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Thermal and Electrical Resistance of Metal Contacts

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AN ABSTRACT OF THE THESIS OF

Roland E. Ott for the MS in Applied Science

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Abstract approved

In engineering practice it is important to know which factors affect the thermal and electrical resistances of metal contacts. This thesis is to investigate some of these factors such as surface roughness and contact pressure. Thermal-electrical contact resistance ratios for metal contacts were calculated from the experimental data.

The technical literature was searched, and several papers were found in which either thermal or electrical contact resistance was studied separately. However, none of the papers recorded data for both thermal and electrical resistances for the same samples.

The information found in these papers has been used as a background for understanding the nature of thermal and electrical contact resistance.

Both of these contact resistances are primarily a function of the load on the contact and the condition of the surfaces. At low pressures only a small fraction of the total gross area of the contacts is in metal-to-metal contact. Increasing the load, flattens the "hills" and reduces both the thermal and electrical contact resistance. This phenomenon is called "spreading resistance" since the flow of heat or electrical current must spread out after they pass through the restricted areas that are actually in contact.

Another type of thermal and electrical resistance, which is called "interface resistance", is caused by a film of foreign material such as an oxide, etc. on the surfaces of the contacting "hills".

If the space between the "hills" of a contact is filled with air, there is a heat flow by convection currents. The literature indicates this quantity of heat flow is approximately one thousandth of the total heat flow through metal contacts.

Since the only electrical current conduction mechanism acting between areas not in actual metallic contact is that due to thermionic emission, the electrical resistance for these areas will be extremely high at room temperature for which thermionic emission is negligible.

The experimental apparatus to measure both the thermal and electrical contact resistances consists mainly of a bellows-actuated press which is
operated remotely under a vacuum bell. The press pressure loads the sample metal wafers. A thin-film heat meter is used to indicate the quantity of heat flowing through the metal contacts. The temperature drop caused by the contacts is measured with thermocouples. The temperature difference and the quantity of heat flowing is used to calculate the thermal contact resistance. A strain gage on the bellows-press stem measures the loading on the contact surfaces. Electrical probes are used to measure the electrical resistance across the contact surfaces.

The thermocouples and electrical resistance probes are permanently installed in the outer two smooth copper wafers. This makes it possible to quickly change to other sets of sample wafers of other metals and finishes.

In order to use this permanent arrangement, it is necessary to finish two mating surfaces of the particular set of metal wafers to be tested, similar to the permanent smooth copper wafers so that these two extra mating contact resistances can be found and thus be subtracted from the overall contact resistance.

The data indicates that the thermal-electrical contact resistance ratio can be changed by changing the load on the contacts.

The heat meter has performed very well, and this new method of measuring heat flow will undoubtedly become a standard method of measuring heat flux.
THERMAL AND ELECTRICAL RESISTANCE
OF METAL CONTACTS

by

ROLAND E. OTT

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Mr. Michael Tierney of BLH Electronics supplied sample strain gages and information on how to apply the gages.

Mr. Jack Janacek, Head of the Portland State College machine shop, has been extremely helpful in his efforts to put together the bellows press assembly.

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Numerous situations arise in engineering practice in which it is important to know the thermal and electrical resistances at the junction of two dry metal surfaces. Also it is helpful to know how the contact resistances are affected by the condition of the surface, the applied pressure between the surfaces and the temperature.

Electrical failures on clamped joints are due to high contact resistance. With sufficient electrical current flowing, the power loss at the contact may cause high temperatures if sufficient heat is not carried away. The effect of high temperature is to produce oxidation which in turn increases contact resistance.

The problem of thermal and electrical contact resistance is very important in the operation of solid state devices which are fabricated with dry contacts. These are joints that are not welded or soldered but which must dissipate heat and also carry an electrical current.

The purpose of this investigation is to shed some light on the thermal-electrical contact resistance ratios for metal contacts. The ratios that are established for metal contacts under certain surface conditions and mating pressures can be used to establish the expected thermal conductivity for a particular device by observing the electrical contact resistance only. This would be an advantage since
electrical resistances can be measured more easily than thermal resistance in a completed device with metal surfaces in contact with each other.

