chapter 1

Introduction

When the public thinks about robotics, in particular bipedal humanoid robots, science fiction movies have taken the forefront. Given the state of technology, it may even seem that such advanced robots are only years away, if not, already here. However, in 2015 the DARPA Robotics Challenge destroyed those dreams by highlighting, at the time, the best and most well-funded robotic teams from around the world.

These (mostly) bipedal robots, on average, took almost an hour to do what humans could accomplish in just a few minutes, if the robots could accomplish it at all. Ironically, these robots performed better than DARPA expected. This public failure to match expectations set by the movie industry brought to light the reality of robotics in the current state.

The reality is that robots are not agile, cannot easily adapt to the environment they are placed in, and if they fell over, could not recover. The spurious idea of robots performing, as well as, or better than humans was now replaced with the reality; even the best robots were close to helpless.

Robots that easily adapt to their surroundings have numerous applications; in search and rescue, these robots would be able to save lives of people without risking more lives in the process. Furthermore, these robots are able to go into environments that
humans cannot, such as the Fukushima nuclear disaster, humanoid robots would be able to interact with the environment without exposing humans to the fatal radiation.

Robots need to be able to operate in an environment that was designed for human use. However, current mobile robots are designed like industrial machines and while this works for situations where extreme precision is needed, it does not allow them to adapt to changing environments in a way that would make them useful. For this reason, new designs for robotic joints that are more functional in a mobile platform are needed.

1.1 - Current robotic joint types and limitations

Currently, in robotics the most common type of joints used are revolute joints, also known as hinge joints or pin joints. There are several different examples of these joints, but they all have similar properties. This class of joints has a single degree of freedom, rotation about the pin. They are typically pinned center of the two joining rigid members. The single degree of freedom offered by pin joints makes them desirable for control purposes. Additionally, because of the simplicity of the joint, it is a low cost and easy to replace option.

However, due to the high shear stress that is applied to the joint through normal operations, the joints wear quickly [1]. Clamping forces applied to the pin, or preload, also causes joint fatigue, which leads to premature wearing as it introduces tensile forces, and promotes creep. The ratio between the diameter of the hole and the edge of the material to the edge of the hole has a direct effect on the wear and failure of the joint.
because the stress concentration or bearing force is higher at the hole. Furthermore, failure of the joint is typically catastrophic and causes serious damage because the joint is a single pin without added supports.

In recent years, biomimetic design has led to several different attempts to model and design a mechanical joint similar to the human knee. These designs have looked at different aspects of the knee and attempted to mimic them. Several of these designs include screw-home and patellar analogs [2–5].

These designs often utilize the same simplified 4-bar linkage design created when modeling the human knee. However, the designs that have been put forth are “floating designs,” or complex linkage designs that do not have contacting surfaces like those that the human knee utilizes. This predominately places load onto the pin connections and while the force profile over the entire range of motion differs, the pin joints have to carry the weight just as the solitary pin joint design first mentioned.

Lastly, Hobon et al. [6] modeled the benefits of using what they termed as a rolling knee joint (RK). This joint, (Fig. 1) consists of two rolling cylinders joined by a solid link, which has a pin joint at the center of either cylinder. This design eliminates a portion of the force placed on the pin joint by applying it through the contact point of the cylinders. The RK joint design reduces energy consumption during a walking gait when compared to a standard pin joint.
In the RK joint, the force from the weight of the robot is applied at a one-dimensional line across the cylinder, this force leads to premature wearing, and furthermore an impact load of sufficient force causes permanent deformation of the cylinders.

Energy is needed to keep the robot upright when standing because the design lacks an upright locking mechanism. When fully flexed, the weight of the robot is still applied to the pin joints used to attach the two cylinders.

In this work, I propose a set of joints that will act as a lightweight, robust, and compact replacement to pin joints for the hip, knee, and ankle joints. These proposed designs draw on inspiration from the hip, knee, and ankle joints of humans; they were designed using MRI scans of the equivalent human joint.
The joints use biological principles to imbue them with particular qualities that will offer them superior performance when compared to the standard robotic joint. Some of these qualities include locking in the upright position, much like the human knee as well as a changing moment arm that reduces the amount of force needed to create the same amount of torque using a pin joint.

In the next chapter, I will cover the objectives that I set out to accomplish in this thesis. These goals are what drove my research and properly explains the gap in knowledge that this thesis is filling.

Chapter 3 covers the anatomy and physiology of the joints in the lower half of the body. This chapter is an abridgment of what might be covered in biology, however understanding the main functions of the joints and how they are formed is needed for the subsequent chapters.

The fourth chapter discusses how to convert medical scans into 3D models, where to find medical scans, the capabilities of the MarkForged 3D printer that was used, as well as the design of the engineered joints. Each joint and, if applicable, the subordinate revisions to that joint are listed in order from oldest (version 1) to the newest.

Chapter 5 details the construction and theoretically predicted properties of the joints that were created which will be used later for testing, verification, and if needed, revision. As with Chapter 4, each major section covers a different joint, while each minor section covers the revisions to that joint.
The final chapter discusses the results and limitations of this work. It also recommends future work that could be taken at a later time to improve upon the foundation that this thesis creates.
Chapter 2

Objectives

The primary objective of this research is to develop a way to determine the in vivo kinematics of human joints from MRI and CT scans. Limited in vivo joint kinematic data exists because of the difficulty accurately tracking joint movement using external sensors. This data is important in the design of human inspired robotic joints because the human body is incredibly energy efficient and adaptable, however current robot designs are not.

The data will then be applied to the design of joints for a bipedal walking robot. Simulations will be done to determine both how energy efficient the designed joints are and how effective this new method is in determining human joint kinematics. 3D printed joints will then be constructed to verify the theoretical behavior and predicted kinematics.

This work will create a new methodology for designing mobile bipedal robotic joints that outperform the current designs.

This thesis breaks the designs into three chapter subsections, the hip joint, the knee joint, and the ankle joint. For the purposes of this thesis, the pelvis will be covered in the hip joint section and the foot will be included in the chapter covering the ankle joint and not separately. Each of these chapters covers the different versions that were proposed, designed, and/or tested. These chapters also discuss the advantages of each version, and if applicable, why the version was later modified in favor of its final form.
Chapter 3

Background

This chapter covers the gross anatomy and physiology of the human joints that were used to model the designed robotic joints in this thesis. Understanding the basic biology of each joint will help clarify design decisions made in later chapters. As such, information about the biological structure of the joint, range of motion of the joint, and degrees of freedom of the joint is found here. Included in this chapter is information about the specialized 3D printer used to develop and test the mechanical joints, this information includes mechanical properties of the materials used and material testing results provided by the company.

3.1 - Anatomy of Synovial Joints

Synovial joints are the most common and most flexible type of joint in the human body [7]. Synovial joints join bones with a dense and fibrous capsule that is filled with synovial fluid or synovia. Synovia is a non-Newtonian fluid, which has the consistency of the white of an egg. This fluid acts as lubrication between the cartilage of the joint during movement [8].