I searched the literature and found several papers in which thermal contact resistance or electrical contact resistance experiments were described. However, none of the articles included measurement of both the thermal and electrical contact resistances on the same samples. The information found in these papers has been used as a background to describe the thermal and electrical contact resistance processes. The values that were reported in the articles has served as a basis for estimating what data may be expected from my thesis experiment.

In order to study both of the contact resistances simultaneously, it was necessary to load the contact surfaces. This was accomplished with a bellows press which used nitrogen gas pressure to load the metal contact surfaces. A thermoelectric-type of thin-foil heat meter was placed in series with the metal wafers to measure the heat flow across the contacts. Thermocouples indicated the temperature drop across the metal contacts. A strain gage on the stem of the press was used to indicate the loading between the contacts. Potential type of instruments were used to measure the electrical resistance between the contacts. The whole assembly was placed in the bell jar of a vacuum system in order to prevent thermal convection currents.
CHAPTER 2

THERMAL RESISTANCE OF METAL CONTACTS

There is a close analogy between the thermal and electrical joint-conductance mechanism. The concept of spreading resistance developed through study of electrical contacts is adapted to the interpretation of the behavior of thermal resistance presented by a joint between metal surfaces in a thermal circuit. (12, p. 259)

Data from the references has shown that thermal contact resistance of joints is primarily a function of the load on the contact surfaces. It is possible, at sufficiently high pressures or for sufficiently smooth and flat surfaces for a very large percentage of the surface area of each contact face to be in actual metal-to-metal contact with the other. The thermal resistance of the joint then would be considered to be approximately equal to zero. (12, p. 259)

At low pressures the areas are in metal-to-metal contact over only a small fraction of the total gross contact area. The actual contact area is made up of a large number of separate "hills" or "points" distributed randomly. It is assumed that if a vacuum or even air fills the "void" spaces between the actual contact areas, the majority of the heat flows through the metal-to-metal "hills" since there is such a high resistance to heat flow through the air path or a vacuum. The thermal conductivity through an air film is about one thousandth of
that through the actual metal in contact. It should be mentioned, however, that if hydrogen or helium gas filled the "void" spaces between the actual contact areas, the convection heat flow through these gases would be approximately six times that expected through an air film.

The resistance to heat flow mainly associated with metal contacts can be discussed with the use of the concept of spreading resistance. In this concept, the "lines" of heat flow must "fan out" or "spread out" after passing through the points of actual contact. Since these contact areas are relatively small compared to the overall area of the surfaces, the heat flux is very great at these points. Also the heat must flow latterally at the surface to reach the contact points. As a load is applied to the contacts, the projecting "hills" start to flatten out and a larger total area is available for conducting heat. The rougher the surface, the greater will be the effect on the thermal contact resistance by increasing or decreasing the load. The presence of an oxide film or other foreign material of low thermal conductivity also contributes to the thermal resistance of the joint. However, except at very low pressures, the oxide resistance appears to account for only a small part of the total thermal contact resistance. (12, pp. 259-260)

The conclusions and results of three thermal contact resistance experiments obtained from the literature are included in this thesis
in order to establish some qualitative basis for indicating the important factors in the measuring of thermal contact resistance.

Weills and Ryder came to the following conclusions based on their experimental observations: (12, p. 266)

1. The thermal conductance of a dry joint increases with pressure, linearly for steel, and generally exponentially for aluminum and bronze.

2. The thermal resistance of dry joints decreases with a decrease in the roughness of the surfaces.

3. At a given temperature, pressure, and roughness, the thermal resistance of dry joints decreases in the order of steel, bronze and aluminum.

4. The thermal resistance of a dry joint decreases as the temperature increases.

Jacobs and Starr found the following results: (6, p. 141)

1. After studying copper, gold and silver contacts in a vacuum they found that only in the case of copper does the conductance vary linearly with contact pressure. (The maximum pressure was approximately 2.5 kg/cm².)

2. They found that the thermal conductance was approximately the same when the surfaces were "just touching" or separated by a few milimeters. This radiation conduction is less than 10⁻³ watt/cm/°C.

3. In all cases the thermal conductances are much smaller at the lower temperatures. This is probably due to adsorbed surface films. (The experiments were conducted at 25°C and -195°C.)
Kouwenhoven and Potter experimented with steel samples and arrived at the following conclusions: (9, p. 520-5)

1. Thermal resistance decreases with pressure in a manner which is essentially exponential. The rate of decrease is greater for rougher surfaces. For very smooth specimens the thermal resistance is practically independent of pressure.

2. The inconsistencies and insufficiency of the data make it impossible to predict absolute values of thermal resistance for given roughness and pressures. It is probable that for heat flow measurements the rms. system of designating roughness is inadequate.

3. At constant pressure and in the absence of corrosion, thermal resistance is substantially constant as temperature level is increased.

4. There is need for more accurate knowledge of the actual surface areas in contact as this remains one of the greatest unknown factors in the problem.

There is generally good agreement between the reported results of the three groups of thermal contact resistance experiments. One noticeable exception, however, is the conclusion by Weills and Ryder who found that the thermal contact resistance of a steel joint decreases linearly with pressure (reported as thermal conductance of a dry joint increases with pressure); whereas Kouwenhoven and Potter stated that the thermal resistance decreases essentially exponentially for a steel joint.
CHAPTER 3
ELECTRICAL RESISTANCE OF METAL CONTACTS

Electrical contact resistance is a very extensive subject, including a wide variety of incidental phenomena, such as thermal effects, coherer action and the behavior of different kinds of surface films. A truly comprehensive treatment of electrical contact phenomena would necessarily include the Peltier, Seebeck and Thomson effects as well. However, these three effects belong to the domain of thermoelectricity rather than to electrical contact theory. For a general background, the review of electrical contact resistance can be found in an article by G. Windred. (13, p. 547)

The four main factors that determine electrical contact resistance as follows:

1. The kind of materials used for each contact
2. The condition and roughness of the surfaces
3. The shape of the contact surfaces
4. The mechanical pressure acting between the contacts (13, p. 550)

In regard to materials, it has been found in general that materials of high electrical conductivity, such as silver and copper, give lower electrical contact resistances than those materials of lower electrical conductivity, such as iron and tungsten. (13, p. 550)
A metal surface, even finished to optical flatness, has many points that protrude. Thus, if two of these metal surfaces are brought together under very low pressure, isolated points on the surfaces will touch. An electrical current will encounter a higher resistance at these restricted points. In addition to a greatly increased current density, the constriction of the lines of current flow also causes a lengthening of these lines and thus causes what is known as "spreading resistance", \( R_s \), between the contacts. If the contact surfaces are not perfectly clean, there is also an "interface resistance", \( R_i \), caused by oxide or gas films. The total contact resistance, \( R_c = R_s + R_i \). (8, p. 458-s)

As the load on the contacts is increased, the "hills" between the contacts are deformed more and more until the surface areas are more nearly mated. The maximum pressure that a given material can withstand without irreversibly deforming is based on the hardness or yield point in compression, \( H \), measured in psi. If \( S_b \) equals the load-bearing-contact area in square inches, we may write for ordinary flat surface contacts that \( S_b = 2F/H \). (The force, \( F \), is measured in pounds.) Whenever plastic deformation or splintering of some of the "hills" in a contact takes place, then additional subareas are brought into contact. When the force is applied a second time, this new contact pattern will cause a change in the electrical resistance. (8, p. 458-s)

In addition to the path of electrical current through the "hills" of a contact, there is another possible path of current flow that
should be considered. This path is across the "gap" between the contacts. This electric current would be carried by electrons that can surmount the distance between the contact surfaces. However, at ambient temperatures a sufficient number of electrons do not have enough energy to carry any appreciable current since the "gap" between the non-touching parts of the surfaces is too great. Even polished surfaces, flat to a quarter wave length of light, still have "hills" and "valleys" of over a hundred Angstrom Units, \( \AA \). (8, p. 458-s)