There are six different classifications of synovial joints, however, the focus of this work is on the ball and socket type, such as the hip or shoulder and the hinge type, such as the ankle or the carpals of the wrist. Both of these joint types have distinct movement
characteristics that are primarily defined by the articulating surfaces of the bones. The ball and socket type joint allows for three axes of rotation (flexion/extension, abduction/adduction, and lateral/medial rotation), while hinge type joints only allow for flexion and extension in one plane [8–10].

All synovial joints are made up of a synovial cavity, a joint capsule, and articular cartilage (Fig. 2). The synovial cavity is the space between the bones that is filled with synovia.

Figure 2 - Cutaway of a ball and socket synovial joint

The joint capsule is then further broken up into the outer layer and inner layer, the inner layer is made up of the synovial membrane, which secretes synovia, while the outer layer is a fibrous membrane that sometimes contains ligaments. The articular cartilage functions to reduce friction during movement and protects the joint from impact forces [8, 11, 12].
3.2 - Hip joint anatomy and physiology

The hip joint has three degrees of freedom, all rotational, (Fig. 3). The hip has no translational degrees of freedom.

![Figure 3 - The three degrees of freedom of the hip joint](image)

The hip joint (Fig. 4) is a ball-and-socket synovial joint where the femoral head is the ball and the acetabulum creates a cup-like depression in which the femoral head fits [13].
A synovial joint, as previously discussed, is characterized as a joint that is surrounded by a joint capsule. A joint capsule is a dense and fibrous structure that is analogous to tendons, but forms a sleeve around the joint. For the hip, the joint capsule is primarily formed from three ligaments:

1. Iliofemoral ligament
2. Pubofemoral ligament
3. ischiofemoral ligament

Ligaments are fibrous structures that connect bone-to-bone, similar to tendons, which are fibrous structures that connect muscle to bone. The iliofemoral ligament spans the distance between the anterior inferior iliac spine and the intertrochanteric line of the femur. It is “Y” shaped. This ligament prevents the hyperextension of the hip joint [13]. The pubofemoral ligament has a triangular shape and spans between the superior pubic
rami and the intertrochanteric line of the femur. This ligament prevents excessive
extension and abduction. Lastly, the ischiofemoral ligament spans between the body of
the ischium and the greater trochanter of the femur. It has a spiral orientation and
prevents excessive extension of the joint. These ligaments completely enclose the hip
joint and form the joint capsule.

The only intracapsular ligament is the ligamentum teres (Fig. 5), a round ligament
that connects the femoral head with the acetabulum inside of the joint capsule. The
ligament is the strongest ligament in the body; it also contains blood vessels that supply
the femoral head with its blood supply, although this function is less significant after
childhood. The ligamentum teres also plays a role in joint stability while physically
limiting the range of motion of the joint to prevent superior subluxation (dislocation of
the joint) [14]. The Transverse acetabular ligament, which consists of strong flattened
fibers, prevents inferior subluxation and works in conjunction with the ligamentum teres.
Ligament stiffness is thought to be the primary way the body reduces the need to activate
muscles to help remain upright.
Figure 5 - Lateral view of the hip joint showing the ligamentum teres (cut into two pieces), the only intracapsular joint ligament in the body (green)

The joint capsule is filled with synovial fluid, a non-Newtonian fluid that has the constancy of the white of an egg. The purpose of the fluid is to reduce friction between the articular cartilage and joint during movement. This helps give joints their long life despite the harsh and cyclical loading conditions.

Range of motion for the hip is different for males and females; this is due to the differences in size and joint angles. To complicate this even further, age and lifestyle also have a factor on joint range of motion [15]. However, the range of motion seen in the hip joint is typically between the values listed in Table 1.
Table 1 - Range of motion upper and lower bounds for the human hip joint [16].

<table>
<thead>
<tr>
<th></th>
<th>Lower bound (degrees)</th>
<th>Upper bound (degrees)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flexion</td>
<td>90</td>
<td>135</td>
</tr>
<tr>
<td>Extension</td>
<td>10</td>
<td>30</td>
</tr>
<tr>
<td>Adduction</td>
<td>10</td>
<td>30</td>
</tr>
<tr>
<td>Abduction</td>
<td>30</td>
<td>50</td>
</tr>
<tr>
<td>Internal rotation</td>
<td>30</td>
<td>45</td>
</tr>
<tr>
<td>External rotation</td>
<td>45</td>
<td>60</td>
</tr>
</tbody>
</table>

Important to the geometry of the legs, but not specific to the hip joint itself is the quadriceps angle (q-angle). Q-angle is the angle formed by the femur and the hip relative to the ground (Fig. 6). Specifically it is the angle between a line formed by the resultant force of the quadriceps, made by connecting a point between the anterior superior iliac spine (ASIS) to the mid-point of the patella and a second line from the central patella to the tibial tubercle [17]. As this angle increases, the risk factor for patellar subluxation increases.

Figure 6 - Measuring points used to determine the quadriceps angle (q-angle).
While q-angle differs between subjects and age, for males between 18 and 35 years, the average and healthy q-angle is considered 13.5 ± 4.5 degrees. For females, the q-angle is larger, 18.1 ± 4.5 degrees is considered the healthy range for subjects between 18 and 35 years [18, 19]. Due to the cyclical loading applied to the femoral neck the q-angle an important design consideration when trying to model human legs because it is a strong determiner in fracture risk [19].

### 3.2 - Knee joint anatomy and physiology

The knee joint is one of the largest and most complex joints in the body. This is attributed in part to the forces the knee experiences in normal use. Impact loads from walking or running typically exceeds 4 times bodyweight, the knee joint is responsible for mitigating some of that load.

The knee has six degrees of freedom (DOF), three rotational and three translational (Fig. 5); these degrees of freedom give the knee a complex, but needed motion for normal function.
Coincidently six different ligaments provide stability for the knee (Fig. 8). These ligaments are:

1. Anterior cruciate ligament
2. Posterior cruciate ligament
3. Lateral collateral ligament
4. Medial collateral ligament
5. Popliteofibular ligament
6. Anterolateral ligament
The primary function of the anterior cruciate ligament (ACL) is to resist anterolateral displacement of the tibia on the femur (femur sliding backward on the tibia or the tibia sliding forward on the femur). The posterior cruciate ligament (PCL), has the primary function of resisting posterior tibial displacement (femur sliding forward on the tibia or the tibia from sliding backward on the femur), especially at 90 degrees of flexion [20].

The primary function of the lateral collateral ligament (LCL) is to resist varus displacement at 30 degrees of flexion. Serving a similar role, the medial collateral ligament (MCL) resists valgus angulation (the ligaments work together to prevent the femur from sliding side to side) [20].

The last two ligaments manage the rotational stability of the knee. The popliteofibular ligament (PFL), also known as the Posterior Lateral Corner (PLC), primary function has only been determined in the past 30 years; it resists posterior translation, varus, and external rotation [21]. It is not shown in the image above because it is posterior to the knee while the image above is an anterior view.

Lastly, the recently (re)discovered anterolateral ligament (ALL) has been shown to be an important stabilizer of internal rotation at flexion angles greater than 35 degrees. This means the ALL does not assist the ACL and PCL in stabilization during translation [22]. Because of its recent rediscovery and its location near the LCL, it too is not labeled in the diagram above.
Because the last two of these ligaments deal with the axial rotational aspects of the knee and in robotics we want to limit the degrees of freedom for control purposes, the focus of this thesis and subsequently the joint designs, are primarily on the first four ligaments. These ligaments primarily help stabilize the knee during flexion and extension while resisting medial and lateral translation; this is the main function of the knee that we want to mimic. The additional rotational aspects are then separated from the design, and then added back in at a later time [23].

In order to minimize the force needed to deal with high loads the knee joint utilizes a changing center of rotation. As the flexion of the joint increases, the moment arm across the front of the joint increases. This mechanism keeps the joint compact and greatly reduces force requirements when compared to a static center of rotation.

The knee joint also utilizes what is called a “screw home” mechanism, called such because during the last 20 degrees of extension the tibia with respect to the femur externally rotates by roughly 10 degrees [24]. This mechanism tightens both cruciate ligaments, which lock the knee. The tibia with respect to the femur is then in a position of maximal stability. In this position, the knee requires no extra forces to stay fully extended [24].

3.3 - Ankle and foot anatomy and physiology

Much like the hip joint, the ankle joint is formed from several different bones that have different purposes and dimensions, but for our purposes are grouped together. For
this reason, we are grouping the foot anatomy and physiology with the ankle joint like we did with the hip joint and pelvis.

### 3.3.1 - Ankle anatomy and physiology

The articulating surfaces of the ankle are made up of three different bones, the talus of the foot along with the tibia and the fibula, which together form a bracket shaped socket (Fig. 9). Similar to the hip joint the ankle is a synovial joint; functionally the joint acts as a hinge joint allowing for stable dorsiflexion and plantarflexion only [25, 26]. Eversion and inversion is a result of the movement by the subtalar joint, which is formed by the calcaneus and talus and is distant and separate from the ankle joint [27].

![Figure 9 - The tibia and fibula form a square shaped bracket that fits around the heart-shaped articular surface of the talus](image)

The ankle joint is held together by two main sets of ligaments both originating from a malleolus, the bony prominence on either side of the ankle. The two sets of ligaments are grouped by location medially and laterally [26].
While the ankle and foot has 3 degrees of freedom, modeling the ankle joint alone is typically done as a hinge, because the other degrees of freedom are created by the subtalar joint [28, 29]. For the purposes of this thesis, we will approximate both the hip and ankle joints as ball and socket type joints. This approximation will help remove some of the instability of the ankle joint and give the joint increased range of motion.

### 3.3.2 - Foot anatomy and physiology

The foot is made up of twenty-six individual bones. The calcaneus bone is the largest, strongest, and the most posterior bone of the foot and is the attachment point for the Achilles tendon; superiorly to the calcaneus is the talus, which forms a tri-planar, but uniaxial joint with the calcaneus. The talus also serves as the loading surface for the distal end of the tibia and fibula [30].

Biomechanically, the foot behaves in two separate halves [27]. The two medial most metatarsals and phalanges move in conjunction with the talus forming a chain of interconnected motion [27]. The other three metatarsals phalanges move in conjunction with the calcaneus also forming a chain of interconnected motions [27]. Therefore, we simplify the design of the foot to just two toes instead of needing to recreate all five toes for use in mimicking the biomechanics.
3.4 - 3D printing with continuous fiber

This work uses a MarkForged Mark II 3D printer [31]. The printer prints in a nylon and carbon fiber chop composite called Onyx. It also has the unique and patented ability to print with continuous fiber inlay. The printer has the ability to add continuous fiberglass, High Temperature and High Strength (HTHS) fiberglass, Kevlar or carbon fiber to the prints (Fig. 10).

With each of these fibers having its own mechanical properties, inlayed fiber is used to augment the print depending on the requirements of the part. Thus, we add strength, temperature resistance, or wear resistance by incorporating the corresponding fiber into particular layers or sections of the part.

![Figure 10 - Cutaway of a 3D printed part showing the continuous Kevlar fiber inlay (yellow) inside the nylon and chopped carbon fiber composite (black)](image)

By utilizing this continuous fiber inlay, the company claims a part achieves a strength to weight ratio similar to aluminum. To back these strength claims, the company
tested the mechanical properties of parts with continuous fiber. These properties are measured by a method similar to ASTM D790 and are shown here in table 2 [32–35].

<table>
<thead>
<tr>
<th>Property</th>
<th>Test Standard</th>
<th>Carbon</th>
<th>Kevlar</th>
<th>Fiberglass</th>
<th>HSHT</th>
<th>Aluminum#</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tensile Strength (MPa)</td>
<td>ASTM D3039</td>
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<td>590</td>
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Chapter 4

Methods and Materials

This chapter presents the detailed design and implementation of hip, knee, and ankle bio-equivalent joints, and outlines their strengths as well as their limitations.

Unfortunately, the ability to measure biomechanical quantities of a joint in vivo is limited. I assume that MRI modeling of the joint provides enough biomechanical information that I am able to construct model, because the ex vivo modeling of joints removes some of the normal, or pathological conditions. From this model, I then design a mechanical joint that has properties similar to the corresponding biological joint, for instance the knee, which has a changing center of rotation and the ability to lock in the upright (standing) position.

This chapter also details the design process that was used to create the robot. I will show how I created 3D models using different medical scans and where those medical scans were obtained. Then the chapter covers each of the designed versions for each type of joint.

4.1 - Medical scans to 3D models

MRI scans and CT scans are similar in that they are non-invasive ways of imaging inside of the body. CT scans (or Computerized tomography) use multiple X-rays taken at
different angles to produce cross-sectional images. MRI (Magnetic Resonance Imaging) scans use strong magnetic fields, radio waves, and field gradients to generate cross-sectional images. These cross-sectional images are enhanced to show particular details of the anatomy by adding IV contrast.

CT scans are excellent at looking at bones, but do not provide a clear picture of the soft tissues without the aid of contrast. Conversely, MRI scans are excellent at detecting even slight differences in tissue and is the better choice for showing tendons and ligaments. Therefore, both scans types are necessary to develop a clear understanding of the kinematics and produce a 3D model capable of reproducing the correct motions.

4.2 - Obtaining medical scans

The first step was to acquire medical scans; using the open repository of medical scans provided by the software, I was able to locate several different MRI and CT scans (Fig. 11).
The DICOM files selected needed to be free from injury, had to have adequate contrast to resolve the joint structures, and need to be the same sex due to the biological differences between males and females. Furthermore, preference was given to files of patients that fell into the same age range to minimize the differences between scans. Scans were selected from adult males because the bipedal robot needed to be able handle roughly 91 kilograms (200 lbs.). Lastly, the slice thickness needed to be as small as possible to maximize the fidelity of the 3D model [36].

4.3 - Creating a 3D model

The process of turning medical scans to a 3D model is essentially the same for each joint; for this reason, this thesis will only go into detail about process for a single
joint, the knee joint. The joint was selected for the next chapter because it is the most complex joint that was modeled and is the best to illustrate the process.

3D slicer was used to read the MRI and CT files.

“3D Slicer is an open source software platform for medical image informatics, image processing, and three-dimensional visualization. Built over two decades through support from the National Institutes of Health and a worldwide developer community, Slicer brings free, powerful cross-platform processing tools to physicians, researchers, and the general public.”