The high resistance of a "gap" between metal surfaces has been studied by J. Frenkel. For a "gap" of 10 \( \AA \) and a mean free path of electrons of length approximately equal to 100 \( \AA \) (which roughly corresponds to the mean free path of electrons at room temperature) the resistance of the contact per unit surface area (in \( \text{cm}^2 \)) is of the order of \( 10^{-2} \) ohms. For a "gap" twice as large, or 20 \( \AA \), the resistance is about \( 10^8 \) ohms. Further increases in the "gap" would mean practically no flow of electrical current. For a "gap" of 20 \( \AA \), it would require an electric field of 10 million volts per cm across the "gap", corresponding to a potential difference of 2 volts, to obtain a current of the order of \( 10^{-3} \text{ amp/cm}^2 \). (4, pp. 1610, 1611)

Since the "gaps" normally encountered in metal contacts are greater than 100 \( \AA \), any thermionic current between the contacts can be neglected at ambient temperatures. Thus, it is assumed that at ambient temperatures all measurable electrical current flows through the actual contact "hills" and the film on these "hills". (At high
temperatures thermionic emmission of electrons would carry part of the electrical current.

The results and conclusions of three electrical contact resistance experiments obtained from the literature are included in this thesis in order to establish a qualitative basis for indicating the important factors in the measuring of electrical contact resistance.

Kouwenhoven and Little found the following results: (8, p. 464-s)

1. The value of spreading resistance can be effectively controlled by varying the number of contact subareas, "n". They found for the materials tested (silver, aluminum, bronze and brass) that for "n" equal to about 3000 (approximately 15,000 for a contact of one square inch in area) the value of $R_2$ becomes less than one micro-ohm, and effectively disappears, being negligible compared to $R_1$. The load on the one-half inch diameter specimens was 230 pounds or more.

2. For thin surface films, the interface resistance, $R_1$, may be controlled by varying the load on the contacts. $R_1$ is independent of the contact pattern.

3. Increasing the force on the contacts will reduce both the spreading and interface resistance.

G. Windred reported the results of Dr. Eberhard Contius's dissertation on the influence of the magnitude of pressure and surface upon electrical contact resistance. (The original paper was published in Dresden in 1929.) Some of the conclusions made by Dr. Contius are summarized as follows: (13, pp. 577, 579, 581)
1. In the case of pointed contacts the pressure and resistance are related in accordance with the formula \( R = k/(P)^{1/2} \). The actual or effective contact surface approximates closely to the apparent surface.

2. Contact between plane surfaces is formed by the aggregate of several points of contact, the number and size of which depend upon the applied pressure and the surface condition. Pressure and resistance are related by the formula \( R = k/P^n \), where the exponent \( n \) depends upon the nature of the surfaces. In the case of accurately ground and polished surfaces, \( n = 2 \). With increasing pressure approaching the yield point of the entire contact, the value of \( n \) changes gradually to \( 1/2 \). \( P \) is given in kilograms and \( R \) in ohms. (See Table I for values of constant, \( k \)).

3. Particularly smooth surfaces are characterised by high contact resistance. If, however, the surfaces are very rough, the conditions become similar to those of pointed contacts.

4. In the case of ground and smooth surfaces the contacts of large area have a higher resistance than the smaller ones. In the case of normally finished surfaces there is no appreciable difference in this respect.

A portion of Table I, "Relation Between Contact Resistance and Pressure (E. Contius)":
G. E. Luke reported the following: (10, p. 68)

1. With respect to temperature, the contact resistance of the metals varied; thus, some tests were made with copper in which the contact resistance was slightly decreased with increasing temperatures. This would indicate a negative temperature coefficient. This was verified by tests on the resistance of copper oxide, which had a specific resistance of 39,400 ohms per inch cube at zero degrees C and 2160 ohms per inch cube at 100 degrees C. The contact resistance of brass and iron increased very slightly with increased temperatures.

2. Based on a large number of tests on large copper bus-bars, it has been stated that the contact resistance is inversely proportional to the pressure. Thus, $R = 0.0008$ to $0.0016$ for a cleaned copper surface where $R$ is the contact resistance in ohms and $P$ is the pressure in points. This equation says that the resistance of such a contact is independent of the area of contact and depends only upon the total pressure applied. Thus, for a pressure of 1000 lbs. per square inch, the contact resistance given by Luke is 0.9 micro-ohms per
square inch. Experimental results indicate that brass and iron do not follow such a simple equation.