The software was chosen because it is capable of processing a range of medical imaging data. It parses the different scans and acquire different measurements of tendons directly from the joints themselves.

To create the 3D models, the chosen medical scans in DICOM (Digital Imaging and Communications in Medicine) format were imported into the 3DSlicer software (Fig 12).
The software automatically assembles the scans into a model by organizing the scans; however, the different tissues and bones needed to be selected manually in order to create a model from the scans. The contrast of the scans was adjusted manually to provide the best intensity gradient for the section of interest (bones, tendons, and ligaments) from the surrounding tissues.

CT scans show the bone much clearer than the MRI scans while the MRI scans show the tendons and ligaments with more clarity than the CT scans (Fig 13). By utilizing these larger gradients, the software has a much easier time separating the soft tissue from bone or the ligaments and tendons from tissues.
Figure 13 - Results of a CT scan (left) vs. an MRI scan (right) notice that the CT scan shows a much higher contrast for bones than the MRI scan.

The program then selects sections of each layer of the scan within the stated range (Fig. 14).

Figure 14 - Initial attempt as selecting bone exclusively using the software’s selection algorithm (selection in brown)

I manually cleaned the scans once the software selected and labeled the sections as the target tissue or bone. By removing unwanted selections made by the program. This
step verifies the software selected the correct areas of the scan and requires manually fixes any discontinuities or erroneous selections (Fig. 15).

![Figure 15 - Bone selection (brown) after manual cleanup and verification of selection](image15)

After manual cleaning, I converted the selections to a 3D model using the built in functionality. However, the model is not ready to be used due to how the software processes the slice thickness of the MRI and CT scans layers. Each layer is a simple extrusion to the thickness of the MRI or CT scan slice thickness, which in this case is 1 mm (Fig 16).

![Figure 16 - Initial result from the extrude operation using 3D Slicer. This operation creates a "stepped" effect that needs to be later smoothed.](image16)
This model must be smoothed, so the model was then exported from the 3DSlicer and into another open-source software called Mesh Mixer. This software smooths the scans by determining, then attempting to maintain, tangent continuity.

Tangent continuity occurs when the two curves share a common endpoint and are tangent to one another at that point. A high fidelity model that limits deformation from this process is created by maintaining tangent continuity preferentially over other smoothing operations (Fig 17).

![Figure 17 - (A) The 3D model from 3D Slicer loaded into Mesh Mixer and (B) after the tangent smooth operation is applied](image)

**4.4 - Hip Joint**

The hip is made up of three different fused bones, so for the purposes of designing and building a robot this is simplified to just one. That leaves us with three separate bones, the left and right ilium, and the sacrum.
To design the hip, CT and MRI scans of the lower extremities were used to create 3D models of the joints using an open-source software called 3D Slicer (Fig. 18). This program organizes the Digital Imaging and Communications in Medicine (DICOM) files so they are manipulatable in a 3D environment. The software selects specific portions of each layer, and by applying an extrusion operation corresponding to the layer thickness of the medical scan, creates a 3D model.

Once these layers are extruded, a tangent smooth operation is applied to the model to eliminate the stepping artifacts from the extrusion operation. Using this process, we recreate the structures from the medical scan into a high fidelity 3D model. From these models, the initial articulating surfaces of the designed joint are created and sized similarly to the corresponding joints in the body. The files used to create our hip model
were obtained from an open source biomedical 3D printing community called embodi3d [37].

The hip joint has several different geometric considerations which need to be considered to maximize the life of the designed joint [38, 39]. These geometric parameters (Fig. 19) are the femoral neck length, the narrow neck width, and the neck-shaft angle. The neck of the femur is especially at risk of fracture from loading. The joint geometry in the design comes from the median values of the accepted range for an adult male and not the medical scans since these are considered the ideal values [40]. However, the overall shape of the contacting surfaces is based on the medical scan models (Fig 20).

Figure 19 - Geometric considerations for designing the hip joint and femur

A way to attach the pneumatic actuator securely to each side of the joint needed to be included into the design process because the braided pneumatic actuators are going to need to resist some of the applied load. Adjustable steel hose clamps secure the actuator
to either side of the joint; a recess on both ends of the links keeps the actuator firmly secured when tension is applied to the joint.

As previously mentioned, the hip is broken into three separate bones to mimic the human hip the two ilium and the sacrum (Fig 21). The parts connect to each other the same way the hip does, a spring and damping element was added between the bones using braided pneumatic actuators. These flexible connections help the hip absorb impact loading similar to how the real hip behaves when walking.
4.5 - Knee Joint

The knee joint is one of the most complex joints in the body. This section covers the three different versions of the joint and the design processes for each version.

4.5.1 - Version 1

An early solution at modeling the soft structures of the knee with rigid aluminum connections was to include an adjustable compliant element to the design. A small pneumatic actuator was selected because it matched the diameter of the human tibia. This actuator provides adjustable compliance. Furthermore, pressure in the actuator is
adjustable to limit slip between the surfaces, the main cause of wear, and reduce impact shock as the robot moved or if the robot fell.

Machining cost was a factor so the design needed to be limited to the geometry that could be machined in house. This meant that the most complex geometry that could be created had to be machinable using a 3-axis CNC machine.

The LCL and MCL are located on the outer faces of the knee, so I determined machining solid metal links to act as analogs to these ligaments would be more feasible than trying to model and machine analogs of the ACL and PCL, which are located on the inner faces of the knee.

After determining which ligaments to model, I created the mechanical knee design in SolidWorks (Fig. 22). After several simulations under a variety of rotational input conditions, the proposed joint design was determined to perform similar to the biological counterpart.
To machine the part, the fibular end and tibial head (the two load bearing surfaces), were imported into a CNC program called MasterCAM (Fig. 23). Using this program, the order of cuts, the tolerances, number of passes, and finish to the design are controlled. This program also runs simulations to test the order of operations based on the sizes of the bits used and the operating conditions of the machine, which is set by the program, or by the user.
The distal extremity of the femur and the proximal extremity of the tibia were machined using a 3-axis CNC machine (Fig. 24). This would give the best true to CAD outcome and cut the parts quicker than trying to machine each part by hand on a mill.
The rest of the parts were machined on a mill, lathe, or a 2-axis CNC machine (Fig. 25).

Figure 25 - Aluminum slug being machined for the tibial end using a 2-axis CNC machine.

Welding of the square tube that holds the pneumatic cylinder was done using a TIG welder. Welding of the components was done prior to assembly (Fig. 26). Between setup, takedown, clean up, and waiting to access the 3-axis CNC machine, the fabrication process took roughly 6 weeks from start to finish.

Figure 26 - Initial completion of the knee joint prior to welding
4.5.2 - Version 2

Having access to new equipment, the MarkForged 3D printer, the primary goal of the second joint design was to address problems with the first design. The second goal was to determine the abilities of the new technology and to evaluate the veracity of the claims regarding material properties. Significant changes were not made to the design.