There is generally good agreement between the results of the three groups of electrical contact resistance experiments reported by the researchers.

The formula $R = k/P^2$ given by E. Continent for normal finished plane contacts somewhat resembles the formula $RP = 0.0008$ to $0.0016$ given by G. E. Luke.
CHAPTER 4
MEASUREMENT OF THERMAL AND ELECTRICAL
RESISTANCE OF METAL CONTACTS

Measurement of the thermal and electrical resistances of metal contacts was accomplished with an apparatus that was operated in a vacuum. This arrangement was used in order to prevent heat flow away from the samples by air convection currents.

A bellows press was used to load the contact surfaces. Thus, the load on the sample metal wafers could be changed from outside of the vacuum bell by merely changing the nitrogen gas pressure in the bellows.

The bellows press consists of a base with four steel rods which support a steel upper plate to which the bellows is attached. The support rods have a long thread on the upper end in order to permit adjustment of the height of the bellows assembly. A steel loading stem is connected to the bottom of the bellows and is guided by two plates mounted on the support rods.

A platen is engaged on the end of the loading stem with a ball joint in order to insure that the contact surfaces will be loaded evenly. Resistance wire is wound around a slot which is cut in the upper platen to provide a source of heat. The lower plate was used to conduct the heat away.

A heat meter, which consists of a thin ribbon of semiconductor material, is mounted in series with the metal wafers. The meter
measures the heat flow through the contact surfaces of the metal wafers. (A more detailed description of the heat meter will be given later.) The sample metal wafers are placed between the heat meter on the bottom and the upper permanent wafer on the top.

The thermocouples and electrical resistance probes are permanently installed in the outer two smooth copper wafers. This makes it possible to quickly change to other sets of wafers of other metals and finishes.

With the data available from the thermal and electrical resistance tests on the single smooth copper surface, it was possible to calculate the thermal and electrical resistances of other metal contacts. To accomplish this, two wafers of each of the brass and steel metals were finished on one side similarly to the smooth copper finish and then copper plated. This permitted the sets of the other metal wafers to be mated with the permanently installed smooth copper wafers. Since the thermal and electrical resistances across these two outer smooth copper contacts had been calculated, the net contact resistances for the test samples could be determined.

The load on the metal wafers was measured with a BLH Electronics strain gage cemented to the steel loading stem of the bellows press.

The actual measurement of the heat flow quantity is one of the greatest problems in a thermal contact resistance experiment. The temperature-gradient method has been used extensively in previous experiments; however, this method of measuring heat flow has a possible source of error. Only a small error in the measurement of the slope
of the gradient can cause a large change in the apparent heat flow, especially if the total temperature difference across the resistance is not very great.

In order to insure a more accurate measurement of heat flow, I selected a new method of determining heat flow across the metal contacts with the use of a heat meter. This new way to measure heat flow was developed by Mr. N. E. Hager, Jr. of the Armstrong Cork Company. The heat is measured with a "Thin Foil Heat Meter".

The heat meter used in this experiment consists of a thin-foil differential thermocouple which measures the temperature difference between the two faces of a thin electrical insulator. It is an absolute instrument; i.e., its calibration factor can be calibrated as a function of temperature from the physical and geometrical parameters of the film and the thermocouple materials, and no costly experimental calibration is needed. The particular heat meter used is rated within ± 5% accuracy. The device is found to settle to a stable reading in less than 0.5 sec. The meter has negligible thermal resistance, and its presence does not upset the thermal field under study. These advantages are obtained at the expense of obtaining a very small emf with normal environmental heat fluxes. But the electrical resistance of the meter is so low that good readings can be obtained with modern microvoltmeters. Heat fluxes as low as 0.05 Watts/m² have been detected with 2 second response. (5, p. 1565)

The metal wafers are 1/8 inch thick (0.3175 cm) and 9/16 inch in diameter (1.42875 cm). The wafers were made this particular diameter
so that their area would be equal to 1.6 cm$^2$. The area of 1.6 cm$^2$ was used for contact resistance experiments which were conducted by E. Contius. He developed some relationships between electrical contact resistance and the loading between metal contacts.