However, a few key changes were made to the 3D model to make it more suitable for 3D printing. The lateral and medial faces of the femoral portion of the design were hollowed to lighten the design (Fig. 27). This cut the amount of material needed, shortened the time to print, and did not affect the strength of the design. The other change was to the LCL and MCL connections. The connections were modified for added strength in 3D printing. There were no other significant changes made to the version one design. For example, the first iteration of the second knee joint used the same contact face angles as the first version of the joint.

Figure 27 - Modification of the femoral end to reduce weight.
However, this was changed for the second iteration of the second design. The ability to lock the joint when fully extended was added to the tibial contact face. A protrusion in the center of the tibial contact face was added. This protrusion was shaped to give the shaft that was press fit into the bearings of the femoral end a way to lock when the joint is fully extended (Fig. 28).

![Tibial head showing the addition of the screw-home mechanism](image)

*Figure 28 - Tibial head showing the addition of the screw-home mechanism*

The fibular end of the joint was modified with the addition of a replaceable clip-on face for the load-bearing surfaces of the fibular end of the joint (Fig. 29), which was printed using a Kevlar inlay because of the wear properties of the material.
The fibular end was further modified to include rounded teeth that lock in with the clip-on faces. This modification provided a tight fitting connection that would not create unwanted sliding. The clip-on faces attach in such a way that they do not dislodge from the fibular end of the joint during use (Fig. 30).
4.5.4 - Version 4

With the additional equipment and because I was no longer constrained by the limitations of a 3-axis CNC machine, I redesigned the entire mechanism by modeling the ACL and PCL. This change meant not only could a more compact joint be created, but the geometric complexity of the joint could be increased as well.

Design of the distal end of the femur and the tibial head were done to ensure that the loading surfaces made contact throughout the entire range of motion of the joint. By doing this we redirect the forces from the linkage to the condylar surfaces, this will reduce wear on the pins and reduce the risk of catastrophic failure.

The contacting surfaces of the knee could not be copied outright, because the linkages we are using are solid and the linkages of the human knee are flexible. Instead, a new design for the tibial contact surfaces was designed to reduce sliding while still being compact. For that reason, the curve of the medial condyle, the larger of the two condyles, was chosen for both the contact surfaces of the distal end of the femur.

The tibial head was designed so that when the end of the femur is constrained to the crossed four-bar linkage it maintained contact throughout the range of motion. In order to do this, the shape of the curve created by the femur when constrained by the four-bar linkage was calculated and then used to create a 2-dimensional profile of the contact surface of the tibia. This curve was then turned into the profile of the tibial contact surface using SolidWorks. The rest of the tibial head was then designed around the movement of the linkage so that it would not interfere with the range of motion.
Advantageously, by modeling the ACL and PCL instead of the MCL and LCL in addition to representing them by solid links, the new model without additional modifications had a simplified version of the screw home mechanism that lets the joint lock at full extension. This new locking mechanism was more robust than the one that was created for version 2.

The analog to the screw-home mechanism is achieved using the geometry of the linkage because the design uses a solid and crossed 4-bar linkage design. Limiting the forward movement of link 1 through modification of the condylar surface of the tibial head creates a mechanical stop that prevents any additional forward movement (Fig. 31).

![Figure 31 - The modification of the tibial head to allow for upright locking](image)

Once the joint is in the upright position, the modification to the tibial head creates a locking mechanism such that any amount of loading force applied through the knee – for example while in a standing position – cannot induce a rotation of the joint due to the forward location of the instantaneous center of rotation (ICR) at full extension. The design directs weight through the condylar surfaces of the distal end of the femur and the
tibial head instead of the connecting links of the joint. This broad surface contact spreads out the load and reduces this source of premature wear and failure.

Once the linkage was designed, designing a patella to maximize the efficiency of the knee needed to be done. One of the first considerations for approximating the patella in the design was the contact faces. Contact needs to be maximized to reduce the wear of the surfaces. Additionally, the force vector applied by the patella to the joint should point perpendicularly to the moment arm in order to maximize the torque about the joint applied by the quadriceps muscles. The quadriceps muscles apply forces to the knee joint (Fig.32), where the resultant force \( F(\theta) \) passes through the instantaneous center of rotation and is calculated by

\[
F(\theta) = 2Q \cdot \cos\left(\frac{\theta}{2}\right)
\]  

(1)

The angle \( \theta \) is the angle between the quadriceps tendon and the patellar tendon. Because the ICR curve of the designed joint is flattened, the resultant force is directed perpendicularly to the moment arm and through the ICR longer than an ICR curve that was more convex. By correctly angling the patellar using Equation 1, the resultant force from the actuator is maximized through the entire extension of the joint.
4.6 - Ankle Joint and foot

This section covers the two designs that were created for the foot, the main design consideration for the foot was that it needed to be under actuated and it needed to include the articulations that make the gait of the robot fluid (IE- the feet could not be solid). Two designs of feet were created, both of which are covered in this section.

4.6.1 - Version 1

The design of the foot only needed to be able to function under actuated, the first version was designed using pin joints (Fig 33) and designed using measurements of the human foot obtained from the 3D models.
This design includes the same lever style design the calcaneus (the bone that forms the heel) has in the foot. The protrusion (Fig. 34) adds leverage in the same manner as its biological counterpart.
A braided pneumatic actuator attaches to the underside of the foot at the rear and connects to each of the two metatarsals. This acts as an elastic element and creates the arch of the foot.

4.6.2 - Version 2

The second design corrects the use of pin joints in favor of using braided pneumatic actuators for attachment. The design also better incorporates the braided pneumatic actuator that is used to create the elastic element for the arch of the foot.

An extra contact point was added to the foot design so that the metatarsals of the newly designed foot make contact with the ground. This is a more natural design that gives the robot a larger contact area during the step off portion of the gait (Fig. 35).

Figure 35 – 3D model of version 2 of the foot as seen laterally (and without the pneumatic sleeve, that attaches the joints).

Using the same pneumatic cylinder connections that are used in the hip and ankle, the pin joints were eliminated. This added damping to the foot as well as an elastic element between joints.
The pneumatic actuator that attaches on the underside of the foot from the calcaneus to each of the metatarsals is now inside of the calcaneus (Fig. 36). Unlike the last design, the calcaneus (bone in the heel of the foot) and the talus (joint that forms the ankle) are joined together. This combined structure forms a protective enclosure for the braided pneumatic actuator used for the arch of the foot.

*Figure 36 - By combining the talus and calcaneus, the pneumatic spring element used for the arch is now protected.*
Chapter 5

Results

This section covers the result of testing for each joint. It covers the performance metrics and when applicable, how the designs compare to the pin joint that they are trying to replace.

5.1 – Hip Joint Results

The three pieces of the pelvis are connected using braded pneumatic actuators as a spring and damping element (Fig 37).

Figure 37 - Lateral view of the pelvis showing several vertebrae and better illustrating the connecting surfaces between the sacrum and ilium
Once the hip was designed, the length of the pneumatic actuator needed to be determined in order to maximize the range of motion, because it is dependent upon the stiffness of the braided pneumatic actuator, the pneumatic actuator pressure, the joint gap, and the empty volume inside the pneumatic actuator.

The initial spacing between the two ends of the joint prior to inflation is set such that the range of motion matches closely to the range of motion of the corresponding human joint. By increasing the initial spacing of the two ends of the joint, the braided pneumatic actuator is forced to compress as the joint end comes into contact. This compression of the actuator gives the joint added range because the actuator is no longer fully extended.

Stiffness (k) for these pneumatic actuators is not constant and is a function of the length and pressure of the actuator. This stiffness function is found using a model created by Colbrunn et al. [41] by taking the derivative of actuator force with respect to length

\[ k = \frac{dF}{dL} \quad (2). \]

Using a model Chou and Hannaford developed for braided pneumatic actuators [42] to determine force expressed in terms of gauge pressure \( P_g \) and length (L)

\[ F = \frac{P_g b^2}{4\pi n^2} \left( \frac{3L^2}{b^2} - 1 \right) \quad (3) \]

if we differentiate (3) with respect to L (2) becomes,

\[ k = \frac{b^2}{4\pi n^2} \left( \frac{3L^2}{b^2} - 1 \right) \frac{dP_g}{dL} + \frac{3P_g L}{2\pi n^2} \quad (4) \]
where \( b \) is the thread length of braided sleeve and \( n \) is the number of turns for a single thread in the length of the braided sleeve (Fig. 38).

![Diagram of thread length and turns](image)

\*Figure 38 - Parameters for determining the single thread length of the braided sleeve and the number of turns for that thread.*

Colbrunn et al. [41] assumes that the actuator is a membrane such that the pressure inside the actuator stays constant throughout the range of motion of the actuator. This assumption means

\[
\frac{dP_b}{dL} \approx 0
\]

making this assumption and applying it to (4) we now have

\[
k = \frac{3P_bL}{2\pi n^2}
\]

To determine radial stiffness, the beam model, where the actuator is treated as a slender member and loaded in a single plane is used. This formula relates the applied moment (\( M \)) to the curvature of the beam (\( \phi \)), the internal pressure (\( P \)) and the beam radius (\( r \)) such that
\[ M = Pr^3 \frac{\pi^2[(\pi-\phi)+\sin \phi \cos \phi]-\nu[(\pi-\phi)^2-(\pi-\phi) \sin \phi \cos \phi-(2 \sin \phi)^2]}{\sin \phi+(\pi-\phi) \cos \phi} \]  

where \( v \) is the Poisson’s ratio of the actuator. Equation (6) is used to determine the stiffness as the joint angle changes (Fig. 39). However, this model is only valid when the joint surfaces inside the air muscle do not make contact because once the surfaces make contact we need to take into consideration the restoring forces the joint adds to the model and is no longer be assumed to be zero. The restorative force of the joint links created by the compression force of the actuator along with the added friction, increase the joint stiffness and this change needs to be taken into account.

![Figure 39](image)

*Figure 39 – Calculated change in stiffness as it relates to joint angle at an initial pressure of 25 psi*

The empty volume remaining inside the actuator has significant effects on the range of motion and stability of the joint. As a bending moment is applied to the joint, the contact surface inside the actuator moves along the ball surface, similar to the joints of the human body and is held in place by the actuator. Therefore, the empty volume inside the joint creates a mechanical limit to the amount of motion that the joint achieves.
Table 3 shows the range of motion for the hip joints of the average adult male [43–45], the variables that impact the range of motion should be adjusted to match closely to these values while attempting to maintain maximum joint stability.

Table 3 - Range of motion of the hip joint for the average adult male

<table>
<thead>
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<th>Motion</th>
<th>Range (degrees)</th>
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<td>Flexion/ Extension</td>
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<tr>
<td>Adduction/ Abduction</td>
<td>51-61</td>
</tr>
<tr>
<td>Internal/ External Rotation</td>
<td>79-99</td>
</tr>
</tbody>
</table>

5.2 - Knee Joint Results

This section covers the results from the design of the knee joint; this includes model testing for all the versions.

5.2.1 - Version 1

Testing of the machined joint, (Fig. 40) met with mixed results. The simulation of the joint did not take into full consideration the effect out of plane forces would have on the joint. Due to this, along with machine tolerances – accidental damage to the prototype confounded this issue – the joint did not appear to be suitably stable when applying a combination of force and torque. This instability caused the femoral head to rotate out of the sagittal plane which was would lead to premature wear and could cause damage to the joint.
The tibia and femur bones attach to the knee using a 44.5 mm square tube stock. The condylar joint was created from machined aluminum stock using the MRI scans. The contact surfaces were lined with strips of UHMW plastic film, which helps reduce the coefficient of friction and gives the joint a smooth, wear resistant surface.

The design did not include the cruciate ligaments, but retained the different curved profiles of the lateral and medial femoral condylar surfaces. The intercondylar tubercules (center of tibia) have been expanded upon and used as a rail to help direct the femur in the case of high out of plane forces acting on the joint. For the prototype joint, the patellar surface has been machined in order to guide the patellar analog similarly to a biological femur.

The use of the pneumatic cylinder as an adjustable complaint member worked as expected and added stability to the joint, but also created an internal joint torque pointing towards 45 degrees from full extension.
As previously mentioned the human knee has a screw home mechanism that locks the knee when in the upright position. The design also needed to be redesigned to let the joint lock in the upright position.

No testing of the joint was done and instead it was redesigned to better deal with out of plane forces. Additionally, the weight of the joint needed to be reduced, so other material options needed to be explored.

5.2.2 - Version 2

The second version design was 3D printed instead of machined. The new design underwent modifications to fix the instability of the first joint design and decrease the weight (Fig. 41).
The design has a clip-on loadbearing face for the distal end of the femur. This clip-on end helps reduce cost by giving the option of replacing only the loadbearing surface (Fig. 42).

![Figure 42 - 3D printed femoral end with the clips removed from the end](image)

These grooves help keep contact between the clip-on face and the femoral end to reduce unwanted movement between the two components (Fig 43).

![Figure 43 - 3D printed femoral end with the clips inlayed with Kevlar added back into the femoral end](image)
The design includes a mechanism for locking the joint in the upright position, similar to the screw home mechanism. This addition eliminated the instability the first design had when torque was applied perpendicularly to the joint.

Several design changes to the screw home mechanism had to be made in order for it to function properly; these modifications were made to the center protrusion and consisted of changes in the geometry of the locking portion itself, where the metal bar would rest (Fig. 44).

![Figure 44 - Second version of the 3D printed knee showing locking mechanism (circled)](image)

By increasing the width of the LCL and MCL analog connections, the design reduced the deflection from out of plane forces significantly. This design change also created enough room to use roller bearings; this smoothed the joint movement, reduced the friction, and therefore likely increased the life of the joint when compared to the Version 1 metal-on-metal design.
This joint underwent a series of tests to determine the length of the torque arm, range of motion, and center of rotation (Fig 45).

![Figure 45](image)

*Figure 45 – Theoretical torque requirement to move a 46-kilogram load over the angle of rotation (blue solid line) vs the torque required for a pin joint (red dashed line)*

The joint has a theoretical maximum torque requirement of 100 N-m, which is less than half the torque required to move a pin joint with the same weight.

The sliding to rolling ratio is an important parameter for the assessment of the joint since it estimates the amount of wear on the joint, it was necessary to determine the ratio for the proposed condylar joint [46]. This is calculated by modeling the contacting surfaces of the tibia and femur and the 3D model to create a motion study using SolidWorks software.