Three sets of wafers were finished to a smooth surface by first using a #400 fine grade sandpaper and then polishing them with Crocus cloth. The other three sets of wafers were finished with a No. 80, rough emery cloth. Care was taken to keep the surfaces flat.

The 0.25 inch diameter steel stem permitted a convenient relationship between the kilograms load and the micro-inch indication on the meter. The strain gage read 7.5 micro-inch increments for changes of 5 kilograms in load.

The vacuum system consisted of a mechanical vacuum pump and discharge chamber. Since a very high vacuum was not required, the diffusion pump apparatus was not used. A vacuum was maintained during the tests at approximately 0.5 mm of Hg.

The electrical potential was measured with a current of 0.035 amp flowing across other metal contacts. This current also produced a voltage drop in the leads as well as in the soldered joints. It was necessary, therefore, to determine the voltage drop in the entire external circuit in order to isolate this resistance from the contact resistance. This loss was measured by soldering a wire between the leads to the permanent copper wafers which acted as the electrical potential probes. These two soldered connections simulated the two soldered connections to the copper wafer probes. The wire was
measured to equal the lead lengths between these soldered connections and the terminal points at the copper wafers.

Twenty-five different readings were taken at 0.035 ma, 0.040 ma and 0.045 ma. The resistor was changed each time to control the current.

An interesting thing occurred in the process of measuring the current. The milliamper meter had a bent pointer, but it was the only one available to me. A thought occurred to me, however, that this bent pointer might be used to advantage. I reasoned that possibly the bent pointer could be used as a vernier. This did occur since the bent pointer gradually covered a meter indicating mark as it moved very slightly. It gave the appearance of a changing length from very short to a long black line. With this arrangement I was able to reproduce readings of the external resistance circuit with the 50 ma full scale meter to within two-tenths of a microvolt plus or minus of the average of all of the readings taken at 0.035 ma. The potentiometer read to tenths of a microvolt.

The electrical resistance readings of the smooth and rough steel samples were taken with no heat gradient since the thermoelectric effect of the copper-steel couple would add a considerable potential to the circuit. The electrical resistances of the brass samples were taken with a heat gradient, but this effect is very minor since there is such a small thermoelectric potential difference between copper and brass. This could be considered as a small source of error for any future experimental work, however.
The ultimate goal of my experimental work was to determine the ratio of the thermal to electrical contact resistance at progressively greater loading of the contacts. The summary of these calculations is given in Table 1, Appendix C.
1. The ratio of thermal resistance to electrical resistance can be changed by changing the force between metal contacts.

2. The thermal resistance decreases more than the electrical resistances for the same increase in loading.

3. There is a greater change in the ratio of thermal resistance to electrical resistance for smooth copper and smooth brass contacts for a change of load than for rough copper and rough brass contacts for the same change in loading.

4. The electrical resistance of the rough steel contacts was measured to be very much less than that for the smooth steel contacts for the same loading.

5. The apparent increase of the $R_\theta/R_E$ ratio for rough steel at higher loading is based on the large decrease in the measured electrical resistance since the thermal resistance continued to decrease at the higher loading.

6. The statement by Kouwenhoven and Potter that the fact that the rate of decrease of thermal resistance for steel with pressure is greater for rougher surfaces is "born out" by Fig. 2 of this thesis. (9, p. 520-s)

7. The heat meter has performed very well, and this new method of measuring heat flow will undoubtedly become a standard method of measuring heat flux.
RECOMMENDATIONS

1. If helium gas could be used to surround the metal contacts, the increase in the thermal conductance between the contacts could be measured. Also, tests could be run in air at atmospheric pressure. These two tests could be compared with the tests of the contacts in a vacuum. The test in helium should give a gas conductance approximately six times as great as with air between the contacts. The tests in air could be used to check the value, given by Weills and Ryder, which is about one-thousandth of the total heat that flows through the metal contact.