Rigid body kinematics is applied to determine the sliding to rolling ratio. The ratio is calculated as the difference between the arc lengths on each contacting divided by the arc length of the moving link, or:
\[ \chi(\theta) = \frac{\Delta L_{\text{tibia}}(\theta) - \Delta L_{\text{femur}}(\theta)}{\Delta L_{\text{tibia}}(\theta)} \]  

(8)

where

\[ \Delta L_{\text{tibia}}(\theta) = C_{\text{tibia final}}(\theta) - C_{\text{tibia initial}}(\theta) \]  

(9)

\[ \Delta L_{\text{femur}}(\theta) = C_{\text{femur final}}(\theta) - C_{\text{femur initial}}(\theta) \]  

(10)

are the corresponding incremental differences of the contact arc lengths (Fig. 46).

Figure 46 - Kinematics of sliding to rolling ratio from initial contact point C1 to C2

A sliding ratio of zero indicates pure rolling and a ratio of one signifies pure sliding. If the ratio is between zero and one, the movement is characterized as partial sliding and rolling. For example, a sliding-rolling ratio of 0.7 resulted in 70% sliding and only 30% rolling. If the ratio is positive, then the slip of the femur is higher than the tibia. If the sign is negative, then the tibia has higher slip when compared to the femur.
It is desirable to have the slip as close to zero as possible to minimize the wear of the joint. The sliding-rolling ratio calculation was done over the range of the entire range of motion of the prototype joint from Eq. (8). SolidWorks simulations were then done to determine the sliding-rolling ratio of the proposed knee design with an incremental angle (θ) of 0.75 degrees (Fig. 47).

![Graph showing sliding-rolling ratio vs. knee angle (θ)](image)

*Figure 47 - Sliding and rolling ratio of the proposed joint. Note, the initially high sliding ratio settles because the model settles prior to the start of the rotation.*

Our model suggests a sliding-rolling ratio of 0.159, but if we disregard the initial settling of the 3D simulation, the sliding-rolling ratio drops to 0.126. Due to the complex nature of the human knee, several attempts have been made to analytically model the sliding-rolling ratio [46, 47]. However, these models make several simplifying assumptions that do not accurately characterize the movement of the joint. We cannot confidently estimate the sliding ratio of the human knee joint for comparison, but we expect that the sliding-rolling ratio of our model to be similar to that of the human knee.
(0.3 - 0.5) [47]. It should also be noted that the sliding-rolling ratio of the human knee changes with the change of flexion angle, as does our model plotted in Fig 46.

The proposed joints’ mechanical advantage directly influences the selection of actuators that are used. To calculate the mechanical advantage, the length of the radius arm \( r(\theta) \) needs first to be determined. Using the radius arm the mechanical advantage of the joint is determined (Fig. 48). The mechanical advantage (MA) is calculated by the following

\[
MA = \frac{r(\theta)}{C}
\]  

(11)

where \( C \) is the distance to the center of the joint.

*Figure 48 - Radius arm \( r(\theta) \) changing as a function of the angle of rotation \( \theta \) plotted against the radius arm of a pin joint (red-hashed line)*
5.2.3 - Version 3

Initial prototyping of the joint showed that out of plane forces has a significant effect on the joint when it reached full flexion. To better deal with this, several modifications to the tibial head were made as initial prototype testing went on (Fig. 49).

![Figure 49 - Tibial head changes as the prototype testing progressed](image)

A locking face was added posteriorly to the tibial head (Fig. 50) to eliminate deflection from out of plane forces. This addition was designed specifically to fit into the slot on the distal end of the femur. This had two positive changes to the joint design; first, it becomes the load bearing surfaces for the joint, keeping perpendicular forces from being loaded onto the ACL and PCL of joint. Secondly, it increases the moment arm of the joint to the full length of the tibial head.
The constructed joint (Fig. 51) will be tested later to verify the theoretical results.

Metal fasteners were placed directly into the print so that metal shafts and lubricated sleeve bearings could be added to reduce friction at the joint connections. By
adding the fasteners directly into the print, a clamping force is not required to keep the link on the shaft.

Figure 52 shows the linkage configuration used in the construction as well as the link designation, angle designation, and coordinate system for the following equations.

For n number of moving bodies, there are N number of instantaneous centers of rotation such that

\[ N = \frac{n(n-1)}{2}. \]  \hspace{1cm} (12)

From Equation 12, a four-bar linkage has six ICR, four of which are the joints where two links meet. This leaves two ICR that are not explicitly formed at joints; however, we are only interested in the ICR that is created by the crossing of the links.
This ICR is of interest in particular because any force that creates rotation about the joint need to pass through this point.

This is the ICR formed by the intersection of the lines created from links 1 and 3, where link 1 is the PCL, link 3 represents the ACL, and links 2 and 4 represent the fibular end and tibial head respectively. This closed link configuration is defined as four vectors in a closed polygon where the sum is zero, written as

\[ \overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} + \overrightarrow{DA} = \mathbf{0}. \]  

(13)

However, because \( \overrightarrow{DA} \) is parallel to the origin it is reduced to just the length \( L_4 \).

Then vector equation may be rewritten in complex-number form such that

\[ L_1e^{i\theta_1} + L_2e^{i\theta_2} + L_3e^{i\theta_3} + L_4 \]  

(14)

Next Equation 14 is separated into the real and imaginary parts

\[ L_1 \cos(\theta_1) = L_3 \cos(\theta_4) + L_2 \cos(\theta_3) + L_4 \]  

(15)

\[ L_3 \sin(\theta_1) = L_3 \sin(\theta_4) + L_2 \sin(\theta_3) \]  

(16)

Solving to find the intersection of the two links, we obtain the set of equations for the instantaneous center of rotation given in x and y coordinates

\[ x = L_4 \frac{\tan(\theta_4)}{\tan(\theta_4) - \tan(\theta_1)} \]  

(17)

\[ y = L_4 \frac{\tan(\theta_4) \cdot \tan(\theta_1)}{\tan(\theta_4) - \tan(\theta_1)} \]  

(18)
The length of the links which correspond to our designed joint are \([L_1, L_2, L_3, L_4] = [1.85, 0.92, 2.03, 1.57]\) given in inches. The ICR only moves \(\pm 0.2\) inches out of plane from the desired line of action and has a maximum overall moment arm of 2.7 inches prior to the addition of a patella (Fig 53).

The designed joint is only 2.8 inches wide and has a range of motion of 151 degrees; this is roughly the same size and range of motion of the human knee. In a fully extended position, such as when standing, the joint will not rotate past that point so that no extra energy is needed to keep the joint in that position. This feature, in conjunction with the large moment arm, should greatly reduce the energy requirements of a robot when compared to a robot using a non-locking pin joint at the knee.

![Figure 53 - Instantaneous center of rotation plot of proposed joint for the full range of motion.](image)

I created a motion study to determine the sliding to rolling ratio of the joint using SolidWorks (Fig 54). First, the travel arc length of the tibia \((\Delta L_T)\) and the travel arc length of the femur \((\Delta L_F)\) are defined as
\[ \Delta L_T(\theta) = C_{Tf}(\theta) - C_{Ti}(\theta) \quad (12) \]

\[ \Delta L_F(\theta) = C_{Ff}(\theta) - C_{Fi}(\theta) \quad (3) \]

where \( C_{Ti} \) and \( C_{Fi} \) are the initial contact points and \( C_{Tf} \) and \( C_{Ff} \) are the final contact points of the tibia and femur given an incremental flexion angle (\( \theta \)).

Once the travel arc length is calculated, the sliding to rolling ratio (SR) is calculated by

\[ SR(\theta) = \frac{\Delta L_T(\theta) - \Delta L_F(\theta)}{\Delta L_T(\theta)} \quad (4) \]

Figure 54 - Kinematics of sliding to rolling ratio from initial contact point C1 to C2

A SolidWorks Motion Analysis simulation was done to determine the sliding to rolling ratio with regard to flexion and was calculated at 0.5-degree intervals through the full range of motion of the joint (Fig. 55). The ratio of sliding to rolling of the proposed joint, on average is 0.079 with a minimum value of 0.018 and a maximum value of 0.28.
5.3 - Ankle and foot

This section will focus primarily on the construction instead of the theoretical behavior of the joint because the hip and ankle joint share the same design.

5.3.1 - Version 1

The ankle is approximated as a ball and socket joint; the talus has a ball along with the connections needed to anchor the pneumatic actuator to the joint (Fig 56).

Figure 55 - Sliding to rolling ratio over the designed joints range of motion where zero is a pure rolling condition and one is a pure sliding condition, which increases wear.
A lever arm that was added to the calcaneus to mimic the lever arm the calcaneus has in the foot (Fig. 57). This addition better mimics the human foot because the calcaneus applies a force in the same manner; however, the design leaves the pneumatic cylinder that would act as a spring element unprotected. This pneumatic cylinder would be located just below the lever arm; the attachment point was not included, because this was just a test print.
There only needed to be two toes instead of the five we have because the foot behaves as two separate sections [29]. This meant that the design could be simplified, which also means that it could meet the requirement for it being under-actuated and is shown in the anterior view below in Fig. 58.

Figure 58 - Anterior view of the 3D printed version 1 foot showing the two toes

5.3.2 - Version 2

The second foot design created a more natural foot while also creating a larger footprint (Fig. 59). Furthermore, while almost the entire foot is rounded, drop-testing shows that the design is very resilient to tipping and is much more stable than the previous design.
Figure 59 - Foot design version 2 seen laterally after the assembly using the pneumatic actuators as synovial joints

This design also included two hollow tubes inside the printed foot bones that allowed air to inflate all of the joints from a single connection at the ankle (Fig. 60).

Figure 60 – Section view of the talus in SolidWorks showing the tube inside the model that lets air flow down into the other joints of the foot
Next, the ankle joint needed to be tested to insure that the gap created was large enough to accommodate the pneumatic actuator. Figure 61 shows the full ankle and foot joint assembled with the pneumatic actuators.

*Figure 61 - 3D Printed foot version 2 with the pneumatic actuator sleeve for the ankle added*
Chapter 6

Discussion

With respect to the hip and ankle joints, both joint stiffness and damping is expected to change as the angle of the joint changes, due to the increase in the curvature of the pneumatic actuator and the associated change in pressure, this change mimics the observed behavior of the human ankle [48–51]. This behavior should help stabilize a bipedal robot just as it helps stabilize humans.

Additionally, the joints should exhibit increased stability as the angle of the joint increases because the stiffness of the joint is expected to increase as a result of bending. This means the joint is expected to behave closer to a rigid joint as the angle increases; this too should be beneficial in robotic control.

Because braided pneumatic actuators have a protective fiber braid around the air bladder, should the air bladder puncture or become damaged, if the joint is in tension, the fiber braid should support the load which should help limit damage to the system as a whole. Conversely, if the air bladder fails and the joints are in tension, the fiber wrapping should mechanically limit the joint movement and while the system dynamics of the joint have changed, as long as the load applied to the fiber braid does not exceed its tensile strength the joint should remain semi-functional.

With respect to the knee, the comparison of the ICR curve with one developed by Fekete et al. [50] demonstrate that the placement of the curve is similar to the placement of the ICR curve of the human knee. Due to the compliance of tendons in the human
knee, unlike the solid links used in the current design, the ICR curve of a human knee is more convex than the ICR curve of the designed knee. However, the placement of the curve is similar to the placement of the ICR curve of the human knee and the flattened ICR curve of the designed joint has desirable properties with respect to the force requirements to create motion.

There are too many variables to determine the sliding to rolling ratio of the human knee in vivo so we cannot confidently include a graphical comparison. However, current research on the subject suggests the sliding to rolling ratio of the human knee is between 0.3-0.46 [46, 52].

By mimicking the design of the human knee, the designed joint is comparable in size while having several of the knees’ desirable properties. This is in part due to the complex geometry that was obtained from 3D printing instead of using traditional methods. 3D printing also reduced the time of construction to just over one day as compared to potentially weeks of traditional machining.

Because the joint is made primarily from a nylon-carbon fiber chop and has a continuous carbon fiber inlay, the joint has exceptional strength giving it functionally, but weighs just 0.66 pounds. Furthermore, the majority of the weight of the joint is due to the steel fastening hardware added internally to the design mid-print and not from the print material itself.

One of the goals in the design of our knee joint was to reduce wear, with an average sliding to rolling ratio of 0.079; the joint has a significantly lower sliding to
rolling ratio than the human knee. By having continuous contact of the loading faces, the load applied to the pins is minimized and the addition of the locking extension on the rear of the tibia transfers a majority of the forces that would be placed on the pins at full flexion. By removing most of the loading forces from the pin connections, the joint will be less likely to suffer from a catastrophic failure and should last significantly longer than the traditional pin joint.

Reynolds et al. [53] using a sudden reduction in load with constant pressure experimentally determined the independent estimates for the spring coefficient (K) and the damping coefficient (B) of braided pneumatic actuators. They determined that both the increase linearly with the change in pressure and that B and K could be functions of loading. Furthermore, that as the applied load increases damping of the system increases and the system becomes overdamped, however when the load decreases the system acts closer to a critically damped system.

This behavior should help increase the controllability of the system because the system will not oscillate due to perturbations. This also means that damping is expected to increase as the joint angle increases, which should further help stabilize the system. The proposed ankle joint should be adjusted to match closely with the human range of motion of the ankle as shown in table 4.

<table>
<thead>
<tr>
<th>Table 4 - Average ankle joint range of motion</th>
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<td>Ankle joint</td>
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Future work concerning the hip and ankle joints should include experimentally testing the relationship between the length of the pneumatic actuator, the joint gap after pressurization, initial pressure of the actuator, and the remaining volume inside the actuator to create a more complete model of the joint.

Once a more complete model is created, testing should be done using alternative pneumatic actuators constructed from materials with increased elasticity and flexibility. These properties should be adjusted using this new model in conjunction with the mechanical and material properties of the joints they are mimicking.

Future work for the knee should involve wear testing and further material property testing to verify the material properties data given from MarkForged. This will help better characterize the joint lifetime and failure modes.
Bibliography