2. Tests could also be conducted with carbon wafers if one side of two of the carbon wafers were covered with a copper film deposit. This test would indicate the magnitude of non-metal contact resistance.

3. Tests at very low pressures and at higher pressures would give useful data.


APPENDIX A

DESCRIPTION OF INSTRUMENTS

Potentiometer
Leeds and Northrup Company, type K-Z, No. 1133030, used with a
standard cell, 1.0185 volts, range 1 x 10^-7 to 1.6 volts.

Galvanometer

Strain Indicator (For SR-4 strain gages)
Baldwin-Lima-Hamilton, Type N, measures in micro-inches.

DC Milliamp Meter
Sensitive Research Instrument Corporation, Model "University",
No. 921548, range 0-50 ma.

Heat Meter
Armstrong Cork Company, No. 61666-D, thin-foil type (area,
1.44 cm^2).

Vacuum Gage Indicator and Probe
NCR Equipment Corporation, type 701.
APPENDIX B

SAMPLE CALCULATIONS

At 10 Kg load for smooth copper wafers

\[
\text{Temp. Diff.} = \frac{(239.0 - 198.5) \times 10^{-6} \text{ volts}}{43.217 \times 10^{-6} \text{ volts per } ^\circ \text{C}}
\]

\[
= 0.94 ^\circ \text{C}
\]

\[
Q = \text{Heat Flow} = \frac{21.2 \times 10^{-6} \text{ volts} \times 1.44 \text{ cm}^2 \text{ (watts)}}{1540 \times 10^{-6} \text{ volts per cm}^2}
\]

\[
= 19.8 \times 10^{-3} \text{ watts}
\]

\[R_{TC} = \text{Thermal contact resistance, } \frac{\text{cm}^2 \cdot ^\circ \text{C}}{\text{watt}}, \text{ for one joint of copper}\]

\[K = \frac{Q}{\text{Temp. Diff.}}\]

\[
R_{TC} = \frac{1}{K} = \left(\frac{\text{Temp. Diff.}}{Q} - R_{TC}^1\right) \frac{1}{7}
\]

\[
R_{TC} = \left(\frac{0.94 \times 1.6 \text{ cm}^2}{19.8 \times 10^{-3}} - 8.7\right) \frac{1}{7} = 2.6 \text{ cm}^2 \cdot ^\circ \text{C} \text{ watt}
\]

\[R_{TC}^1 = \text{Thermal resistance of six } \frac{1}{8}'' \text{ thick copper wafers}\]

\[
\left(\frac{0.75(2.54)}{0.239(0.92)}\right) = 8.7 \text{ cm}^2 \cdot ^\circ \text{C} \text{ watt}
\]
\[ R_{EC} = R - R_L - R_{EC}' \]

R = Total measured electrical resistance was measured at 0.035 amp

\[ R_L = \text{Electrical resistance of leads to permanent copper wafer probes} = 625.0 \times 10^{-6} \text{ volts} \]

\[ R_{EC}' = \text{Electrical resistance of six 1/8" thick copper wafers} \]

\[ = (1.76 \times 10^{-6})(0.75)(2.54) = 3.4 \times 10^{-6} \text{ ohm/cm}^2 \]

\[ R_{EC} = \left( \frac{636.4 - 625.0}{0.035} \right) \times 10^{-6} - 3.4 \times 10^{-6} \]

\[ = \frac{1}{7} = 74.2 \times 10^{-6} \text{ ohm/cm}^2 \]

\[ L = \frac{R_{EC}}{R_{EC}} = \frac{9.6}{74.2 \times 10^{-6}} = 1.29 \times 10^5 \]

At 10 Kg load for rough copper wafers

Two mating surfaces, of the assembly of the six rough finished copper wafers, were finished similarly to the smooth copper wafers; therefore, two of the resistances, calculated for smooth copper contacts, were also subtracted from the total calculated resistances for the rough copper wafers. This left five rough surface contacts.

\[ R_{TC} = \left( \frac{0.90 \times 1.6}{22.9 \times 10^{-3}} - 8.7 - 2 \times 9.6 \right) \frac{1}{2} = \frac{7.1}{\text{cm}^2 \cdot \text{°C}} \text{ watt} \]

\[ R_{EC} = \left( \frac{633.0 - 625.0}{0.035} \right) \times 10^{-6} - 3.4 \times 10^{-6} - 2 \times 74.2 \times 10^{-6} \]

\[ = 42.8 \times 10^{-6} \]

\[ L = \frac{7.1}{42.8 \times 10^{-6}} = 1.66 \times 10^5 \]

Note: The values for "L" were kept in numerical units only for comparison purposes.
**APPENDIX C**

**TABLE 1**

**SUMMARY OF RATIOS OF THERMAL TO ELECTRICAL CONTACT RESISTANCE**

<table>
<thead>
<tr>
<th>Kg Load</th>
<th>Smooth Copper</th>
<th>Rough Copper</th>
<th>Smooth Brass</th>
<th>Rough Brass</th>
<th>Smooth Steel</th>
<th>Rough Steel</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2.84</td>
<td>2.10</td>
<td>3.78</td>
<td>3.34</td>
<td>0.131</td>
<td>***</td>
</tr>
<tr>
<td>5</td>
<td>1.46</td>
<td>1.86</td>
<td>2.74</td>
<td>2.62</td>
<td>0.110</td>
<td>1.0</td>
</tr>
<tr>
<td>10</td>
<td>1.29</td>
<td>1.66</td>
<td>2.50</td>
<td>2.41</td>
<td>0.124</td>
<td>0.87</td>
</tr>
<tr>
<td>15</td>
<td>1.07</td>
<td>1.63</td>
<td>2.04</td>
<td>2.16</td>
<td>0.117</td>
<td>0.80</td>
</tr>
<tr>
<td>20</td>
<td>0.99</td>
<td>1.34</td>
<td>1.95</td>
<td>1.75</td>
<td>0.161</td>
<td>0.69</td>
</tr>
<tr>
<td>25</td>
<td>0.94</td>
<td>1.17</td>
<td>1.84</td>
<td>1.55</td>
<td>0.192</td>
<td>0.72</td>
</tr>
<tr>
<td>30</td>
<td>0.74</td>
<td>1.10</td>
<td>1.61</td>
<td>1.50</td>
<td>0.196</td>
<td>0.80</td>
</tr>
<tr>
<td>35</td>
<td>0.75</td>
<td>0.79</td>
<td>1.54</td>
<td>1.50</td>
<td>0.178</td>
<td>0.94</td>
</tr>
<tr>
<td>40</td>
<td>0.66</td>
<td>0.88</td>
<td>1.41</td>
<td>1.32</td>
<td><strong>1.59</strong></td>
<td></td>
</tr>
<tr>
<td>45</td>
<td>0.63</td>
<td>0.81</td>
<td>1.55</td>
<td>1.31</td>
<td><strong>13.38</strong></td>
<td></td>
</tr>
</tbody>
</table>

* These ratios were calculated on an observed very low electrical resistance.

** Failed to get a heat meter reading.

*** Failed to get an electrical resistance reading.

\[
R_T = \frac{cm^2 \cdot ^\circ C}{\text{watts}} \quad R_E = \frac{\text{ohms}}{cm^2}
\]

Note: The above ratios are \(x10^5\).
APPENDIX D

MAY 67

Equipment assembly of experimental apparatus

MAY 67

Vacuum gage, below table, galvanometer and potentiometer on table, and vacuum ring and bellows press in the background
Nitrogen supply pipe to vacuum ring and bellows press, terminal connection box and the strain indicator on the right.

Nitrogen pressure gage and relief valve, vacuum ring, bellows press and platen heater which presses on the wafers.
Fig. 1

APPENDIX E

Load - Kilograms

Graph showing the relationship between load and electrical resistance for different materials: Rough Brass, Smooth Brass, Rough Copper, Smooth Copper, Rough Steel, and Smooth Steel.
Fig. 3

Electrical Resistance Over X1000

Smooth Steel

Rough Steel

Smooth Brass

Rough Brass

Smooth Copper

Rough Copper

* From Reference 13, p. 580
(1/16 cm² Flat Copper contacts)

Load - Kilograms